

Phenomenology of the Higgs Triplet Model with the mass difference at the LHC

Kei YAGYU (Univ. of Toyama)

M. Aoki, S. Kanemura, KY, arXiv: 1110.4625 [hep-ph]

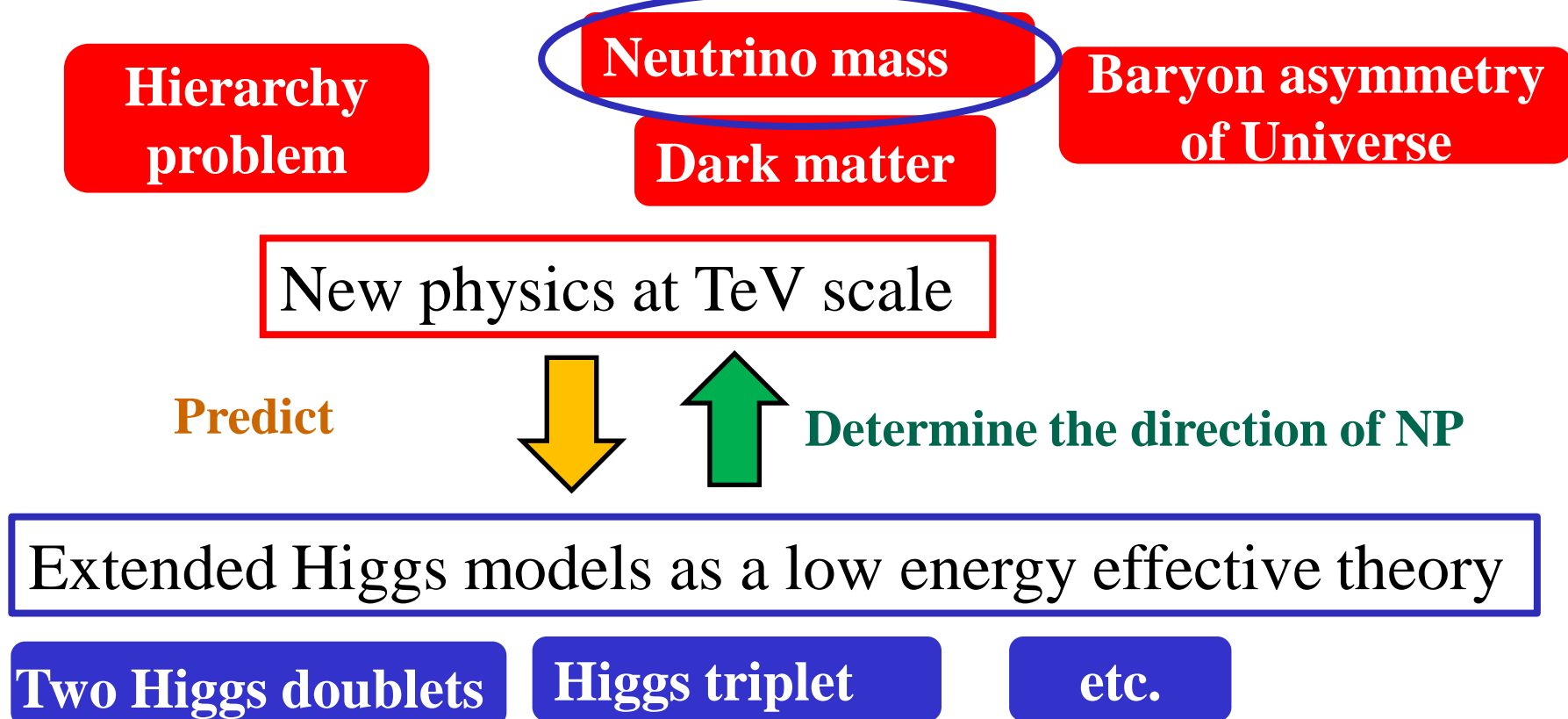
18, November 2011 KIAS Phenomenology Workshop

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- Generation mechanisms for neutrino masses
- The Higgs Triplet Model
 - Decay
 - Production
 - LHC phenomenology
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Introduction

- **Higgs sector is unknown**
 - Minimal ? or Non minimal ?
 - Higgs boson search is starting at LHC
- **Some new physics models predict extended Higgs models**



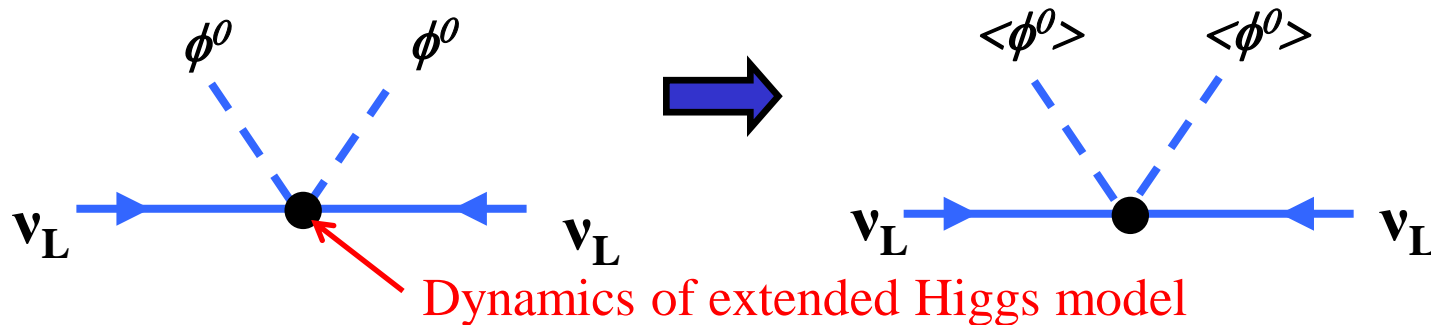
Generation mechanisms for neutrino masses

Majorana masses of neutrinos are given by the dimension 5 operator, where 2 units of lepton number are broken.

$$\mathcal{L}_{\text{eff}} = \frac{c}{M} \overline{\nu}_L^c \nu_L \phi^0 \phi^0 \quad \longrightarrow \quad m_\nu \left[\frac{c \langle \phi^0 \rangle^2}{M} \right] \overline{\nu}_L^c \nu_L$$

$\langle \phi^0 \rangle \sim 246 \text{ GeV}$
 $m_\nu \sim 0.1 \text{ eV}$
 $c/M \sim 10^{-14} \text{ GeV}^{-1}$

The Higgs boson acquires the VEV



There are scenarios, where neutrino masses generate through dynamics of **extended Higgs models**.

Ex. 1 The type II seesaw model (at the tree level)

Ex. 2 Radiative seesaw models (at the loop level)

*Cheng, Li (1980); Schechter, Valle, (1980);
 Magg, Wetterich, (1980);
 Lazarides, Shafi, Wetterich, (1981);
 Mohapatra, Senjanovic, (1981).*

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 Zee, (1986); Babu, (1988);
 Krauss, Nasri, Trodden, (2003);
 Ma, (2006); Aoki, Kanemura, Seto, (2009).*

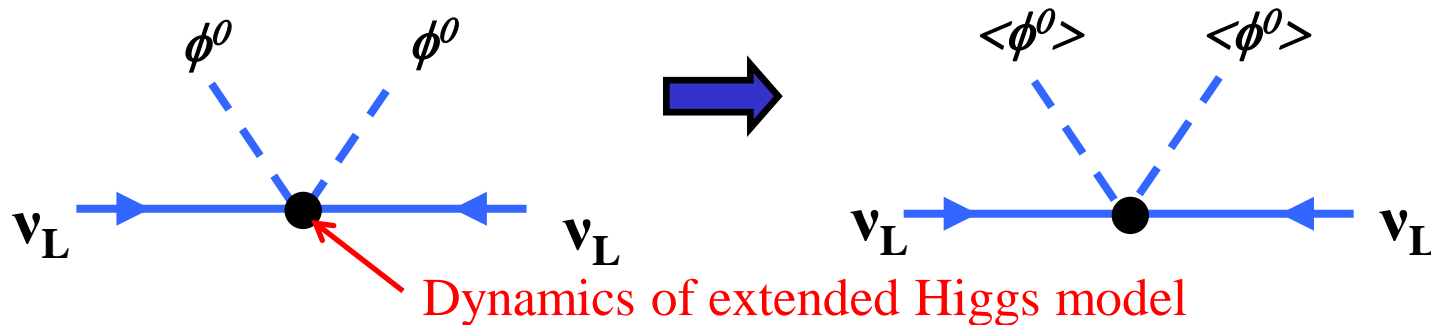
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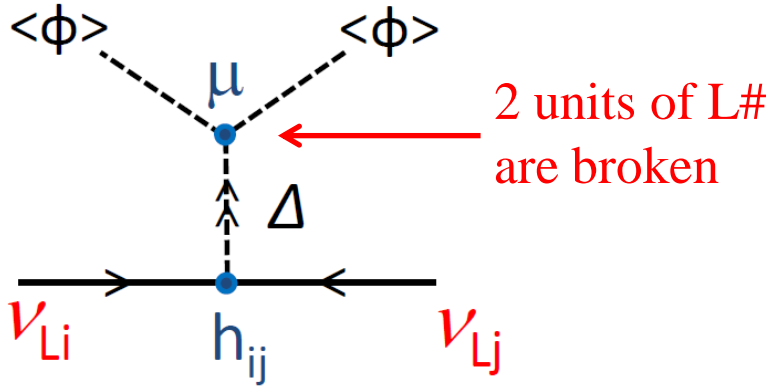
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Type II seesaw model (Higgs Triplet Model)

The Higgs triplet field Δ ($Y = 1$) is added to the SM.

