

# Phase fluctuation in AF order and its effect on the pseudo-gap in electron doped cuprates

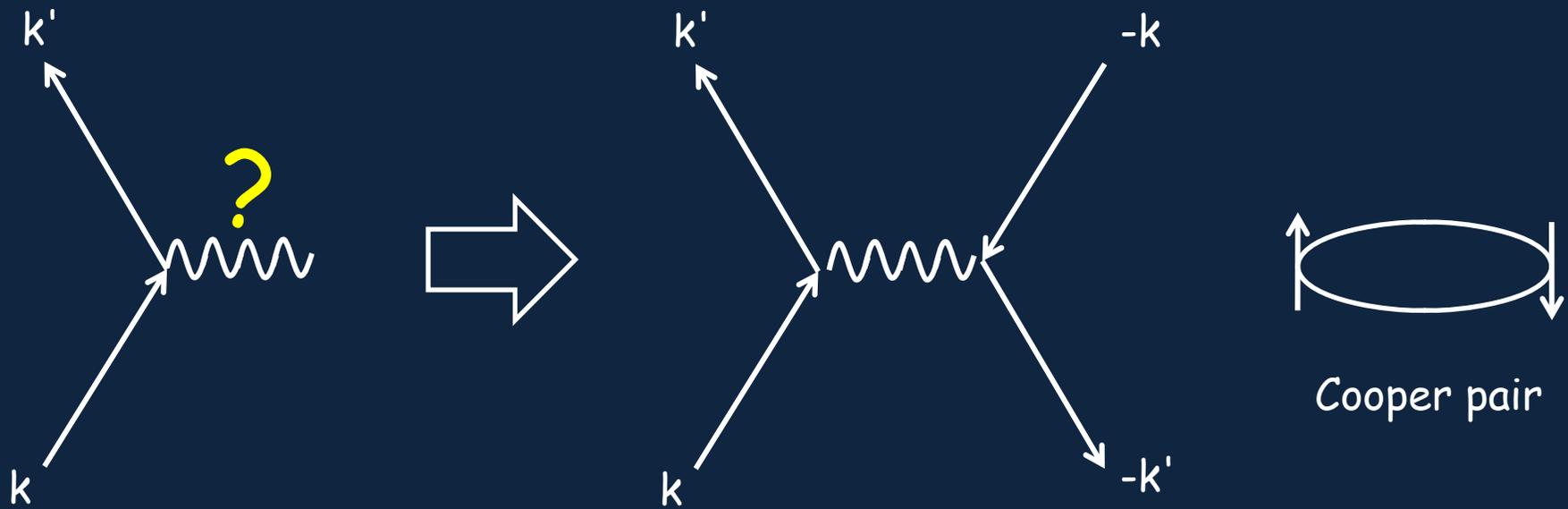
Chang Young Kim

*Yonsei University*

# Outline

1. Review
2. ARPES results
3. Spin-fermion model
4. AF phase fluctuation model
5. Conclusion

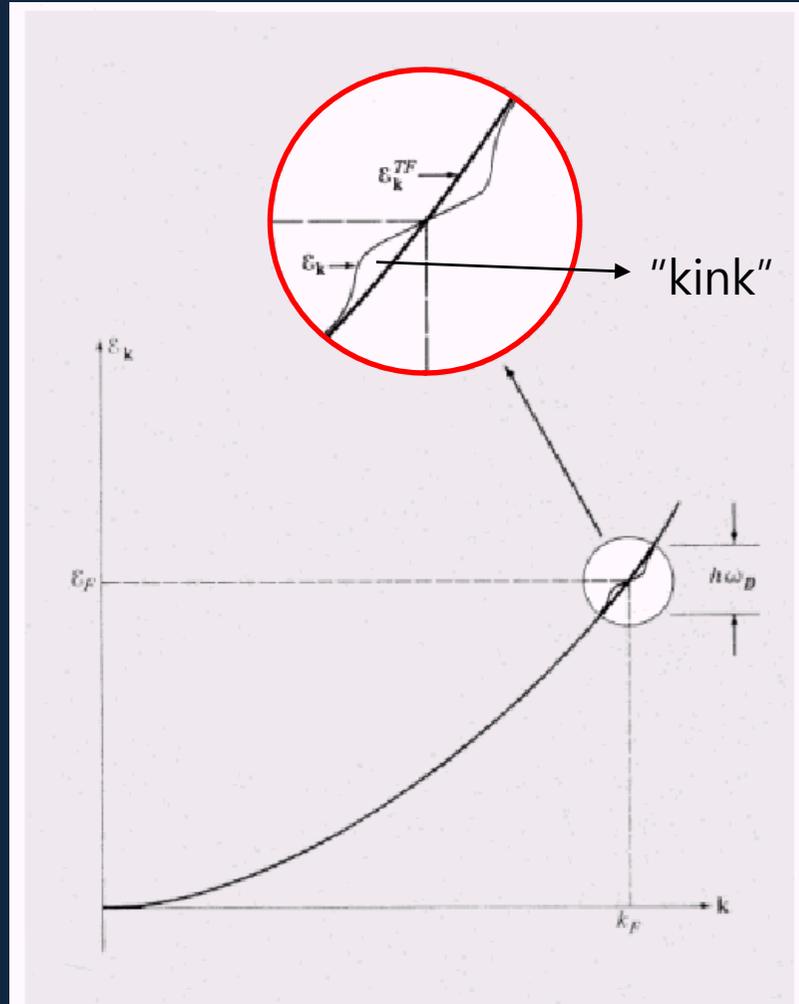
# What interacts with electrons in HTSCs?



Lattices, spins, etc

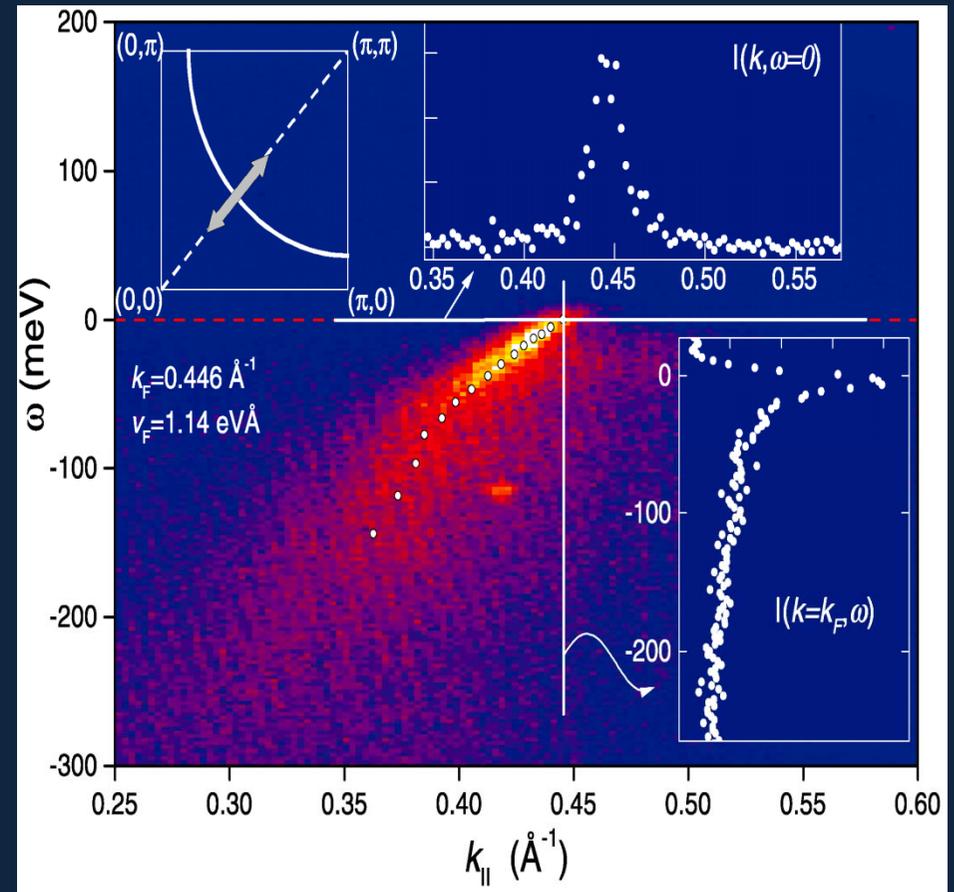
# Information in spectral functions

## Electron-phonon coupling



Ashcroft, Mermin "Solid State Physics"

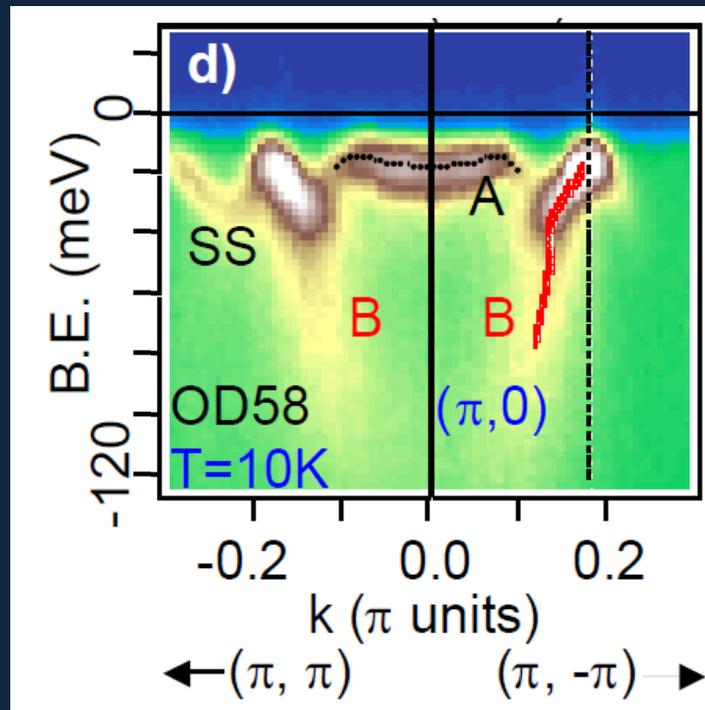
## 'kink' in the spectral function



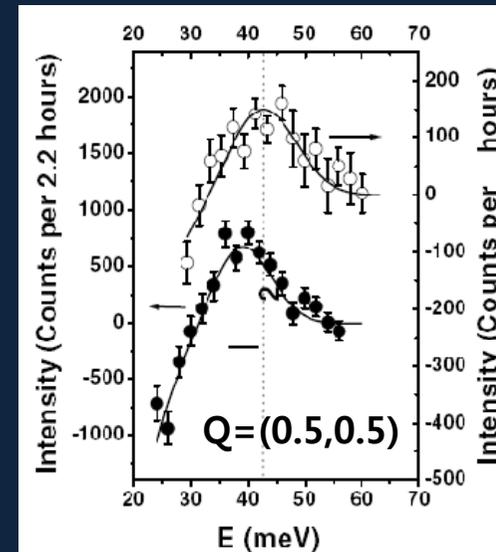
T. Valla, Science, 1999

# Controversies in h-doped HTSCs

Strong kink in Bi2212



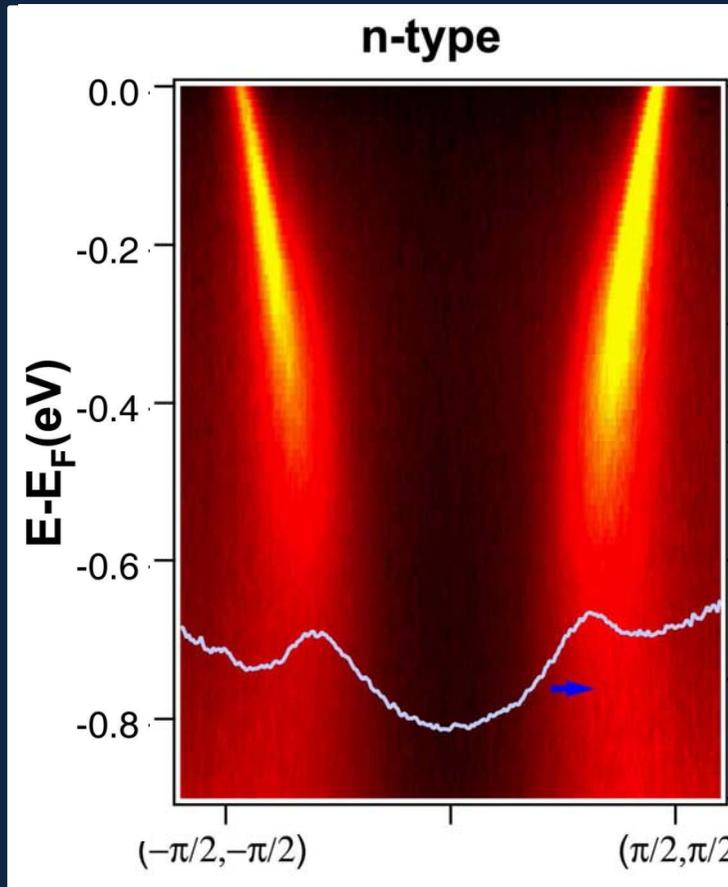
A. Gromko et al., PRB



H. He et al. PRL (2001)

- Similar energy scales
- Superconducting gap, Pseudo gap,
- Phonons, Magnetic resonance mode