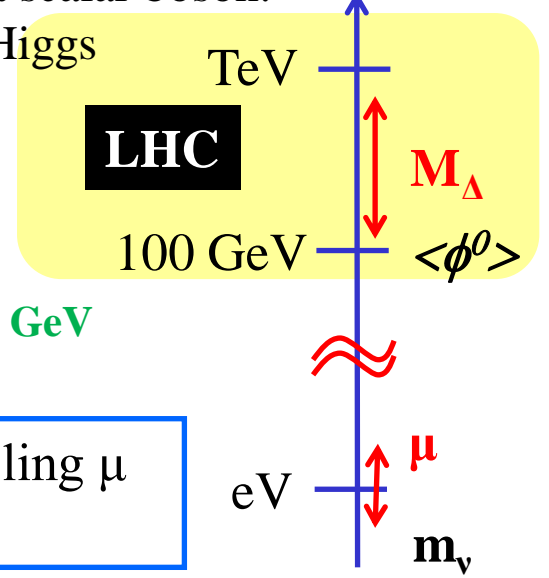
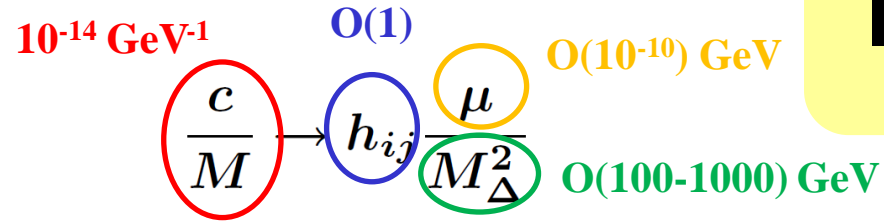
$$\mathcal{L}_{\text{typeII}} = h_{ij} \overline{L}_L^{ci} \cdot \Delta L_L^j + \mu \Phi \cdot \Delta^\dagger \Phi + \dots$$

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_L$
Φ	1	2	+1/2	0
Δ	1	3	+1	2



$$(m_\nu)_{ij} = h_{ij} \frac{\mu \langle \phi^0 \rangle^2}{M_\Delta^2} = h_{ij} v_\Delta$$

M_Δ : Mass of the Triplet scalar boson.
 v_Δ : VEV of the triplet Higgs



When we consider the TeV scale M_Δ , the L# violating coupling μ has to be of $O(10^{-10})$ GeV.

The Higgs Triplet Model (HTM)

The Higgs potential

$$V = m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i\tau_2 \Delta^\dagger \Phi + \text{h.c.}] \\ + \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[(\Delta^\dagger \Delta)^2] \\ + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi.$$

$$\Phi = \begin{bmatrix} \varphi^+ \\ \frac{1}{\sqrt{2}}(\varphi + v + i\chi) \end{bmatrix}$$

$$\Delta = \begin{pmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \Delta^0 & -\frac{\Delta^+}{\sqrt{2}} \end{pmatrix}$$

$$\Delta^0 = \frac{1}{\sqrt{2}}(\delta + v_\Delta + i\eta)$$

Mass eigenstates: (SM-like) **h**, (Triplet-like) **H⁺⁺, H⁺, H, A**

Mass spectrum:

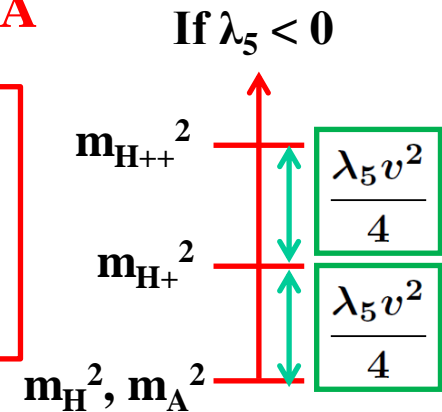
$$m_h^2 \simeq 2\lambda_1 v^2$$

$$M_\Delta^2 \equiv \frac{v^2 \mu}{\sqrt{2} v_\Delta}$$

$$m_{H^{++}}^2 \simeq M_\Delta^2 - \frac{v^2}{2} \lambda_5$$

$$m_{H^+}^2 \simeq M_\Delta^2 - \frac{v^2}{4} \lambda_5$$

$$m_A^2 \simeq m_H^2 = M_\Delta^2$$



The characteristic mass spectrum: $m_{H^{++}}^2 - m_{H^+}^2 \simeq m_{H^+}^2 - m_{\phi^0}^2$ is predicted. Measuring this spectrum, the model can be tested !

The Higgs Triplet Model (HTM)

The Higgs potential

$$\begin{aligned}
 V = & m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i \tau_2 \Delta^\dagger \Phi + \text{h.c.}] \\
 & + \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[(\Delta^\dagger \Delta)^2] \\
 & + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi.
 \end{aligned}$$

$$\Phi = \begin{bmatrix} \varphi^+ \\ \frac{1}{\sqrt{2}}(\varphi + v + i\chi) \end{bmatrix}$$

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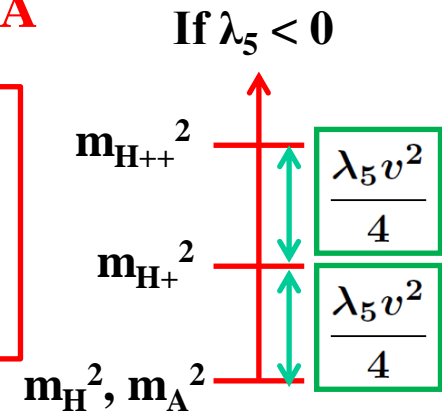
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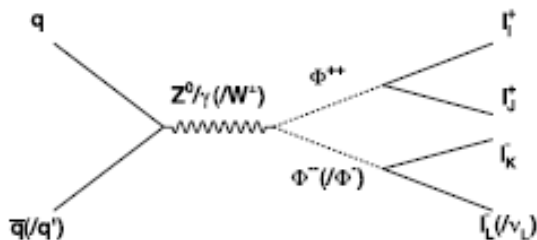


In this talk, we discuss **how we can test the HTM in the case with the mass difference** at the LHC.

Exotic Higgs Φ^{++} : EPS Results

V. Sharma, Lepton Photon 2011

- Arises in models with extra Higgs triplets
 - $\Phi^{++}, \Phi^+, \Phi^0$
- Triplet responsible for small neutrino mass
- Unknown neutrino mass matrix
 - unknown branching ratios → broad search
- Below $M \approx 2M_W$, only leptonic decays



CMS Preliminary

$$\text{BR}(\Phi^{++} \rightarrow e^+e^+) = 100\%$$

$$\text{BR}(\Phi^{++} \rightarrow e^+\mu^+) = 100\%$$

$$\text{BR}(\Phi^{++} \rightarrow \mu^+\mu^+) = 100\%$$

$$\text{BR}(\Phi^{++} \rightarrow e^+\tau^+) = 100\%$$

$$\text{BR}(\Phi^{++} \rightarrow \mu^+\tau^+) = 100\%$$

$$\text{BR}(\Phi^{++} \rightarrow \tau^+\tau^+) = 100\%$$

BP1: normal hierarchy

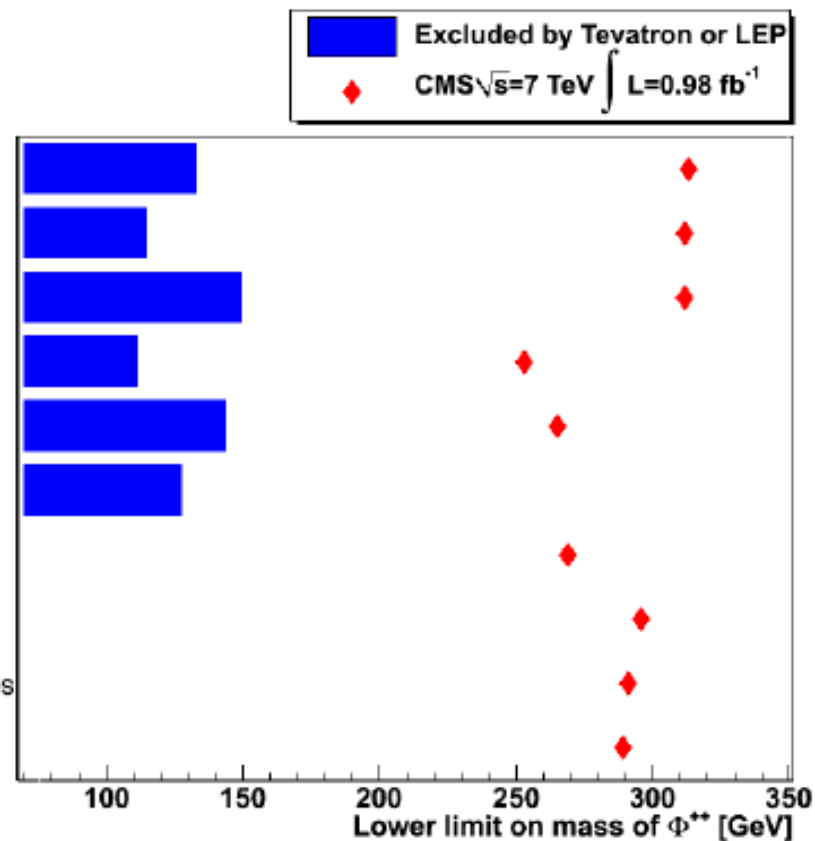
BP2: inverse hierarchy

BP3: degenerate masses

BP4: equal branchings

When $H^{++} \rightarrow l^+l^+$,
 $m_{H^{++}} > 250 - 300 \text{ GeV}$.

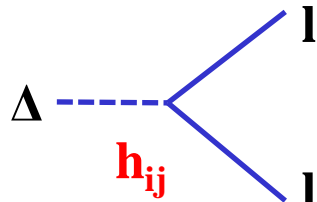
This bound cannot be applied
 when H^{++} does not decay into
 the same sign dilepton.



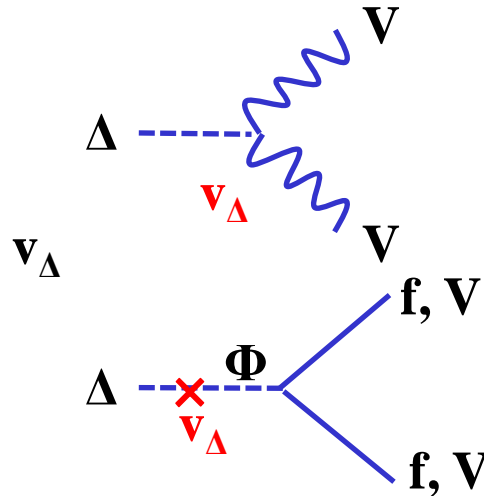
Decay

The decay of Δ -like scalar bosons can be classified into 3 modes.

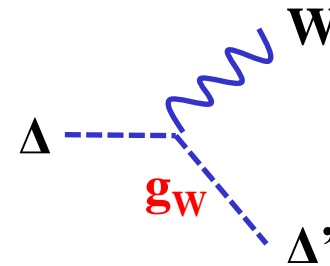
1. Decay via h_{ij}



2. Decay via v_Δ

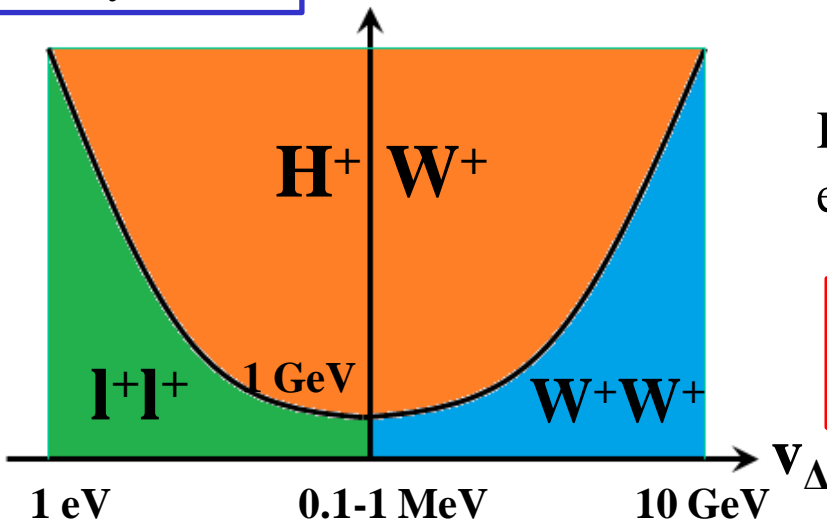


3. Decay via g_W



Decay of H^{++}

Δm

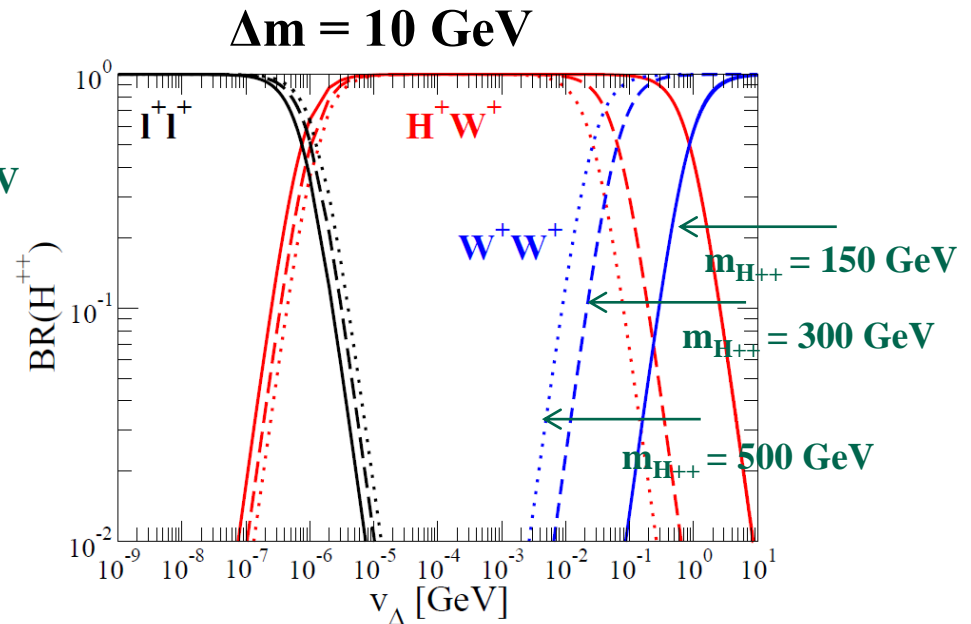
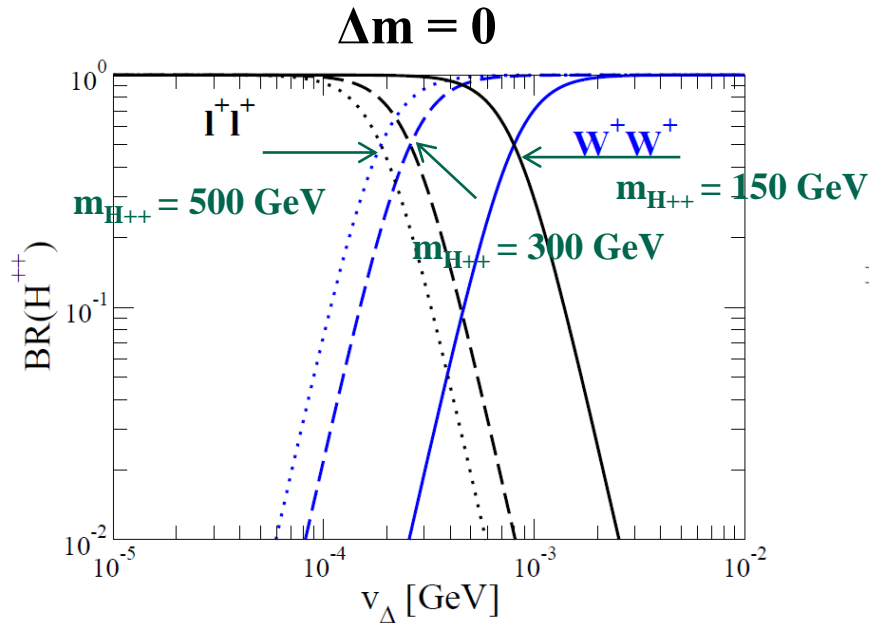


Decay modes of 1 and 2 are related to each other by the relation:

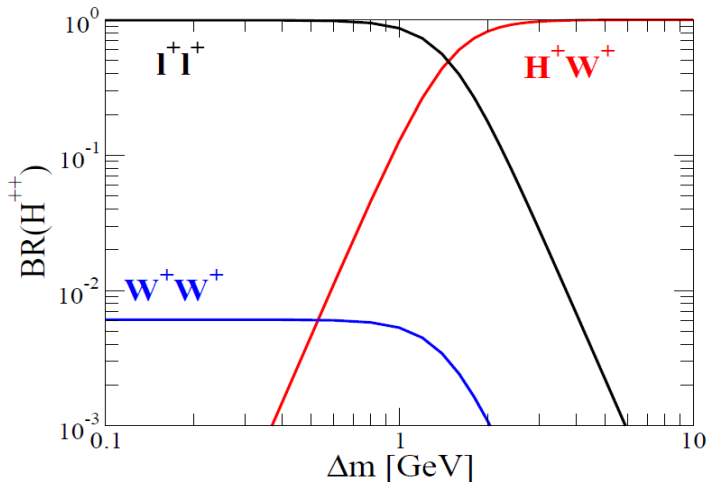
$$(m_\nu)_{ij} = h_{ij} v_\Delta$$

Decay of the triplet like scalar bosons strongly depend on v_Δ and Δm ($\equiv m_{H^{++}} - m_{H^+}$).