# Energy scales in e-doped HTSCs

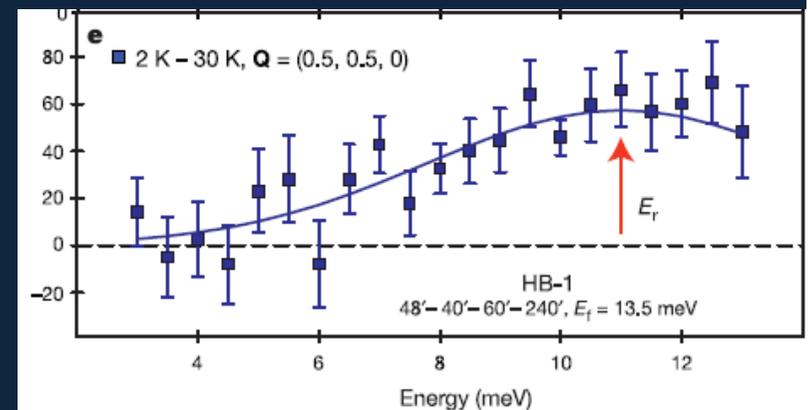


- ← Superconducting gap ( $\sim 3$  meV)
- ← Magnetic resonance mode ( $\sim 10$  meV?)
- ← Low E kink ( $\sim 50$  meV)
- ← Pseudo gap ( $\sim 100$  meV)

← High E kink ( $\sim 500$  meV)

B. Moritz et al., NJP

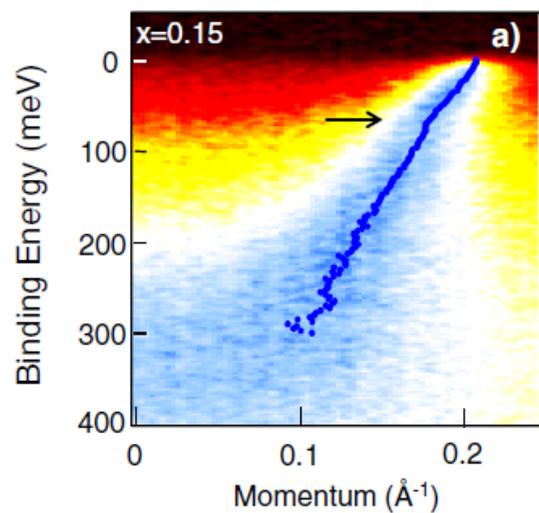
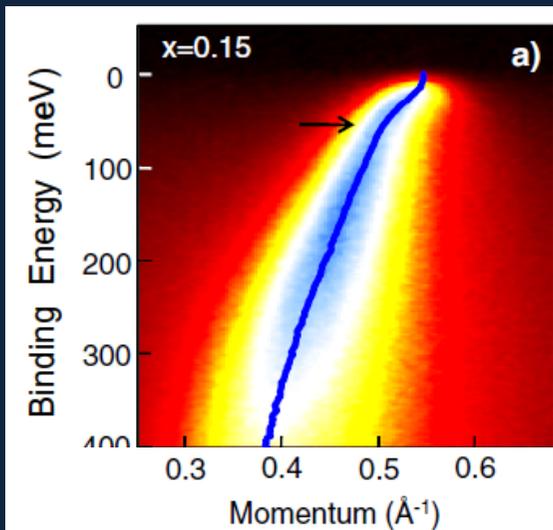
Spin resonance mode?



S. Wilson, Nature **442**, 59 (2006)

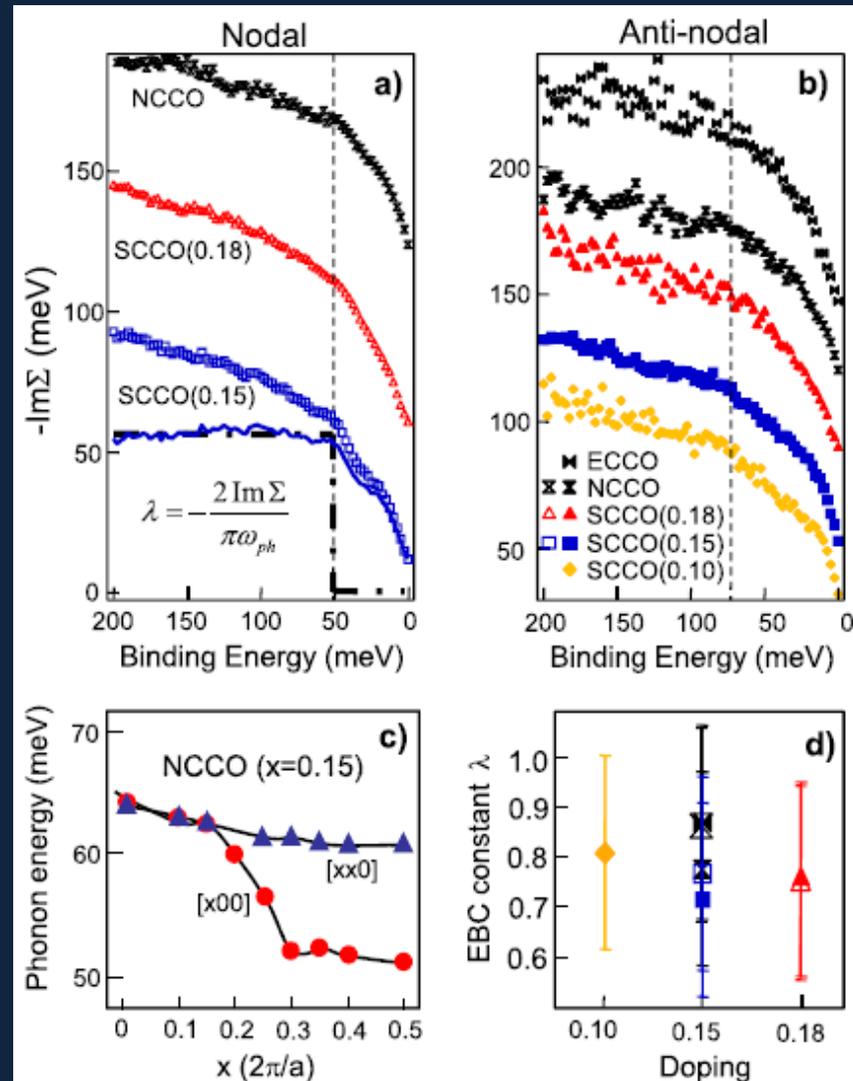
# Phonons in e-doped HTSCs

Isotropic e-phonon coupling ( S. R. Park, PRL 101, 117006 (2008) )