Branching ratio of H^{++}



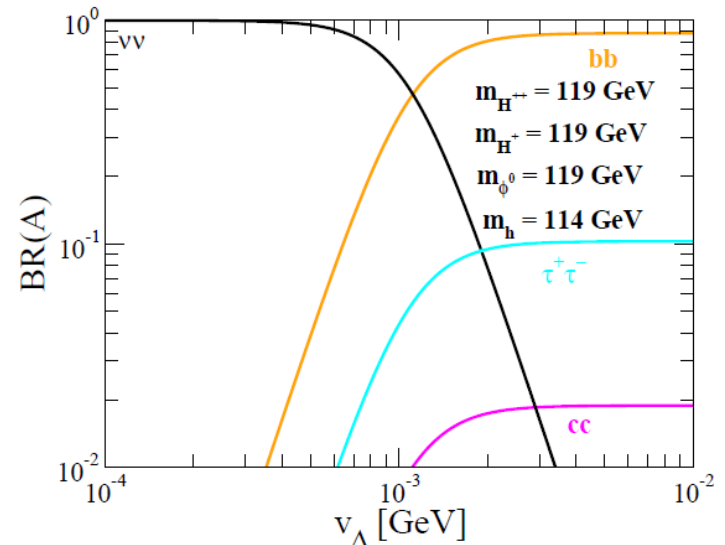
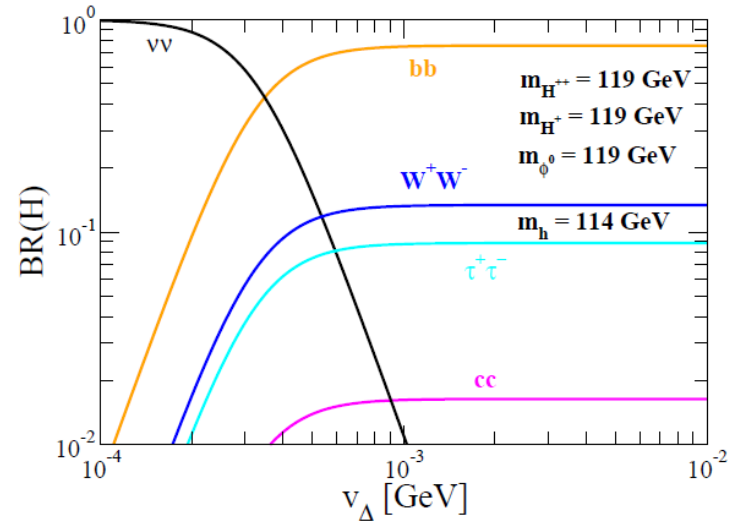
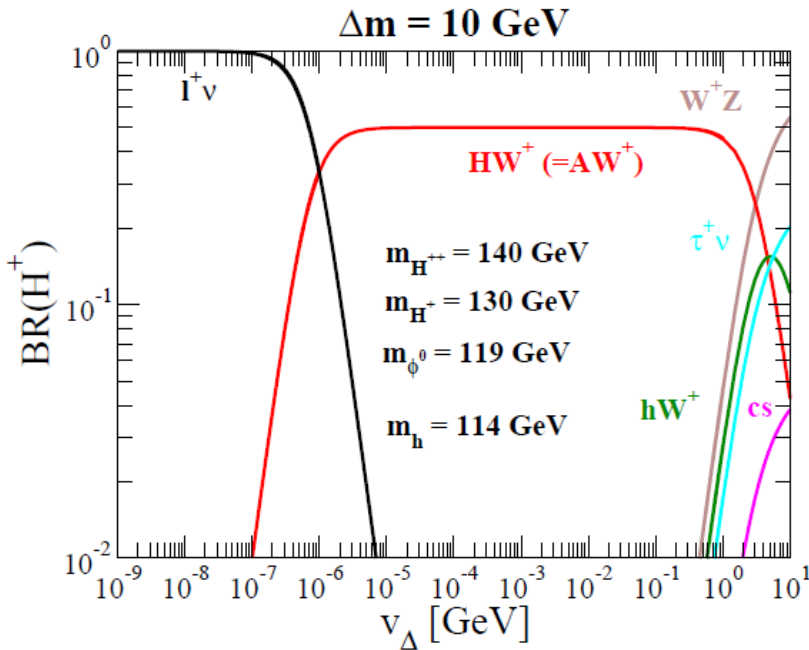
$v_{\Delta} = 0.1 \text{ MeV}, m_{H^{++}} = 200 \text{ GeV}$



Chakrabarti, Choudhury, Godbole, Mukhopadhyaya, (1998);
 Chun, Lee, Park, (2003);
 Perez, Han, Huang, Li, Wang, (2008);
 Melfo, Nemevsek, Nesti, Senjanovic, (2011)

Phenomenology of $\Delta m \neq 0$ is drastically different from that of $\Delta m = 0$.

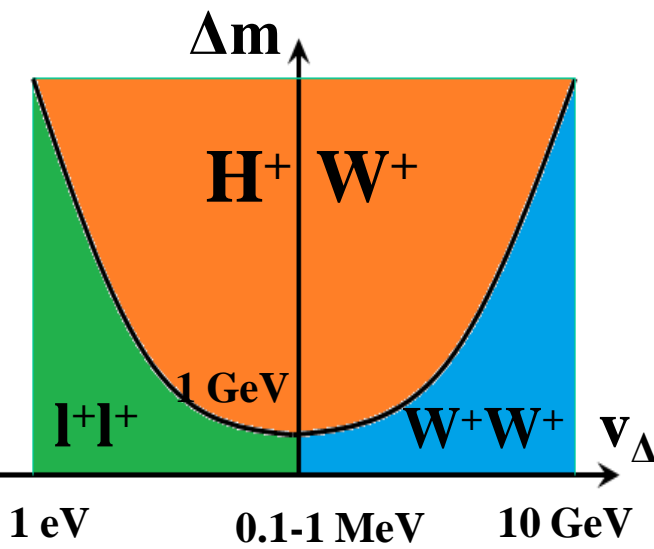
Branching ratios of H^+ , H and A



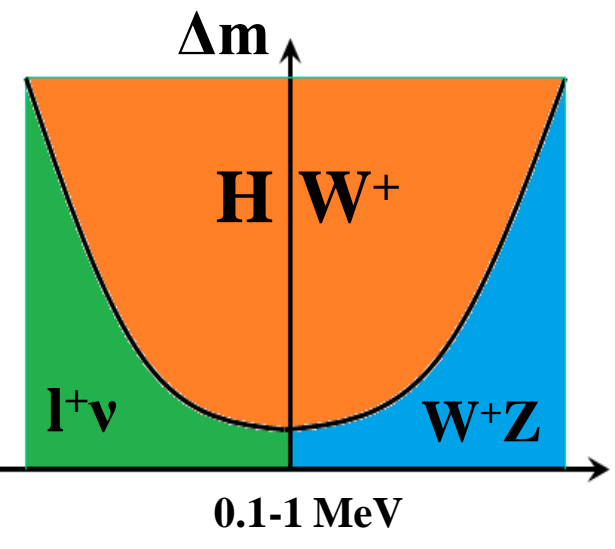
- ★ The $H^+ \rightarrow \phi^0 W^+$ mode can be dominant in the case of $\Delta m \neq 0$.
- ★ The $\phi^0 \rightarrow bb$ mode can be dominant when $v_\Delta > \text{MeV}$.

Light Δ [O(100) GeV] Scenario

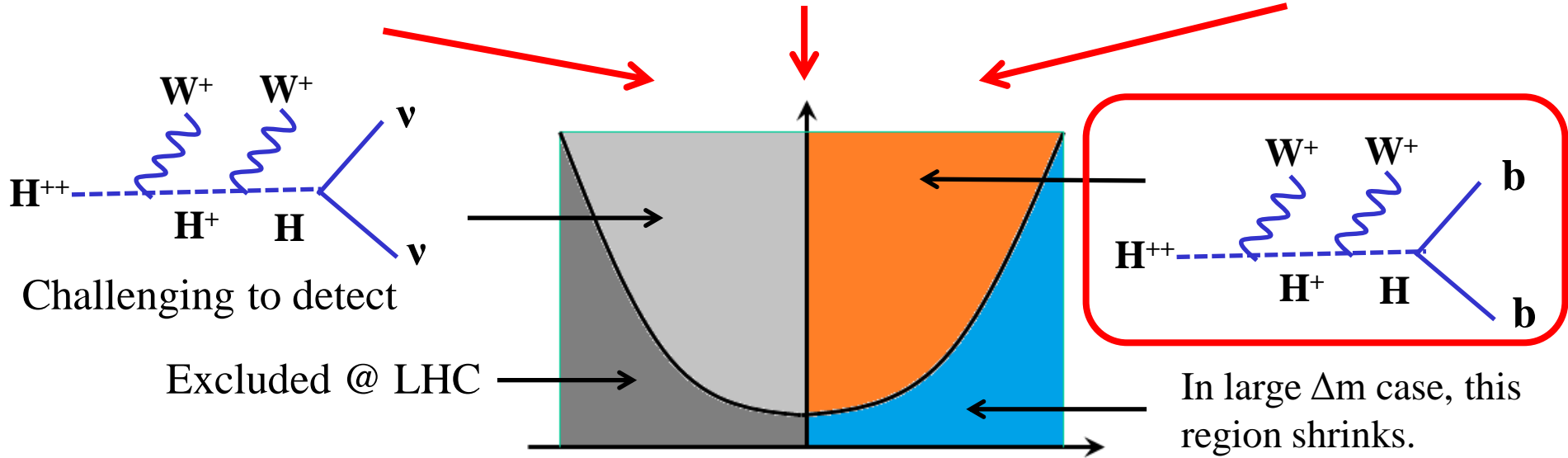
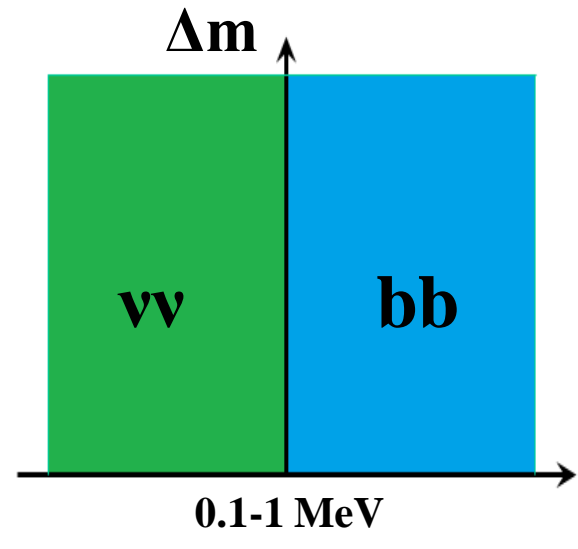
Decay of H^{++}



Decay of H^+



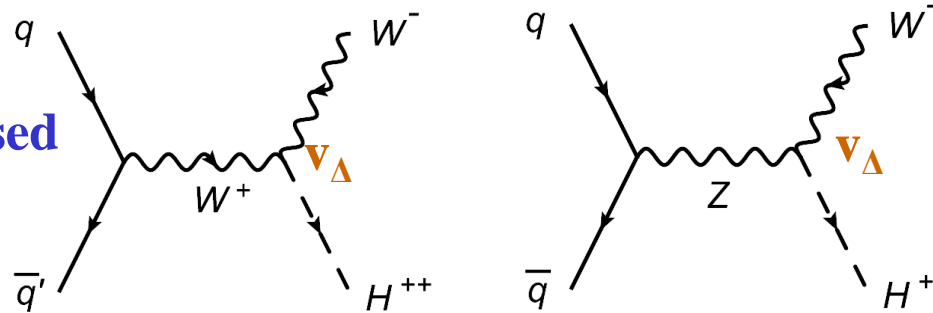
Decay of H or A



Production mechanisms at LHC

W associate

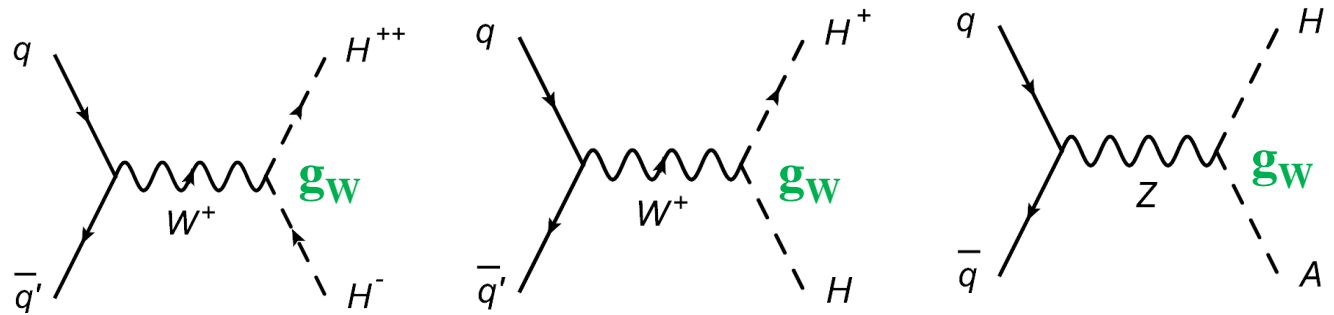
- depends on $v_\Delta \rightarrow$ **Suppressed**



Main production process

Drell-Yan

- depends on g_W



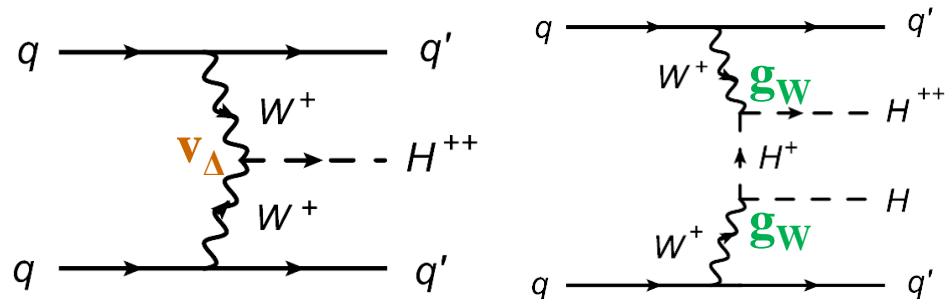
Vector Boson Fusion

- depends on $v_\Delta \rightarrow$ **Suppressed**

- depends on g_W ,

but unitary cancellation works

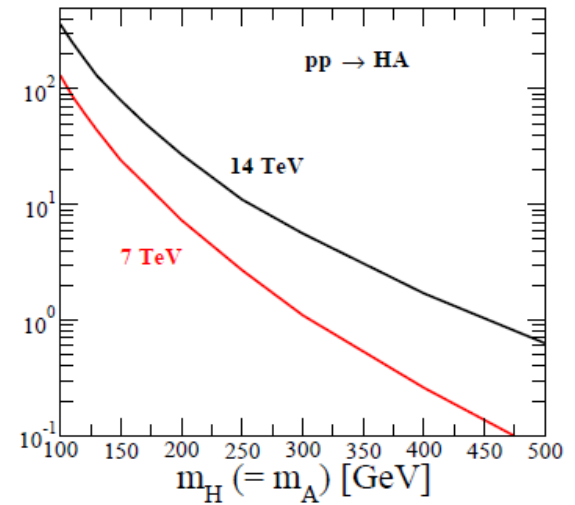
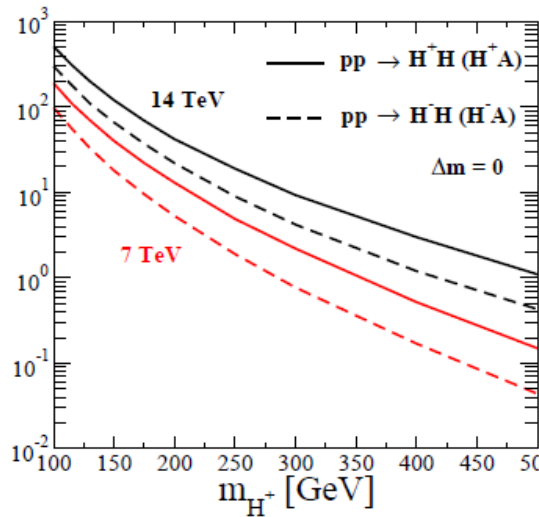
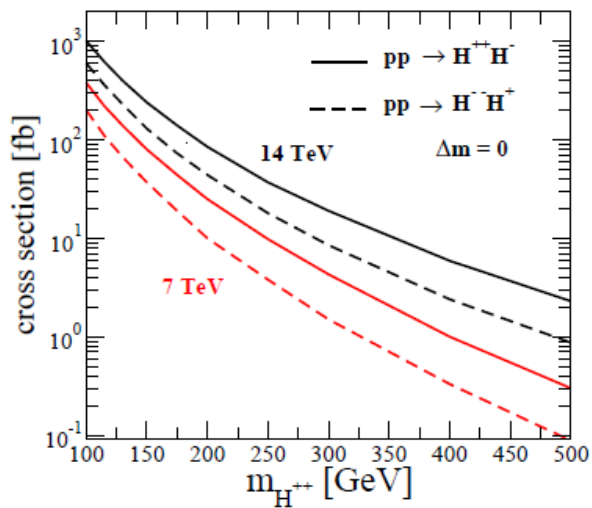
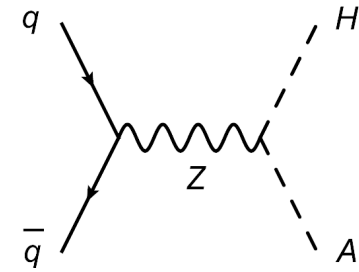
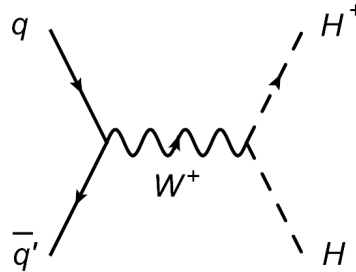
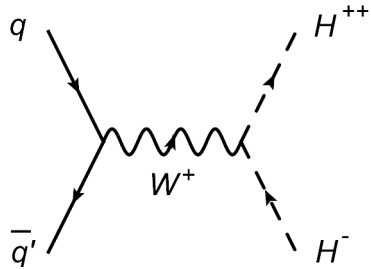
\rightarrow **Suppressed**