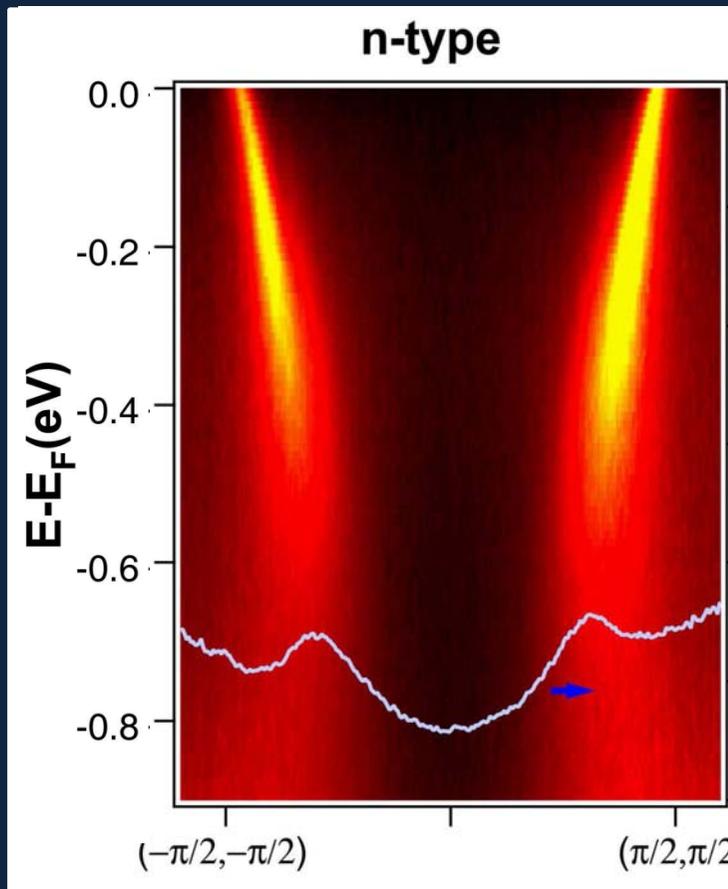


Nodal

Anti-nodal

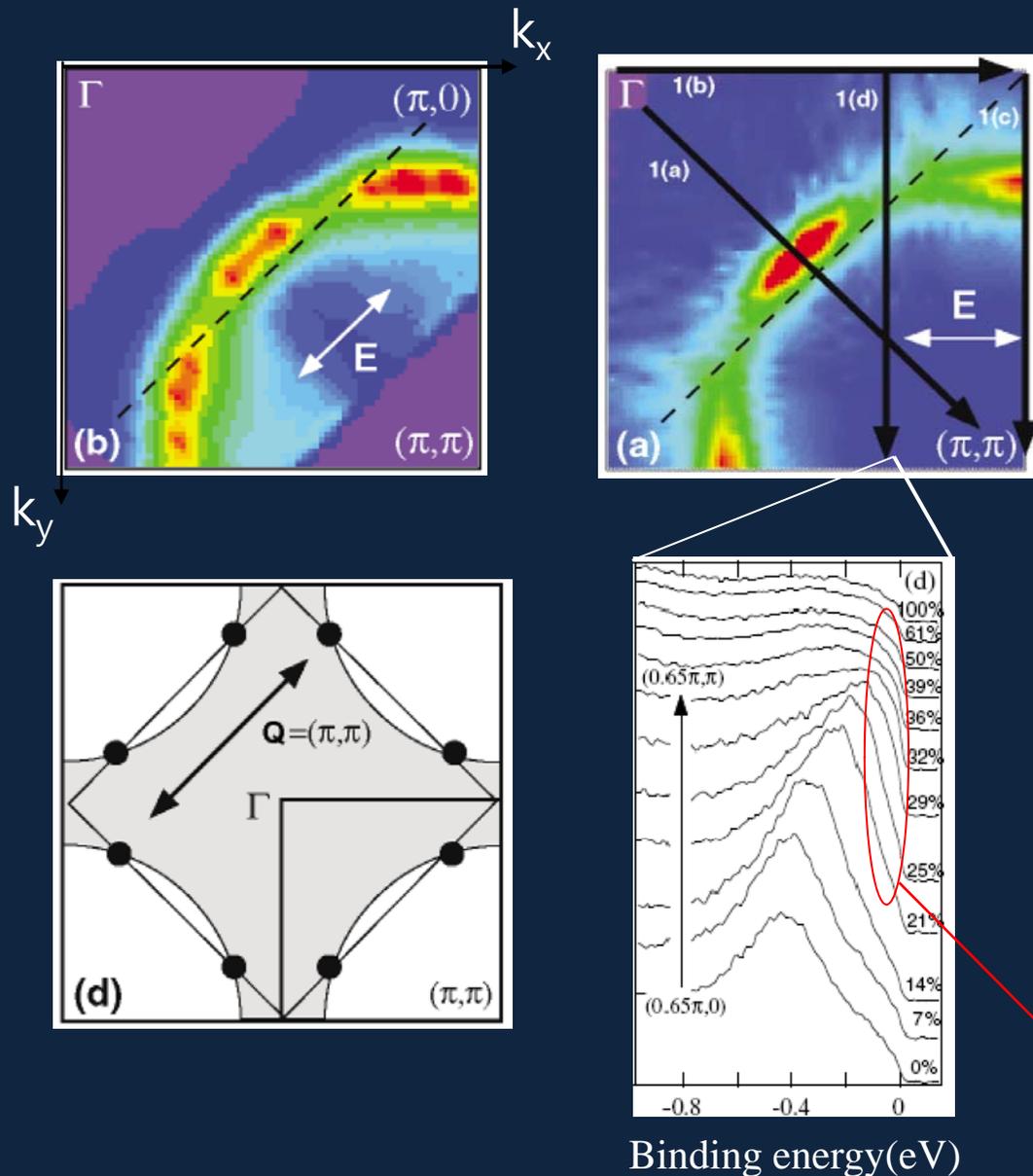


# Wish to look at pseudo-gap



- ← Superconducting gap ( $\sim 3$  meV)
- ← Spin resonance mode ( $\sim 10$  meV?)
- ← Low E kink ( $\sim 50$  meV)
- ← Pseudo gap ( $\sim 100$  meV)
- ← High E kink ( $\sim 500$  meV)

# PG in electron doped cuprates



- Spectral weight suppression near  $E_F$  at the intersection of AF Brillouin Zone Boundary (AFBZ) and the underlying FS

- Coupling to a bosonic mode localized at  $Q=(\pi, \pi)$ ?

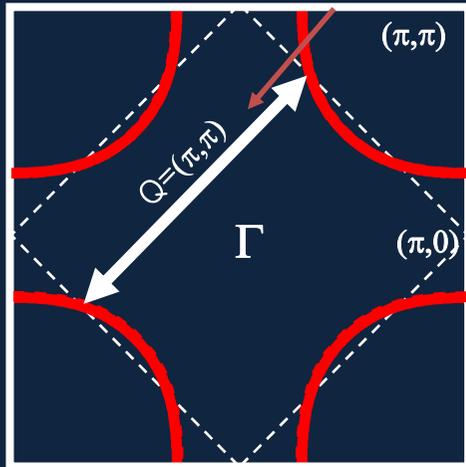
Pseudo-gap effect

N. P. Armitage

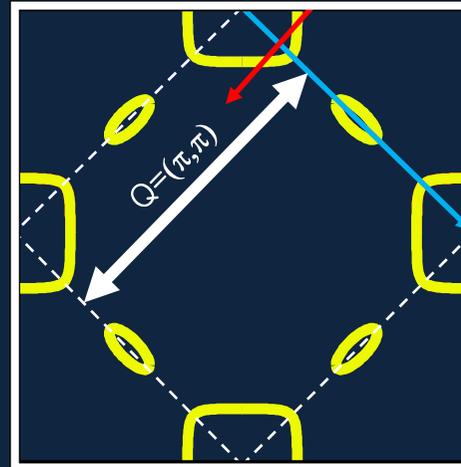
PRL (2001)

Static  $\sqrt{2} \times \sqrt{2}$  order

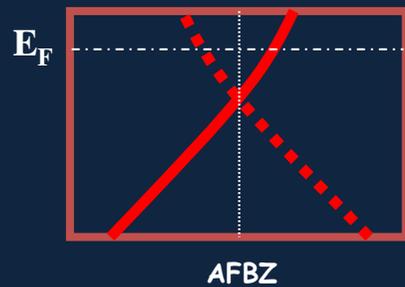
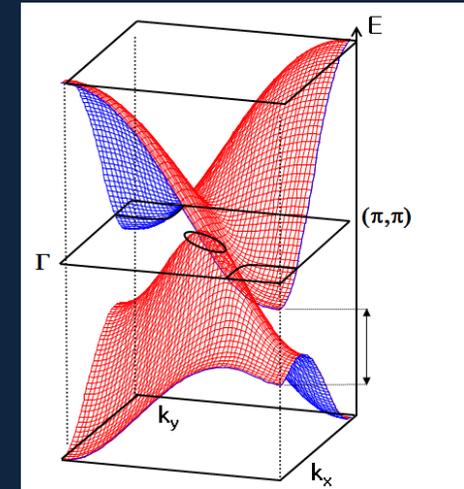
# $(\pi, \pi)$ scattering from $\sqrt{2} \times \sqrt{2}$ order?



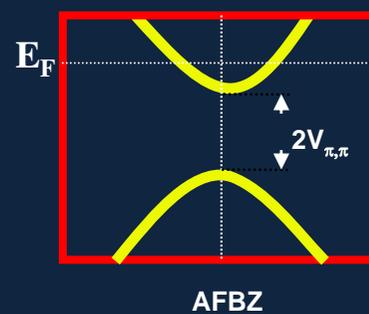
Original Fermi surface



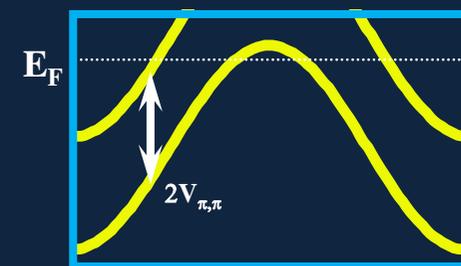
Reconstructed Fermi surface



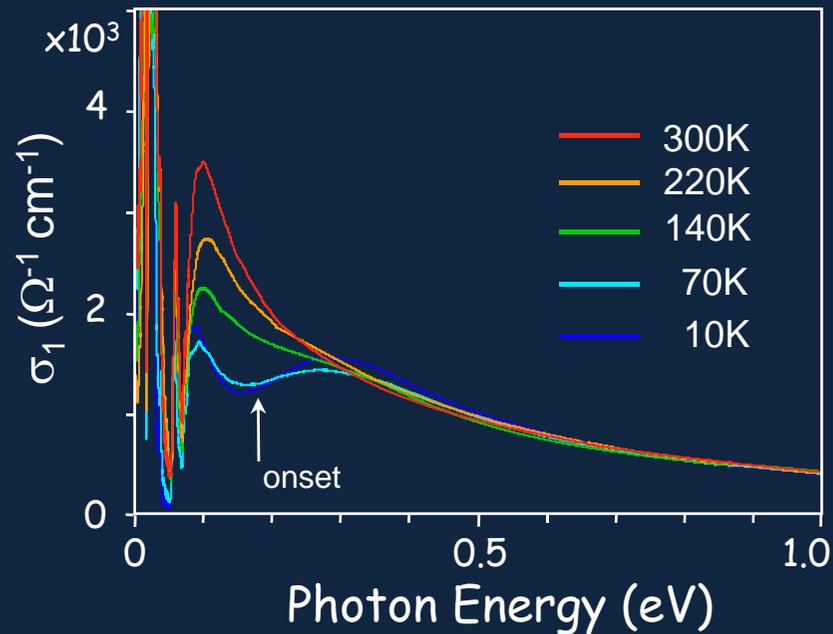
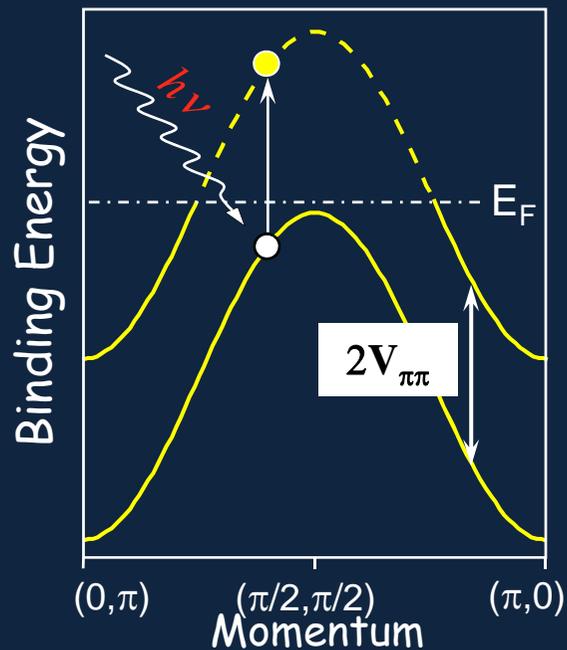
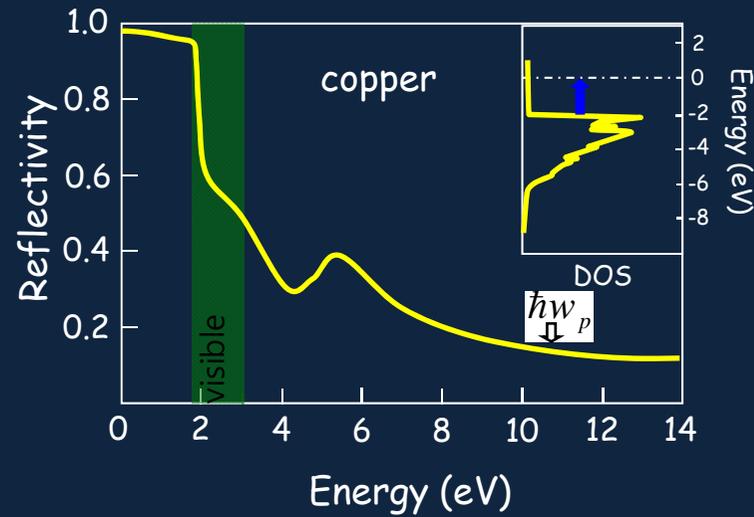
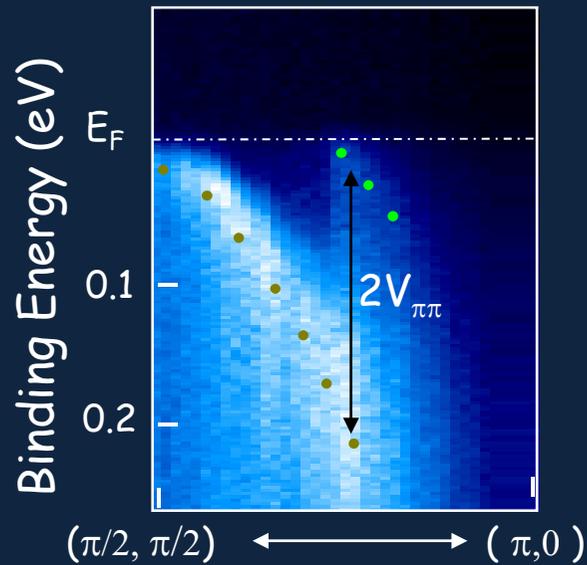
Band Structure