Production cross sections

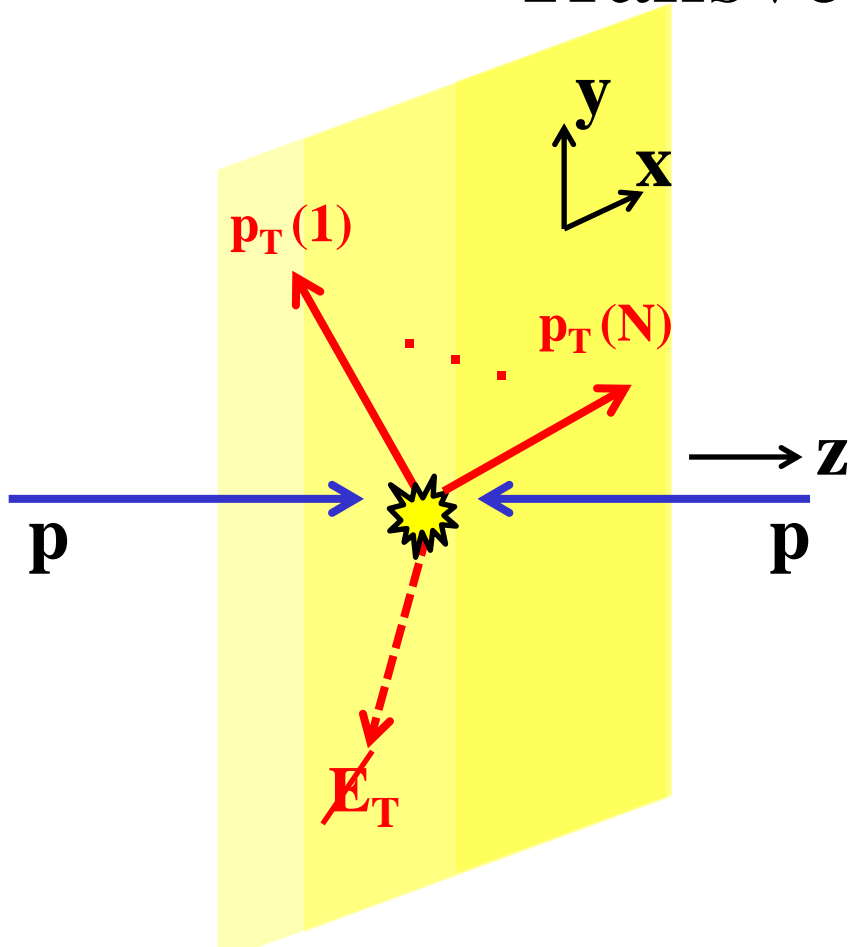
Akeroyd, Aoki, PRD72 (2005);

Perez, Han, Huang, Li, Wang, PRD78 (2008).



The magnitude of these production cross sections is around 1-100 fb.

Transverse mass



Missing transverse energy:

$$\cancel{E}_T = - \sum_i^N p_T(i)$$

Transverse mass:

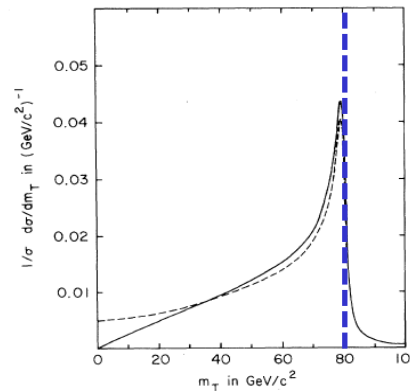
φ : azimuthal angle
 $p_T = p_T(a) + p_T(b) + \dots$

$$M_T^2 = (\cancel{E}_T + p_T)^2$$

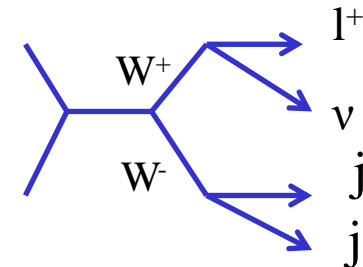
$$\simeq 2|\cancel{E}_T||p_T|(1 - \cos \varphi)$$

Smith, Neerven, Vermaseren, PRL50, 1983

Ex. The W boson mass reconstruction



This endpoint shows the W boson mass.



By using transverse mass distribution,
 the masses of Δ -like scalar bosons can be reconstructed.

Mass reconstruction

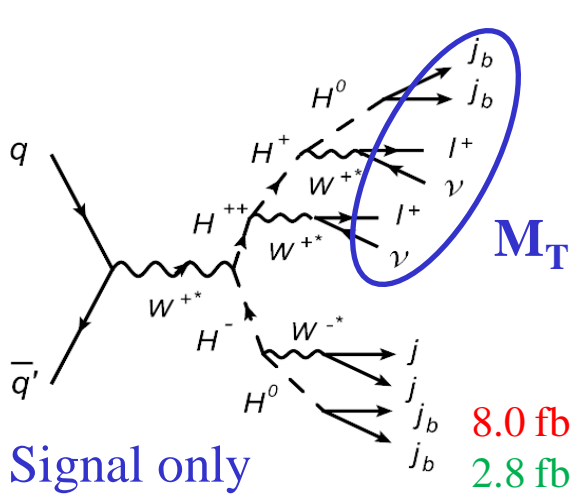
H^{++}	↑	140 GeV
H^+	—	130 GeV
H, A	—	119 GeV
h	—	114 GeV

$$v_\Delta = 10^{-2} \text{ GeV}$$

$$qq' \rightarrow H^{++}H^- \rightarrow (l^+l^+ \nu \nu b b)(jjbb)$$

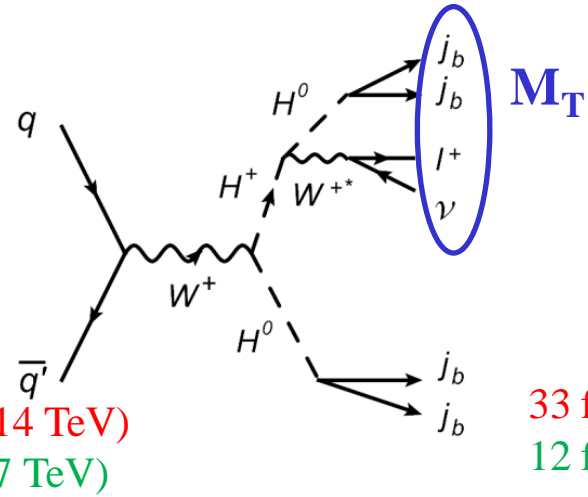
$$qq' \rightarrow H^+H \rightarrow (l^+ \nu b b)(bb)$$