AFBZ



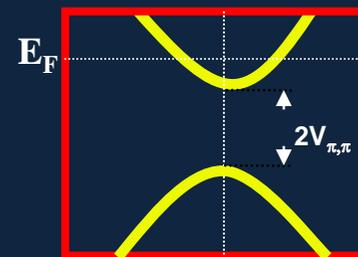
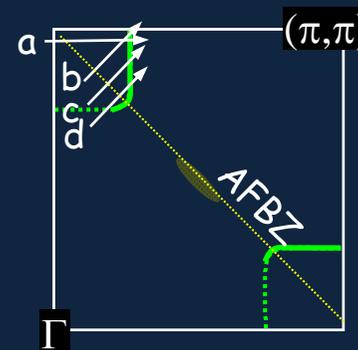
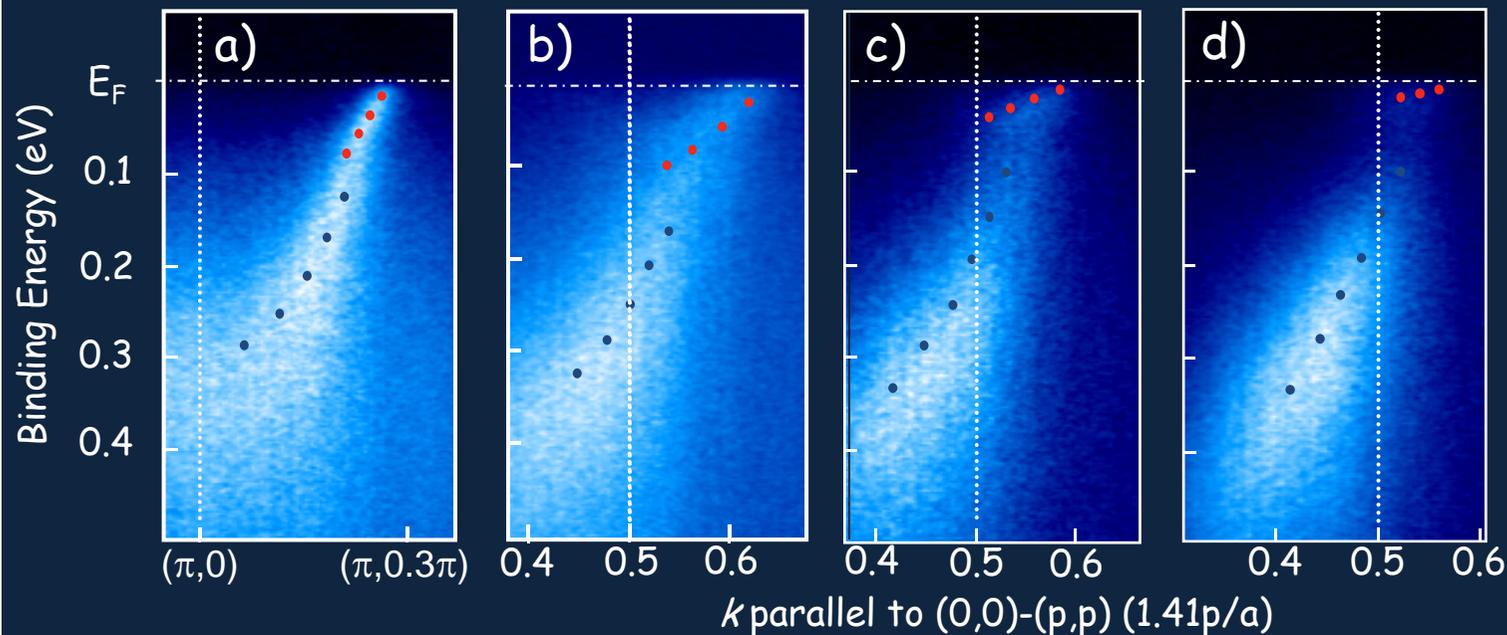
# Inter-band transition



# Overshooting problem

S. R. Park *et al.*, PRB® (2007)

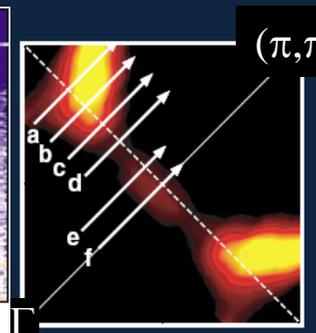
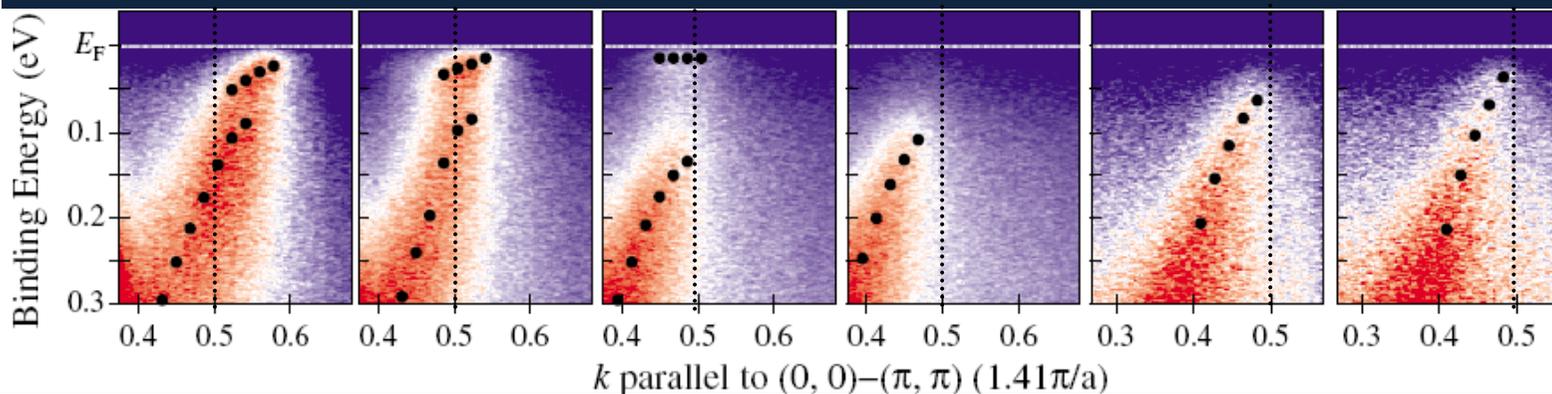
SCCO( $x=0.15$ )



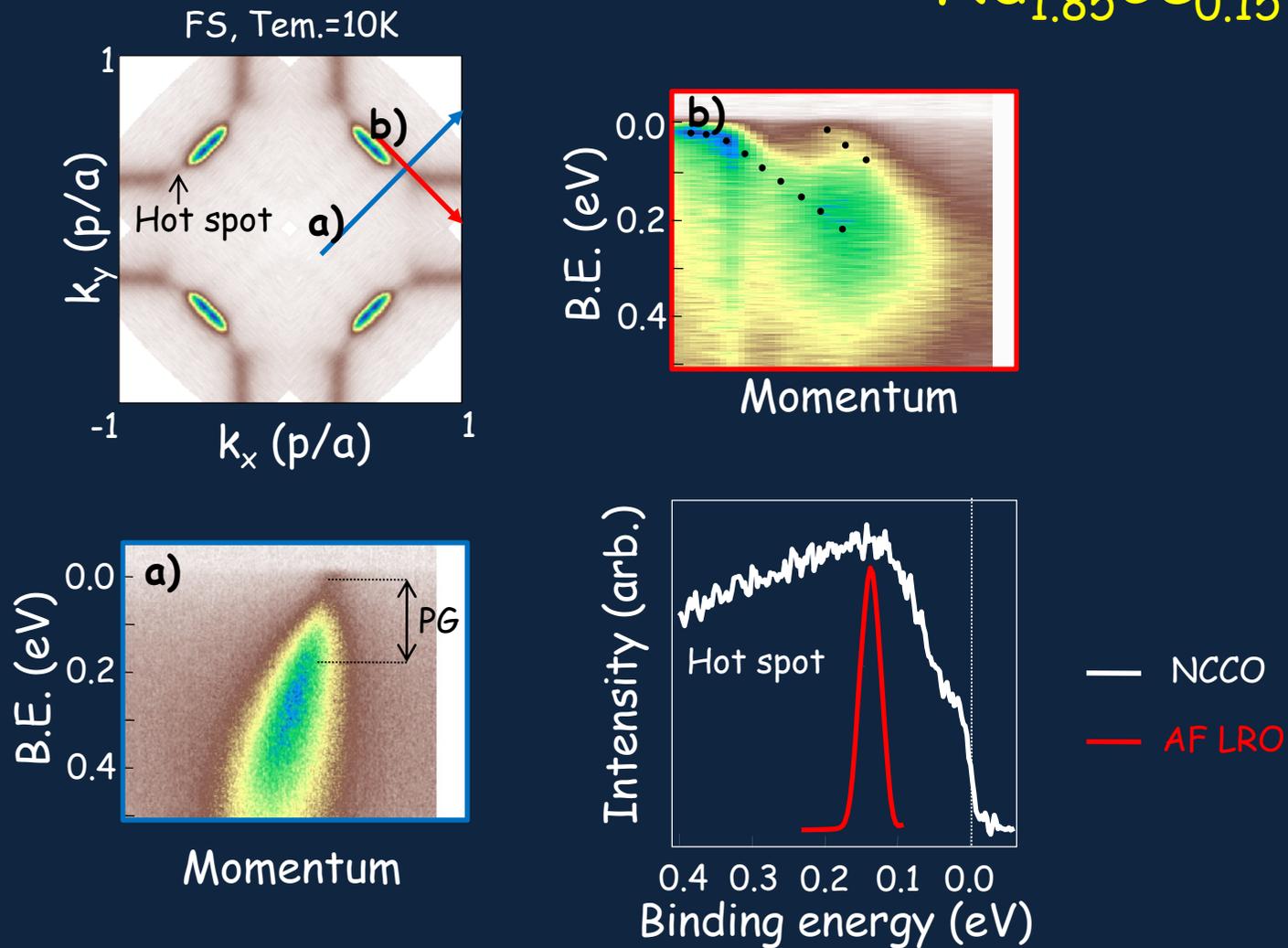
AFBZ

H. Matsui *et al.*, PRL (2005)

NCCO( $x=0.13$ )



# $E_F$ spectral weight at hot spot



Two problems:

1. Band overshoots across AFZB
2.  $E_f$  Spectral weight @ hot spot

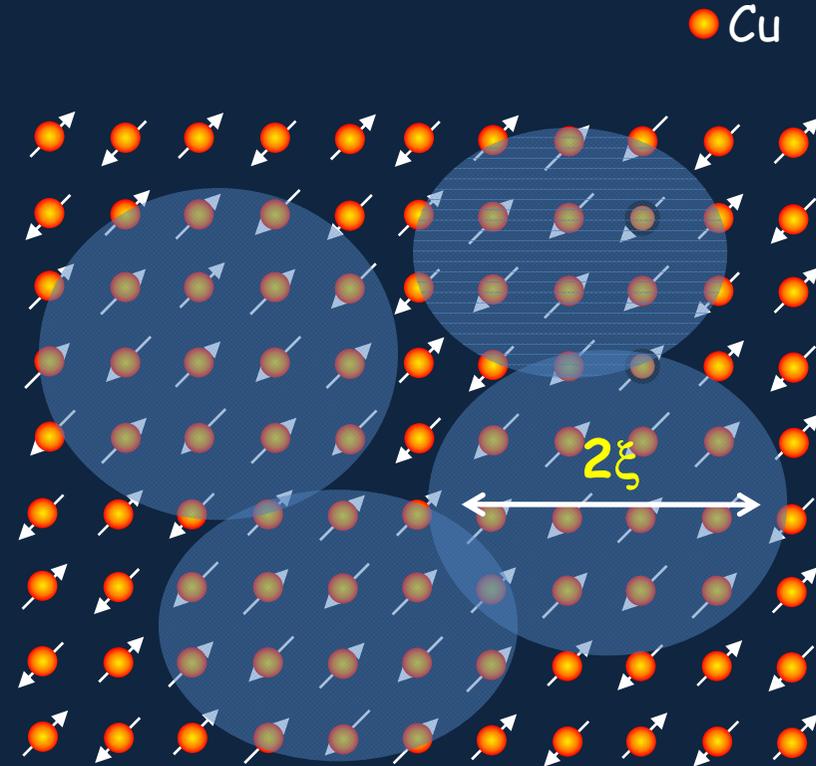
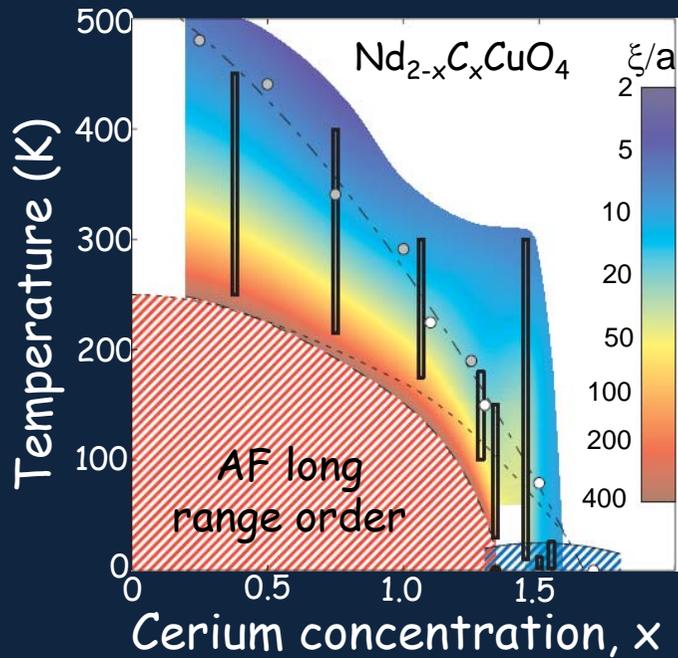
In addition:

What is the origin of scattering?

(Spin-fermion, localized moments, ...)

# Effect of short range order?

AF correlation length  
by INS



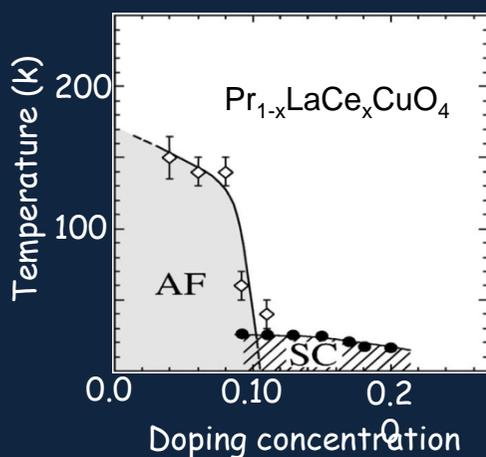
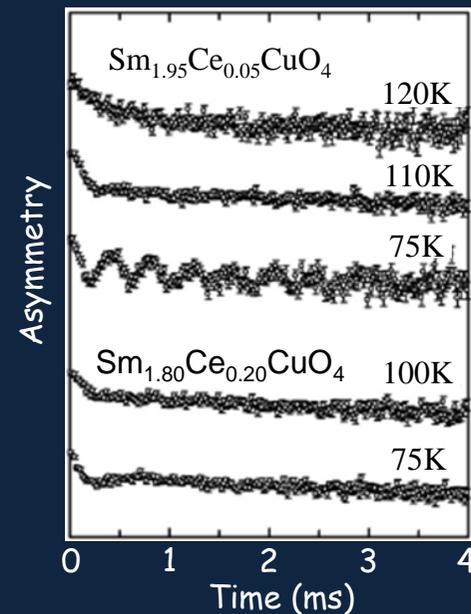
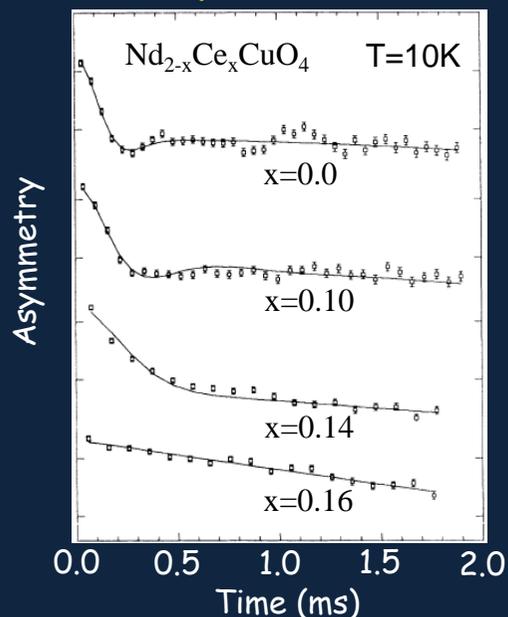
E. M. Motoyama *et al.*, nature (2007)

How to control the ordering length?

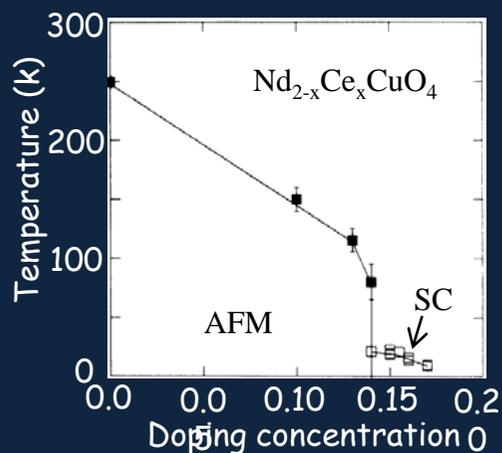
# Rare earth element dependent AF

: muon spin relaxation

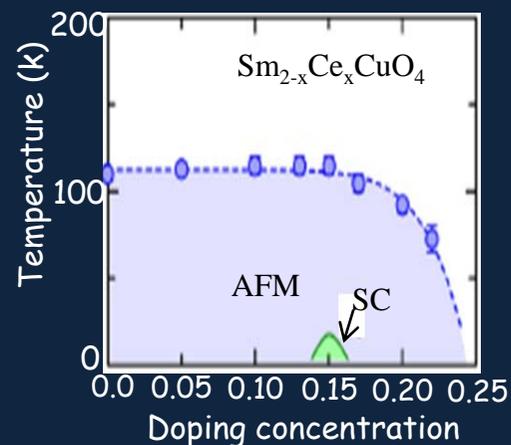
- heavier rare-earth element, stronger AF
- static AF cover all SC dome in SCCO



M. Fujita *et al.*, PRB, 2003



G. M. Luke *et al.*, PRB, 1990



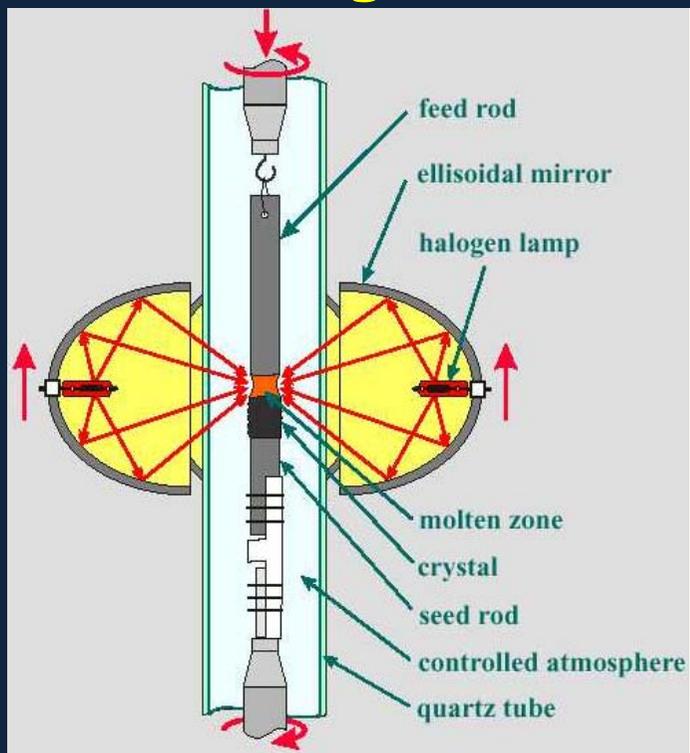
T. Sasakawa, unpublished

# Samples



57 <sup>2</sup> D <sub>3/2</sub> La Lanthanum 138.9055 [Xe]5d6s <sup>2</sup> 5.5769	58 <sup>1</sup> G <sub>4</sub> Ce Cerium 140.116 [Xe]4f5d6s <sup>2</sup> 5.5387	59 <sup>4</sup> F <sub>3/2</sub> Pr Praseodymium 140.90765 [Xe]4f6s <sup>2</sup> 5.473	60 <sup>1</sup> I <sub>3/2</sub> Nd Neodymium 144.24 [Xe]4f6s <sup>2</sup> 5.5250	61 <sup>6</sup> H <sub>5/2</sub> Pm Promethium (145) [Xe]4f6s <sup>2</sup> 5.582	62 <sup>7</sup> F <sub>5/2</sub> Sm Samarium 150.36 [Xe]4f6s <sup>2</sup> 5.6437	63 <sup>6</sup> S <sub>7/2</sub> Eu Europium 151.964 [Xe]4f6s <sup>2</sup> 5.6704	64 <sup>7</sup> D <sub>3/2</sub> Gd Gadolinium 157.25 [Xe]4f5d6s <sup>2</sup> 6.1498	65 <sup>6</sup> H <sub>15/2</sub> Tb Terbium 158.92534 [Xe]4f6s <sup>2</sup> 5.8638
89 <sup>2</sup> D <sub>3/2</sub> Ac Actinium (227) [Rn]6d7s <sup>2</sup> 5.17	90 <sup>3</sup> F <sub>2</sub> Th Thorium 232.0381 [Rn]6d7s <sup>2</sup> 6.3067	91 <sup>4</sup> K <sub>11/2</sub> Pa Protactinium 231.03588 [Rn]5f6d7s <sup>2</sup> 5.89	92 <sup>6</sup> L <sub>6</sub> U Uranium 238.02891 [Rn]5f6d7s <sup>2</sup> 6.1941	93 <sup>6</sup> L <sub>11/2</sub> Np Neptunium (237) [Rn]5f6d7s <sup>2</sup> 6.2657	94 <sup>1</sup> F <sub>0</sub> Pu Plutonium (244) [Rn]5f7s <sup>2</sup> 6.0260	95 <sup>8</sup> S <sub>7/2</sub> Am Americium (243) [Rn]5f7s <sup>2</sup> 5.9738	96 <sup>6</sup> D <sub>2</sub> Cm Curium (247) [Rn]5f6d7s <sup>2</sup> 5.9914	97 <sup>6</sup> H <sub>15/2</sub> Bk Berkelium (247) [Rn]5f7s <sup>2</sup> 6.1979

## Floating zone



# Experiments

- ARPES experiments: Stanford Synchrotron Radiation Lab.
- Energy resolution : 15 meV
- Temperature : 15K