$$qq \rightarrow HA \rightarrow (bb)(bb)$$

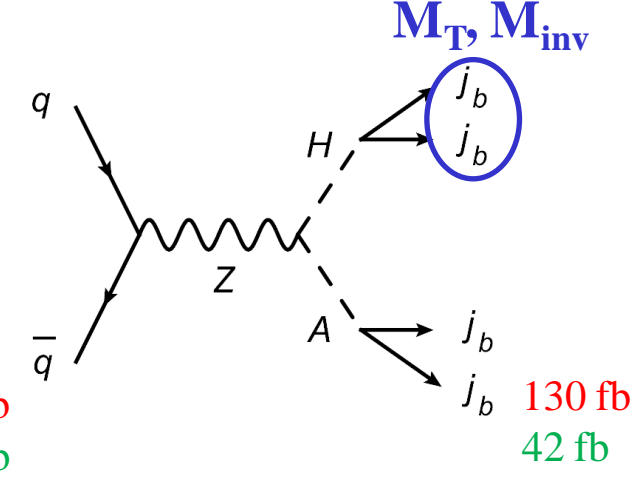


Signal only

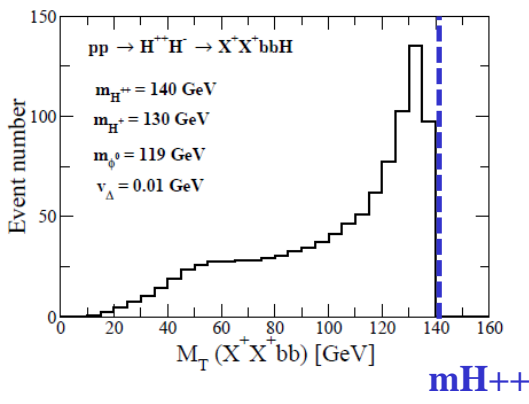
8.0 fb (14 TeV)
2.8 fb (7 TeV)



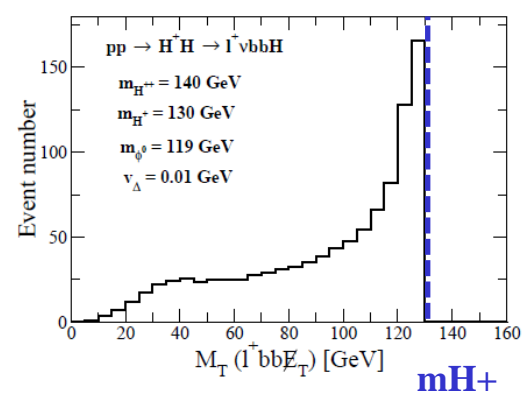
33 fb
12 fb



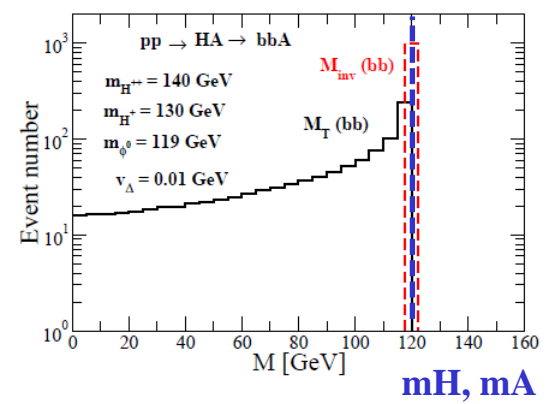
130 fb
42 fb



$m_{H^{++}}$



m_{H^+}



m_H, m_A

All the masses of the Δ -like scalar bosons may be reconstructed.

Summary

- The type II seesaw model can be explained neutrino masses, which deduces the extended Higgs model (The Higgs triplet model).
- In the Higgs triplet model, a characteristic mass spectrum appears :

$$m_{H^{++}}^2 - m_{H^+}^2 \simeq m_{H^+}^2 - m_{\phi^0}^2$$

- Phenomenology of the HTM in the case with $\Delta m \neq 0$ is drastically different from that in the case with $\Delta m = 0$ ($H^{++} \rightarrow H^+W^+ \rightarrow HW^+W^+$).

- **In our work, we focus on the characteristic mass spectrum, and we outline how the HTM can be tested in the case with $\Delta m \neq 0$ at the LHC.**
- **By measuring the transverse mass distribution and the invariant mass distribution, the masses of the Δ -like scalar bosons may be reconstructed.**

- Background simulation is the future work to clarify the feasibility.

Back up slides

Backgrounds

Signal: $pp \rightarrow H^{++}H^{-} \rightarrow (\phi^0 W^+ W^+)(\phi^0 W^-) \rightarrow \underline{(\ell^+ \ell^+ b \bar{b} E_T)}(b \bar{b} j j)$
8 fb

Backgrounds:

(A): $pp \rightarrow t \bar{t} W^+ W^- \rightarrow (b W^+)(\bar{b} W^-) W^+ W^- \rightarrow \underline{(b \ell^+ \nu)(\bar{b} j j)(\ell^+ \nu)(j j)}$ O(10) fb

(B): $pp \rightarrow t \bar{t} W^+ W^- \rightarrow (b W^+)(\bar{b} W^-) W^+ W^- \rightarrow \underline{(b \ell^+ \nu)(\bar{b} \ell^- \nu)(j j)(j j)}$ O(10) fb

For (A), top reconstruction by the M_T and M_{inv} distributions may be used.
For (B), charge identification for leptons may be used.

Signal: $pp \rightarrow H^+ \phi^0 \rightarrow (\phi^0 W^+)(b \bar{b}) \rightarrow \underline{(\ell^+ b \bar{b} E_T)}(b \bar{b})$
33 fb

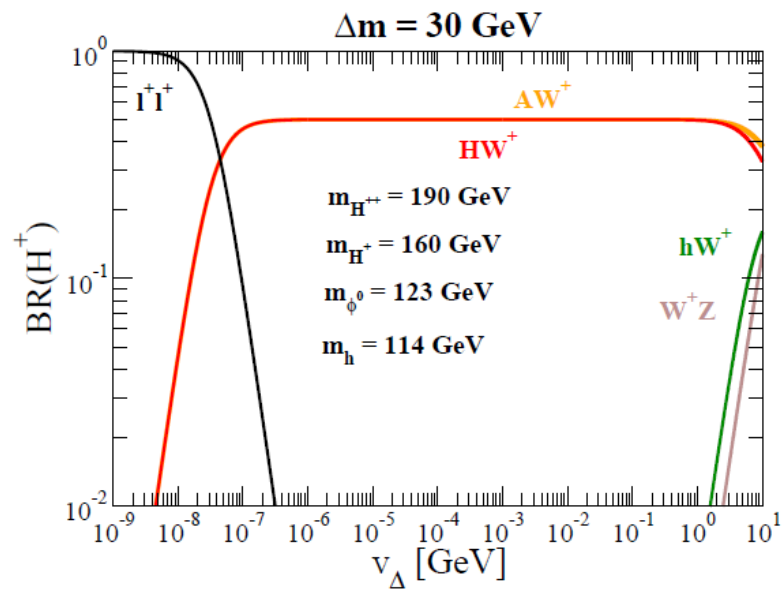
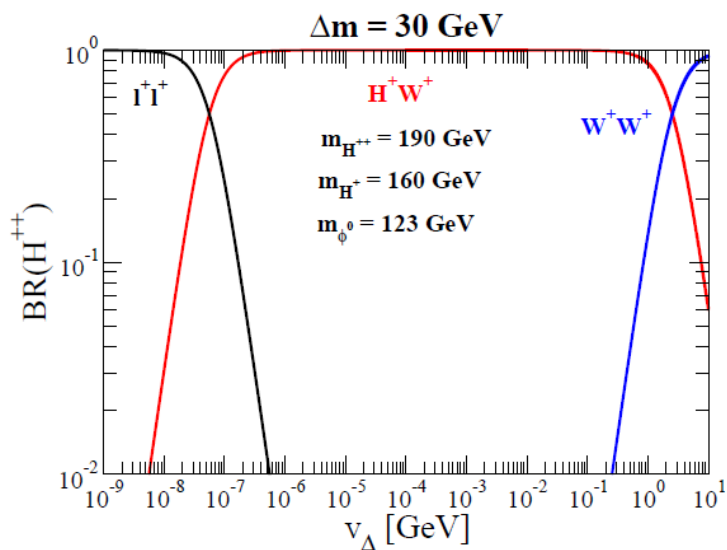
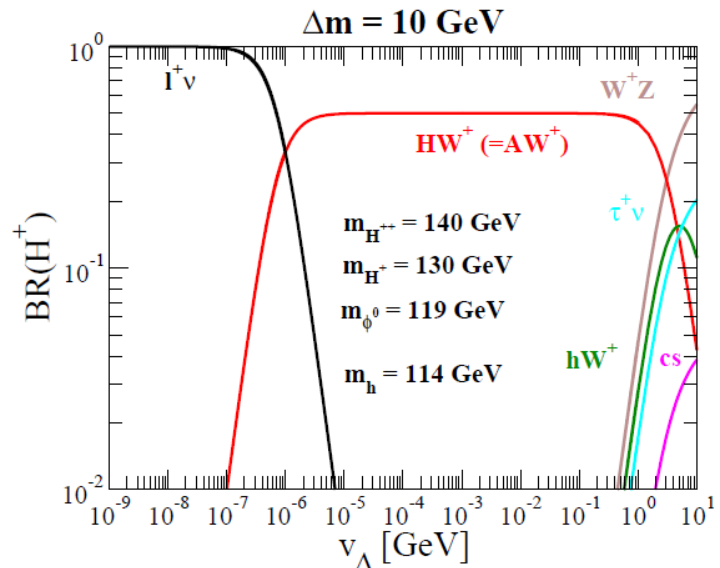
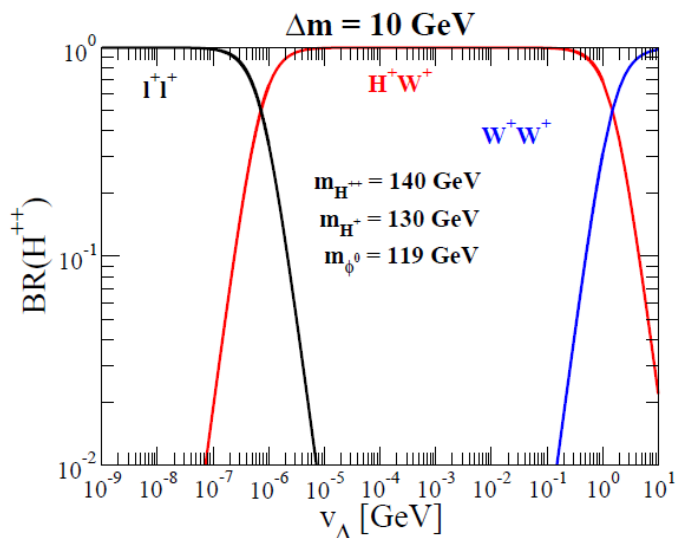
Backgrounds:

(C): $pp \rightarrow t \bar{t} \rightarrow (b W^+)(\bar{b} W^-) \rightarrow \underline{(b \ell^+ \nu)(\bar{b} j j)}$ O(1) pb

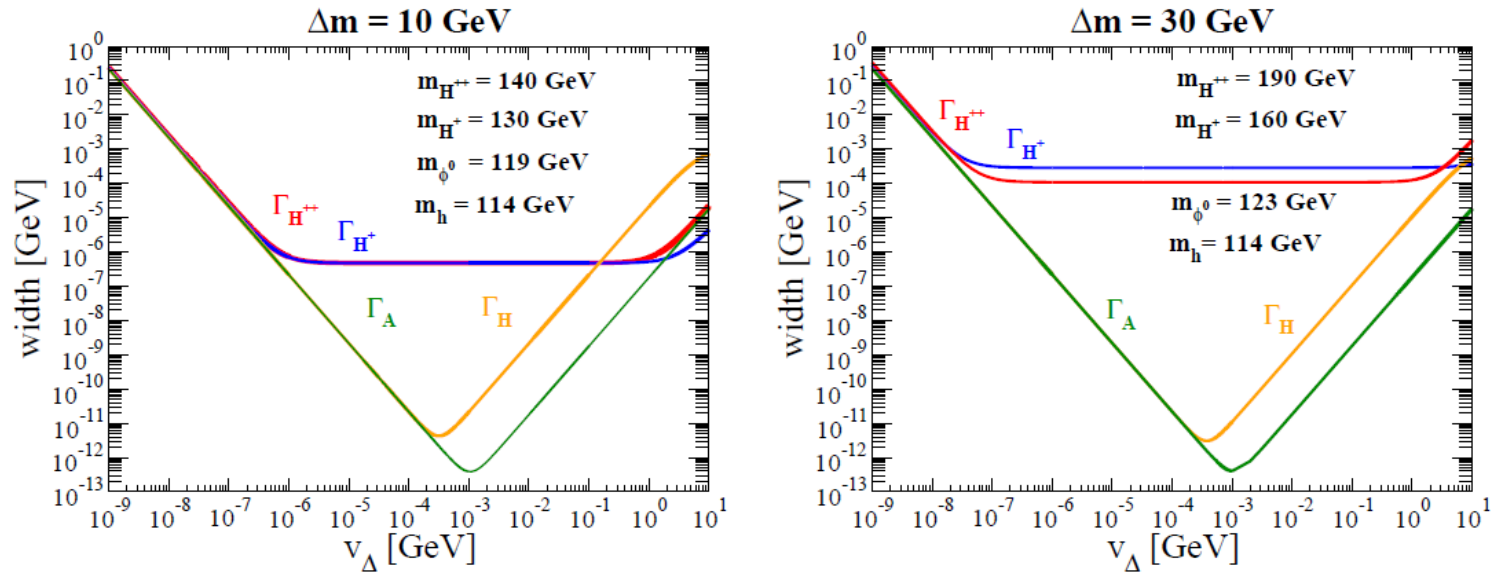
(D): $pp \rightarrow t \bar{t} \gamma^* / g^* \rightarrow (b W^+)(\bar{b} W^-)(j j) \rightarrow \underline{(b \ell^+ \nu)(\bar{b} \cancel{\ell}^- \nu)(j j)}$ O(10) fb

For (C), top reconstruction by the M_T and M_{inv} distributions may be used.
For (D), b-tagging and cut for the low E jet would be useful to reduce the BG.

Large Δm case



Decay widths for Δ -like scalar bosons



In the wide parameter regions, the decay width of the Δ -like scalar bosons is much smaller than that of top quark and massive gauge bosons.

Constraint from the rho parameter

Experimental value of rho parameter is quite close to unity: $\rho_{\text{exp}} \sim 1$

Theoretical prediction of rho parameter strongly depends on structure of Higgs sectors.

$$\rho_{\text{tree}} = \frac{\sum_i v_i^2 [T_i(T_i + 1) - Y_i^2]}{\sum_i 2Y_i^2 v_i^2}$$

Y_i : hypercharge

T_i : isospin

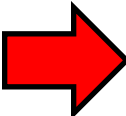
v_i : VEV

▪ Multi-doublet models

- Custodial SU(2) symmetry exists in the kinetic term of Higgs fields.
- $\rho_{\text{tree}} = 1$ is predicted.
- ★ Rho parameter deviates from unity at the 1-loop level.

▪ Models with Higgs triplets

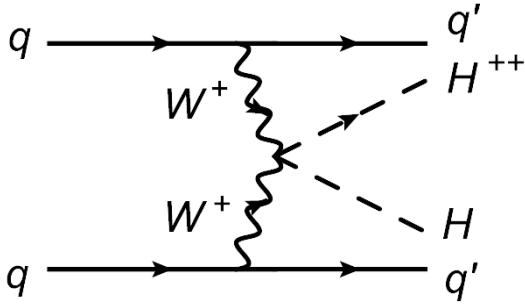
- Custodial SU(2) symmetry is broken in the kinetic term of Higgs fields
- $\rho_{\text{tree}} \neq 1$ is predicted.

- 
1. Triplet VEV is small compared with doublet VEV.
 2. Imposing alignment among triplet VEVs, custodial SU(2) symmetry is restored.

Triplet VEV is constrained from rho parameter

$$\begin{pmatrix} \varphi^\pm \\ \Delta^\pm \end{pmatrix} = R(\beta_\pm) \begin{pmatrix} w^\pm \\ H^\pm \end{pmatrix}, \quad \begin{pmatrix} \chi \\ \eta \end{pmatrix} = R(\beta_0) \begin{pmatrix} z \\ A \end{pmatrix}, \quad \begin{pmatrix} \varphi \\ \delta \end{pmatrix} = R(\alpha) \begin{pmatrix} h \\ H \end{pmatrix}, \quad R(\theta) \equiv \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

$$\cos \beta_\pm = \frac{v}{\sqrt{v^2 + 2v_\Delta^2}}, \quad \cos \beta_0 = \frac{v}{\sqrt{v^2 + 4v_\Delta^2}}, \quad \tan 2\alpha \simeq \frac{v_\Delta}{v} \frac{4M_\Delta^2 - 2v^2(\lambda_4 + \lambda_5)}{M_\Delta^2 - 2v^2\lambda_1}.$$



Model	SM with η ($Y = 0$)	SM with Δ ($Y = 1$)	SM with η and Δ
$ F ^2 =$	$\frac{4v^2 v_\eta^2}{\cos^2 \theta_W (v^2 + 4v_\eta^2)^2}$	$\frac{2v^2 v_\Delta^2}{\cos^2 \theta_W (v^2 + 2v_\Delta^2)^2}$	$\frac{4v_\Delta^2}{\cos^2 \theta_W (v^2 + 4v_\Delta^2)}$
$\rho_{\text{tree}} =$	$1 + \frac{4v_\eta^2}{v^2}$	$1 - \frac{2v_\Delta^2}{v^2 + 4v_\Delta^2}$	1

$$v_\eta = v_\Delta / \sqrt{2}$$