## ➤ ARPES



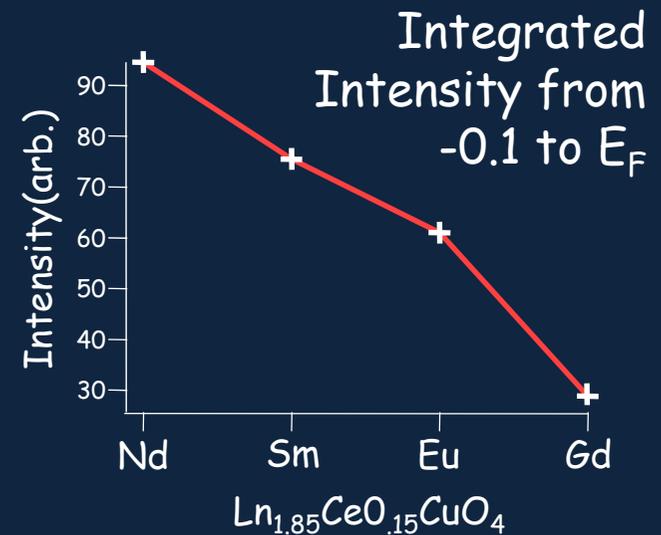
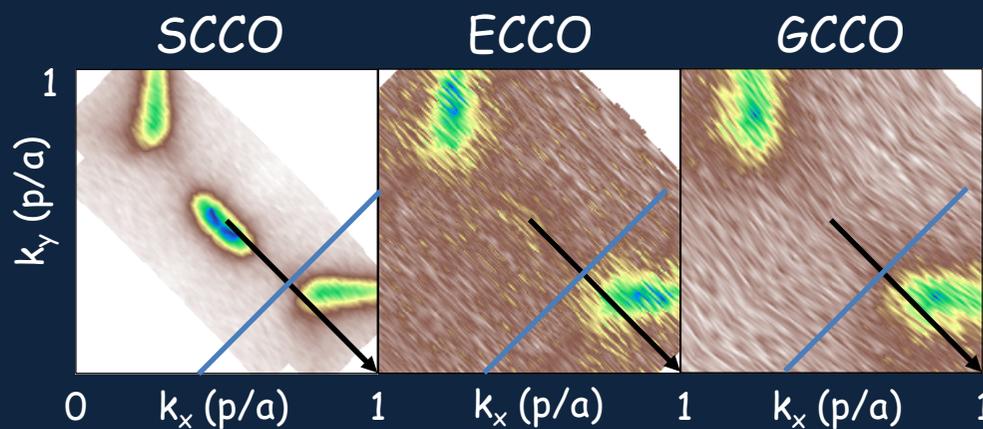
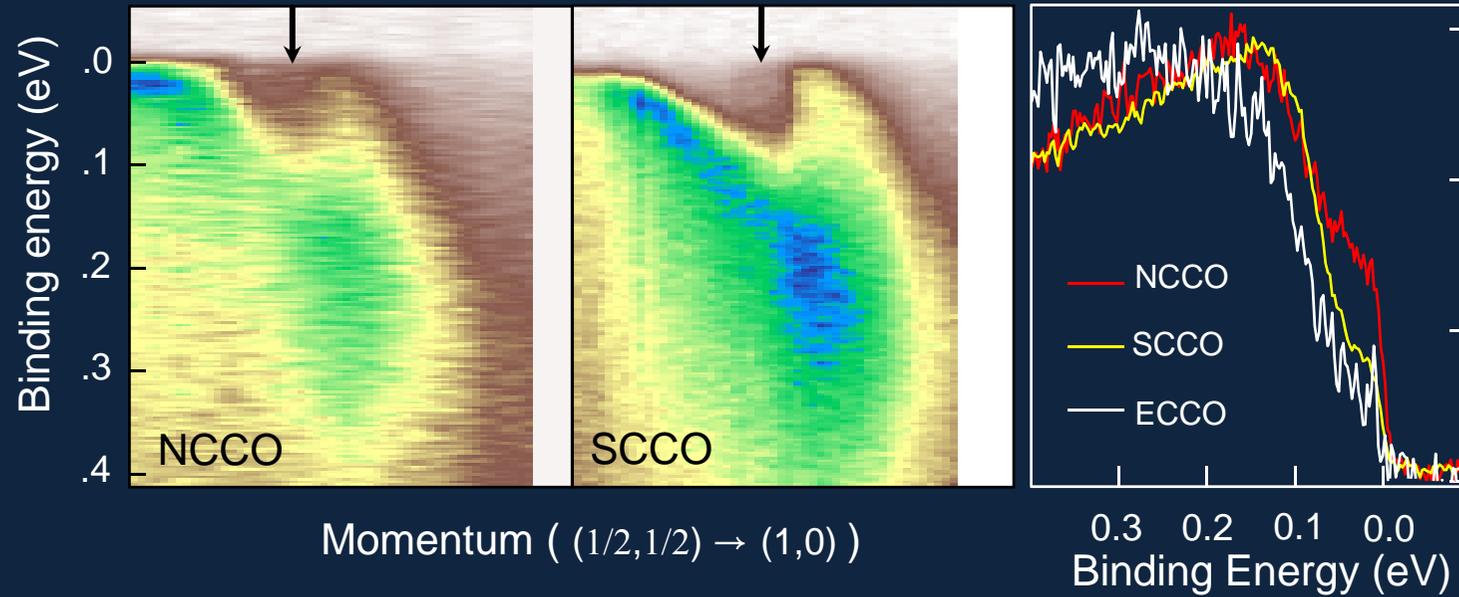
SSRL, Stanford, USA

B.L. 5-4  
high resolution ARPES

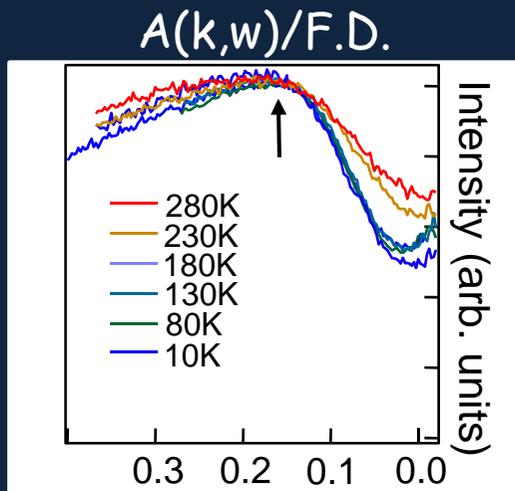
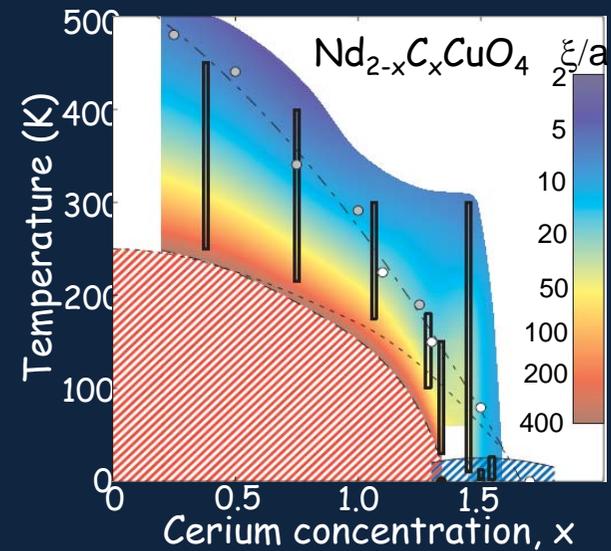
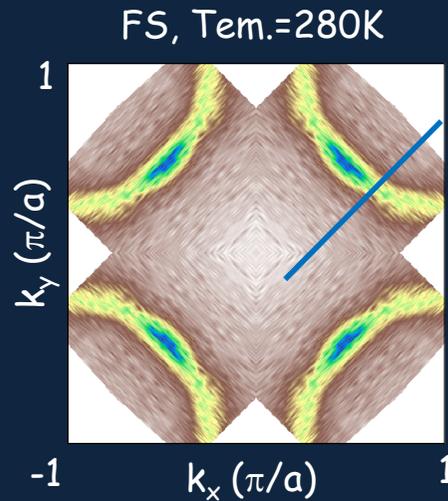
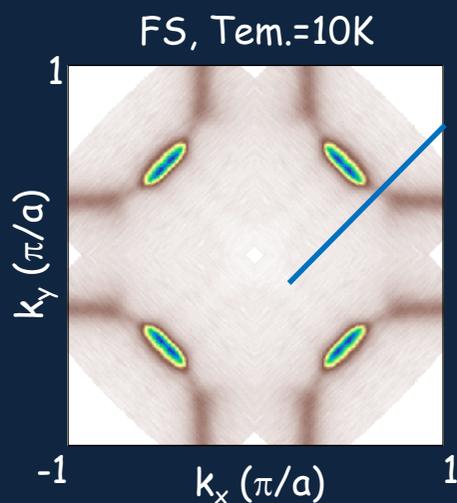
## ➤ Optical



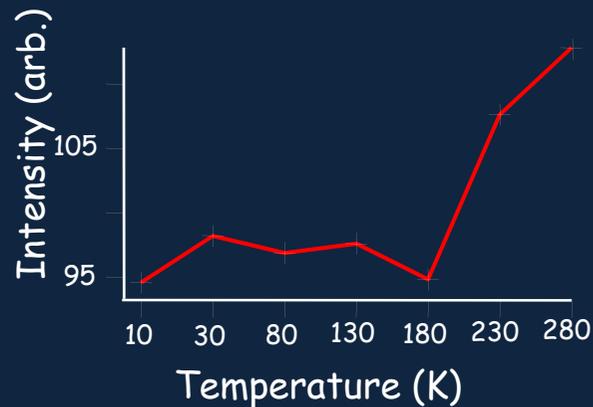
# Rare-earth elements dependent



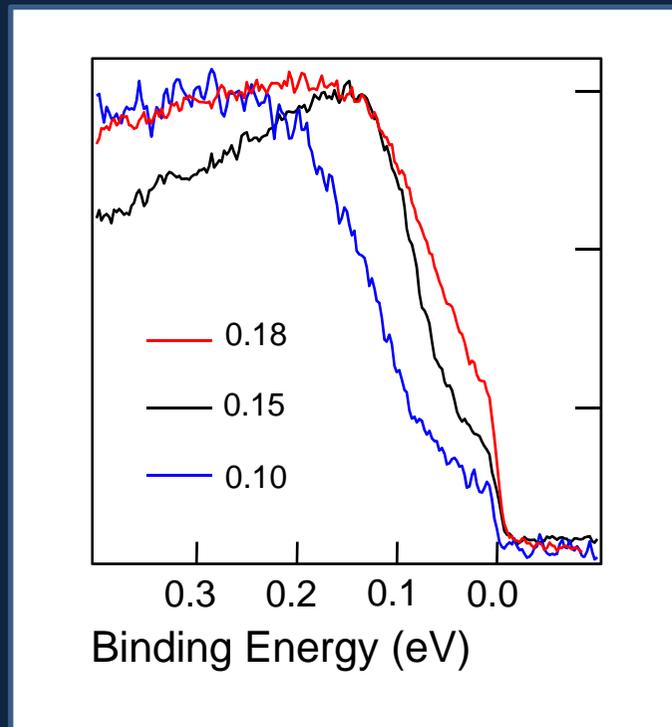
# Tem. Dep. Spectral weight



Integrated intensity from  $-0.1$  to  $E_F$   
 $\sim 1/\text{correlation length}(\xi)$



# Doping dep. spectral weight



Previously also seen in NCCO  
H. Matsui et al., PRB (2007)

Doping, temperature, rare earth dependences all show that:

1. Overall, gap size does not change much
2. Gap is filled up as AF ordering length decreases

⇒ Similar to pseudo-gap in hole doped & reminiscence of phase fluctuation.

# Spin-fermion model

# Coupling to spin excitations

nature  
physics

LETTERS

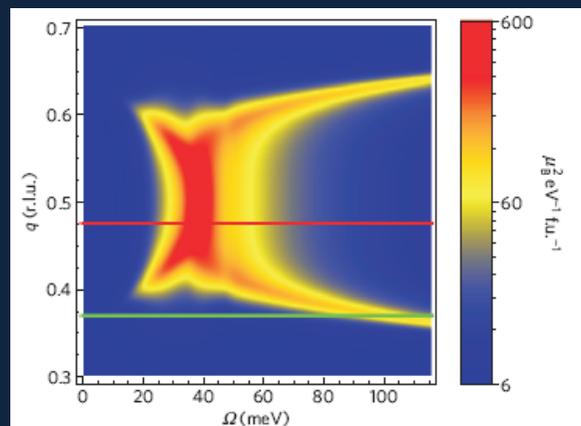
PUBLISHED ONLINE: 18 JANUARY 2009 | DOI: 10.1038/NPHYS1180

## Strength of the spin-fluctuation-mediated pairing interaction in a high-temperature superconductor

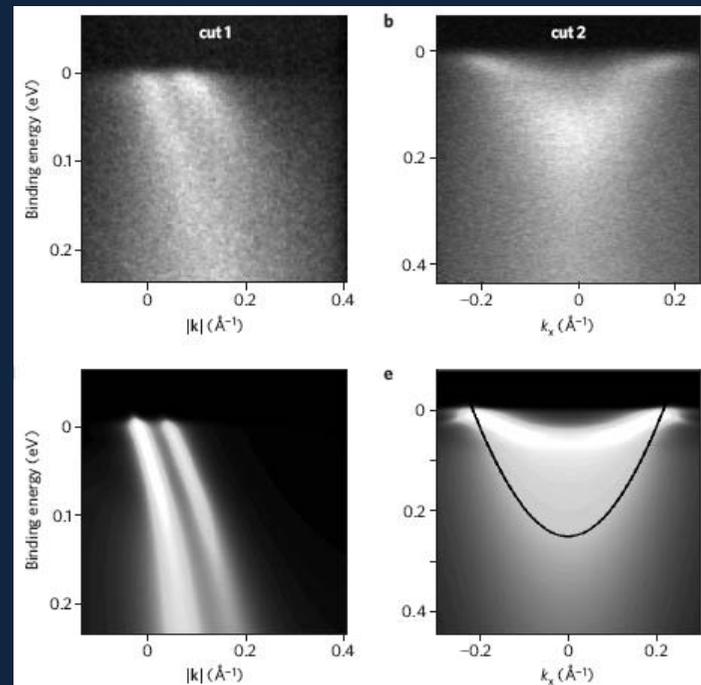
T. Dahm<sup>1</sup>, V. Hinkov<sup>2</sup>, S. V. Borisenko<sup>3</sup>, A. A. Kordyuk<sup>3</sup>, V. B. Zabolotnyy<sup>3</sup>, J. Fink<sup>3,4</sup>, B. Büchner<sup>3</sup>, D. J. Scalapino<sup>5</sup>, W. Hanke<sup>6</sup> and B. Keimer<sup>2\*</sup>

$$V_{\text{eff}}(\mathbf{Q}, \Omega) = \frac{3}{2} \bar{U}^2 \chi(\mathbf{Q}, \Omega)$$

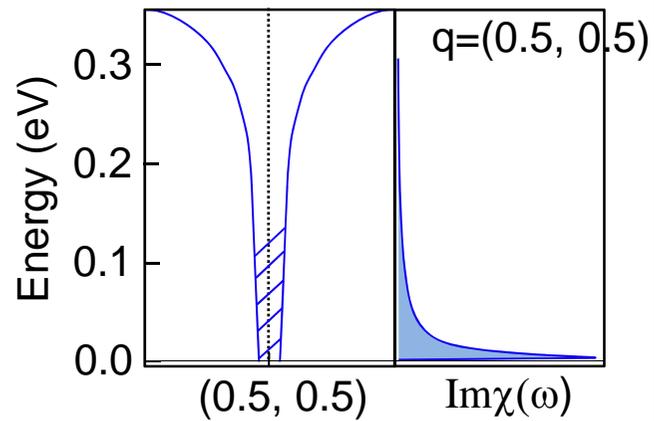
$$U = 1.59 \text{ eV}$$



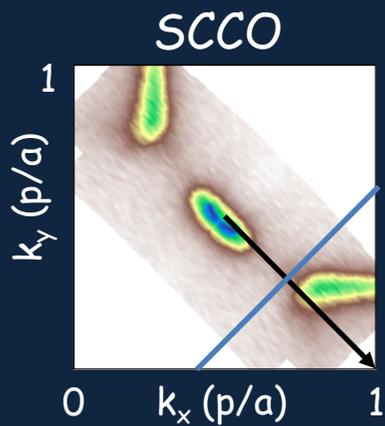
←  $\chi''$



# Electron doped case



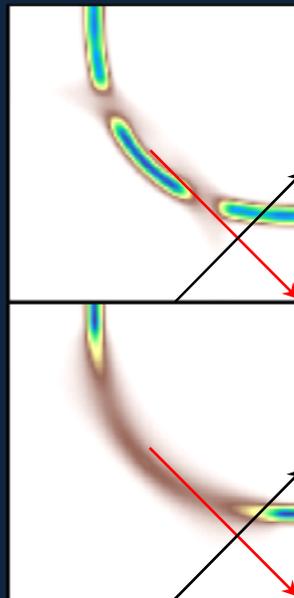
Wilson et al., PRL 96, 157001 (2006)



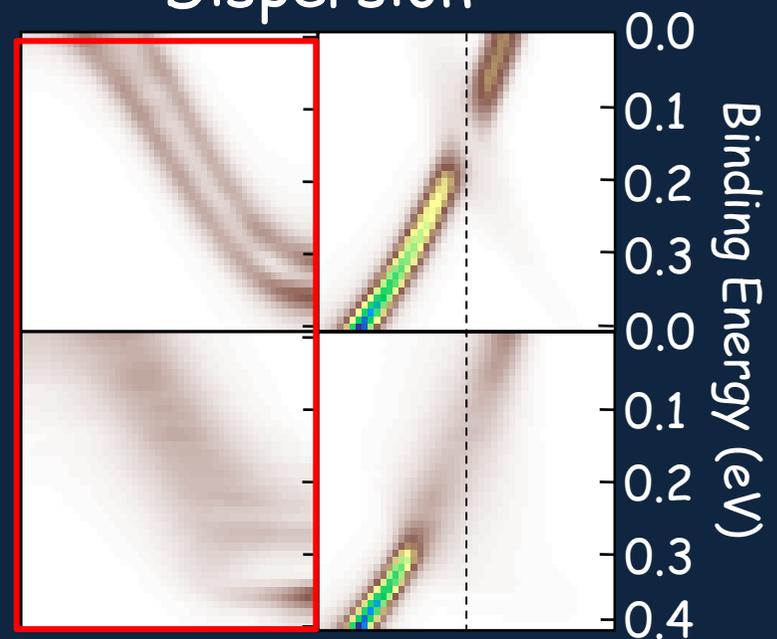
$\xi=16a$

$\xi=4a$

FS



Dispersion



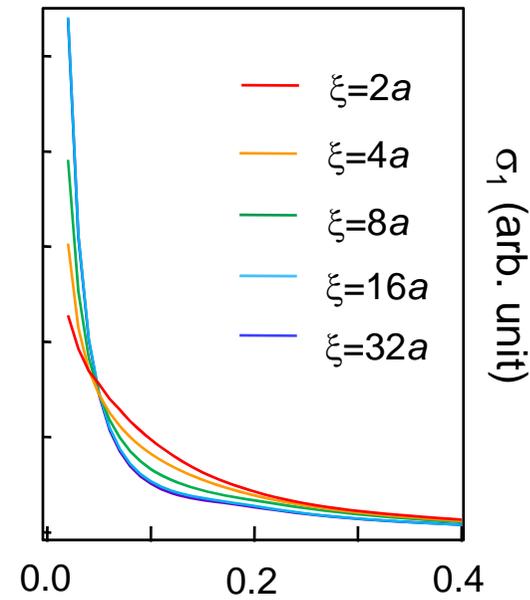
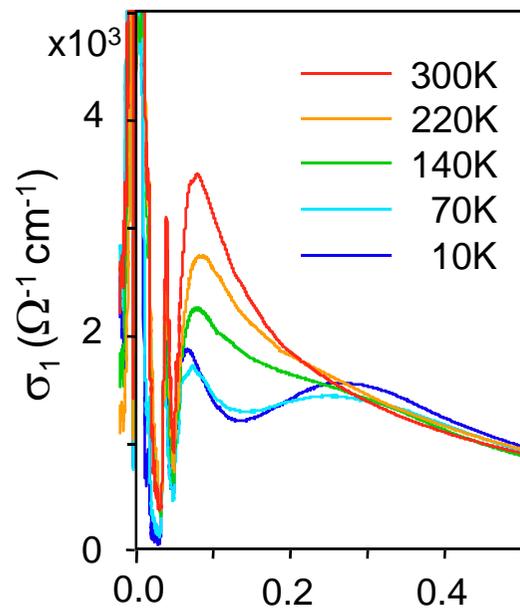
Binding Energy (eV)

Momentum

# Optical conductivity

Experiment

Simulation



Photon Energy (eV)

$\sigma_1$  (arb. unit)

# AF phase fluctuation model

("Yet another spin-fermion model",  
A. Chubukov)

# Subject to potential from AF order

$$H = \sum_{ij} t_{ji} c_{j\sigma}^{\dagger} c_{i\sigma} + \lambda \sum_i \mathbf{m}_i \cdot \mathbf{S}_i$$

$\mathbf{m}_i$  = local magnetic moment

$\mathbf{S}_i$  = electron spin

$\lambda$  = coupling constant

$$S_i^+ = c_{i\uparrow}^{\dagger} c_{i\downarrow}, \quad S_i^- = c_{i\downarrow}^{\dagger} c_{i\uparrow}, \quad S_i^z = \frac{1}{2} (c_{i\uparrow}^{\dagger} c_{i\uparrow} - c_{i\downarrow}^{\dagger} c_{i\downarrow})$$

$$H = \sum_{ij} t_{ji} c_{j\sigma}^{\dagger} c_{i\sigma} + \lambda \sum_i (m_i^+ c_{i\downarrow}^{\dagger} c_{i\uparrow} + m_i^- c_{i\uparrow}^{\dagger} c_{i\downarrow}), \quad m_i^{\pm} = m_i^x \pm i m_i^y$$

$$m_i^{\pm} = (-1)^i m e^{i\phi_i}$$

$\Leftarrow$  AF phase fluctuation

$$G_k = G_{k\uparrow} + G_{k\downarrow} = \frac{\cos^2 \theta_{k-p\uparrow}}{E_{k-p\uparrow}^+ - i\omega} + \frac{\sin^2 \theta_{k-p\uparrow}}{E_{k-p\uparrow}^- - i\omega} + \frac{\cos^2 \theta_{k+p\downarrow}}{E_{k+p\downarrow}^+ - i\omega} + \frac{\sin^2 \theta_{k+p\downarrow}}{E_{k+p\downarrow}^- - i\omega},$$

$$A_k = \cos^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^+ - \omega) + \sin^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^- - \omega) + \cos^2 \theta_{k+p\downarrow} \delta(E_{k+p\downarrow}^+ - \omega) + \sin^2 \theta_{k+p\downarrow} \delta(E_{k+p\downarrow}^- - \omega)$$

$$G_k = G_{k\uparrow} + G_{k\downarrow} = \frac{\cos^2 \theta_{k-p\uparrow}}{E_{k-p\uparrow}^+ - i\omega} + \frac{\sin^2 \theta_{k-p\uparrow}}{E_{k-p\uparrow}^- - i\omega} + \frac{\cos^2 \theta_{k+p\downarrow}}{E_{k+p\downarrow}^+ - i\omega} + \frac{\sin^2 \theta_{k+p\downarrow}}{E_{k+p\downarrow}^- - i\omega},$$

$$A_k = \cos^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^+ - \omega) + \sin^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^- - \omega) + \cos^2 \theta_{k+p\downarrow} \delta(E_{k+p\downarrow}^+ - \omega) + \sin^2 \theta_{k+p\downarrow} \delta(E_{k+p\downarrow}^- - \omega)$$

with

$$\cos 2\theta_{k-p\uparrow} = \frac{\varepsilon_k - \varepsilon_{k+Q-2p}}{\sqrt{(\varepsilon_k - \varepsilon_{k+Q-2p})^2 + 4\lambda^2 m^2}}, \quad \cos 2\theta_{k+p\downarrow} = \frac{\varepsilon_k - \varepsilon_{k+Q+2p}}{\sqrt{(\varepsilon_k - \varepsilon_{k+Q+2p})^2 + 4\lambda^2 m^2}}$$

and

$$E_{k-p\uparrow}^{\pm} = \frac{1}{2}(\varepsilon_k + \varepsilon_{k+Q-2p}) \pm \sqrt{(\lambda m)^2 + \frac{1}{4}(\varepsilon_k - \varepsilon_{k+Q-2p})^2}$$

$$E_{k+p\downarrow}^{\pm} = \frac{1}{2}(\varepsilon_k + \varepsilon_{k+Q+2p}) \pm \sqrt{(\lambda m)^2 + \frac{1}{4}(\varepsilon_k - \varepsilon_{k+Q+2p})^2}.$$

Finally:

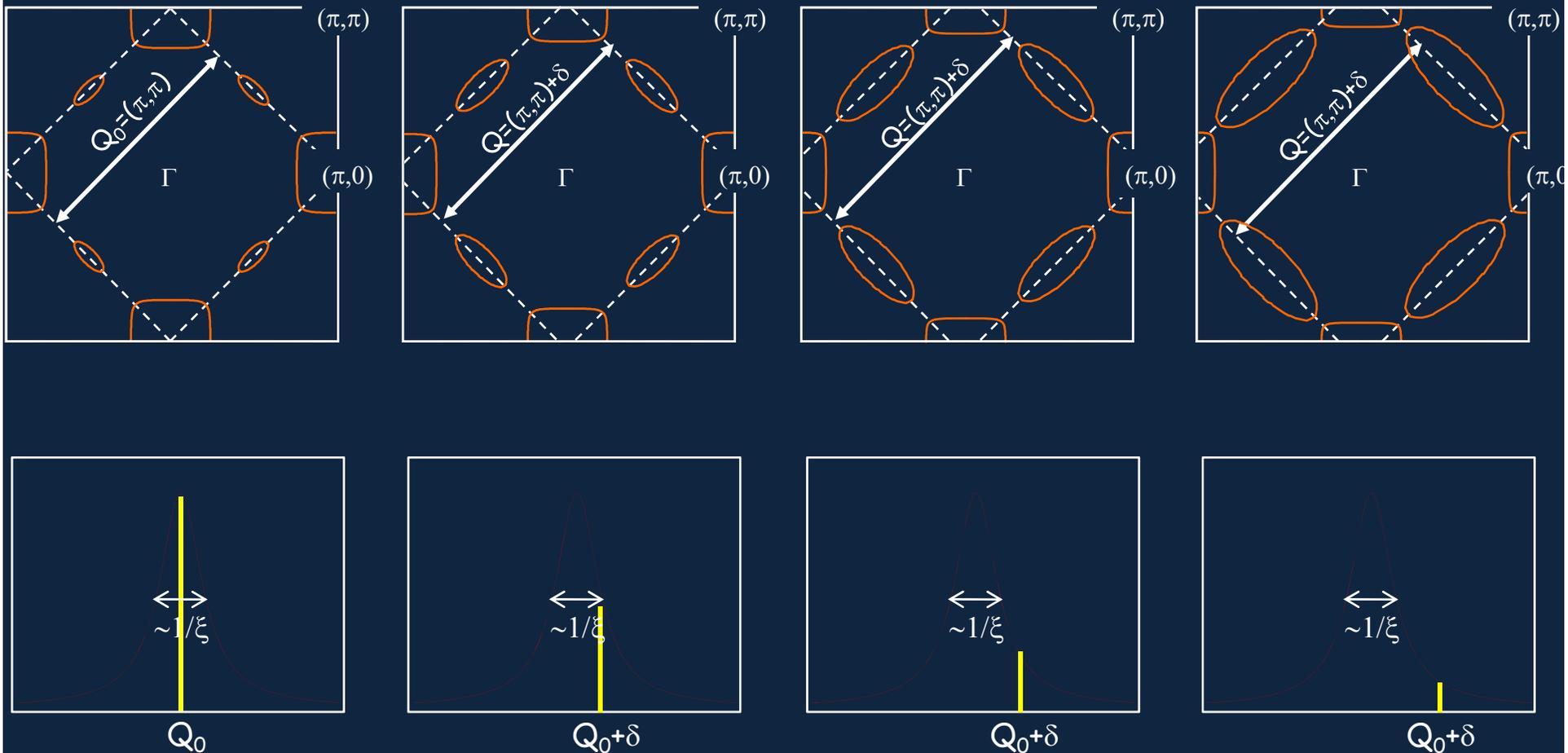
$$\langle A_k \rangle = \int \left( \cos^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^+ - \omega) + \sin^2 \theta_{k-p\uparrow} \delta(E_{k-p\uparrow}^- - \omega) \right) \rho(p) d^2 p.$$

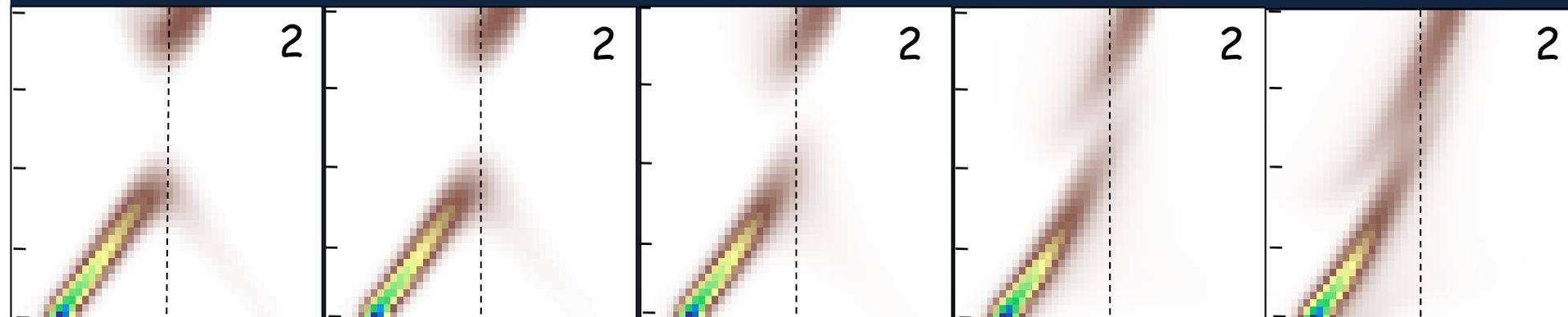
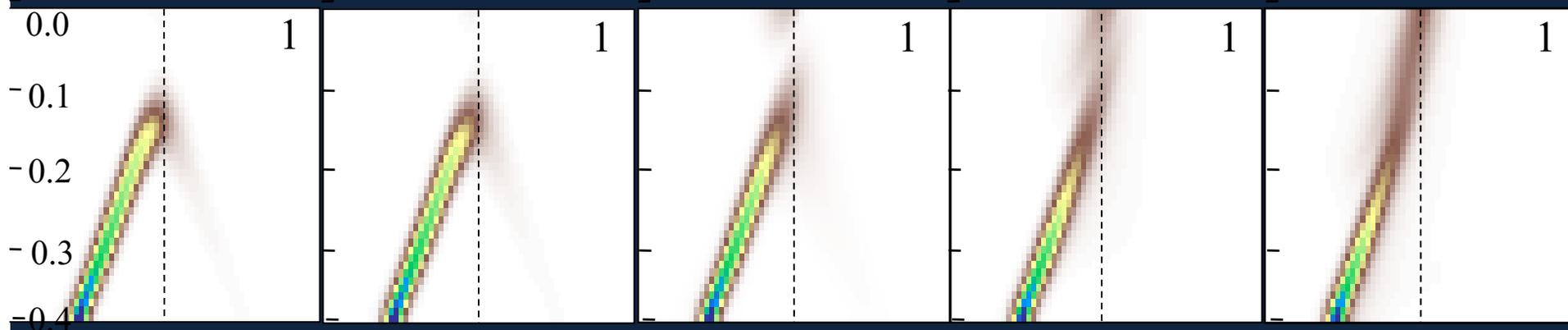
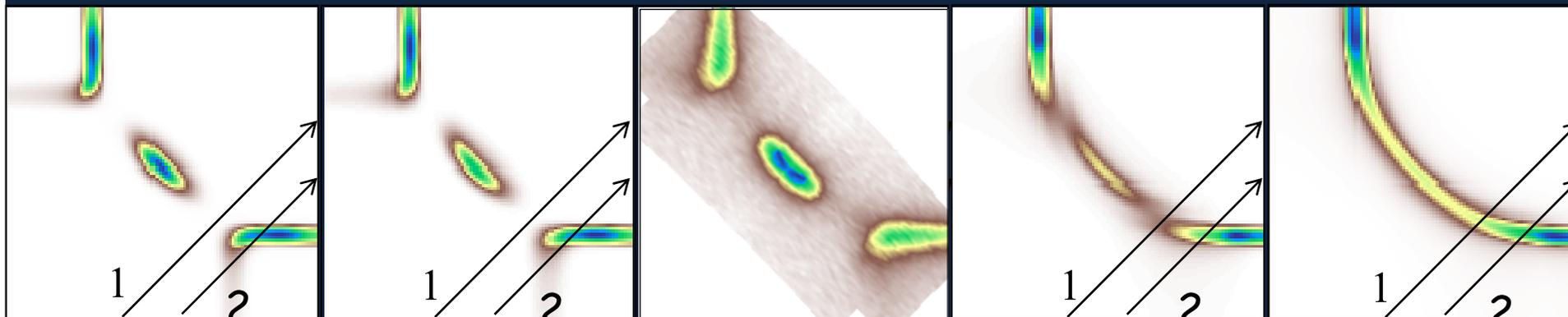
\*  $\xi$  = ordering length

with

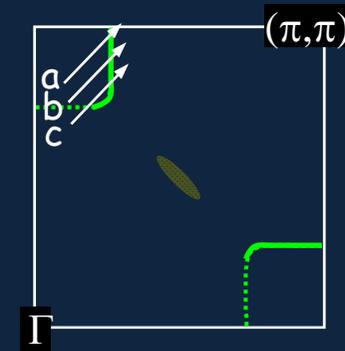
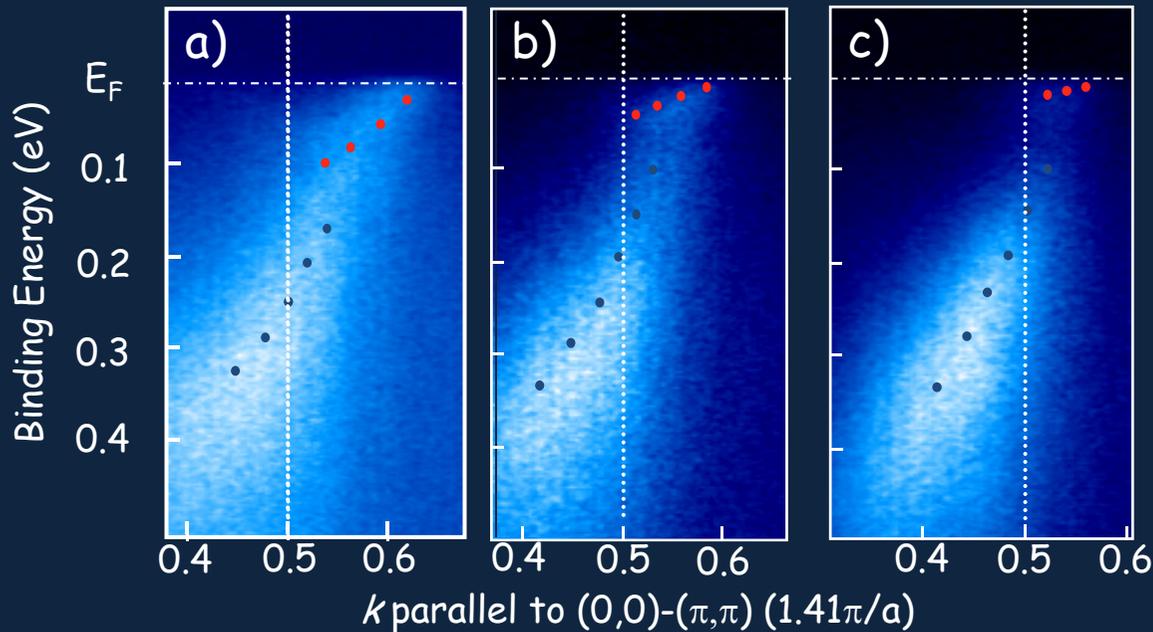
$$\langle A_k \rangle = \int \frac{A_k(\omega)}{p^2 \xi^2 + 1} d^2 p$$

# AF phase fluctuation effect (averaging over different Q's)

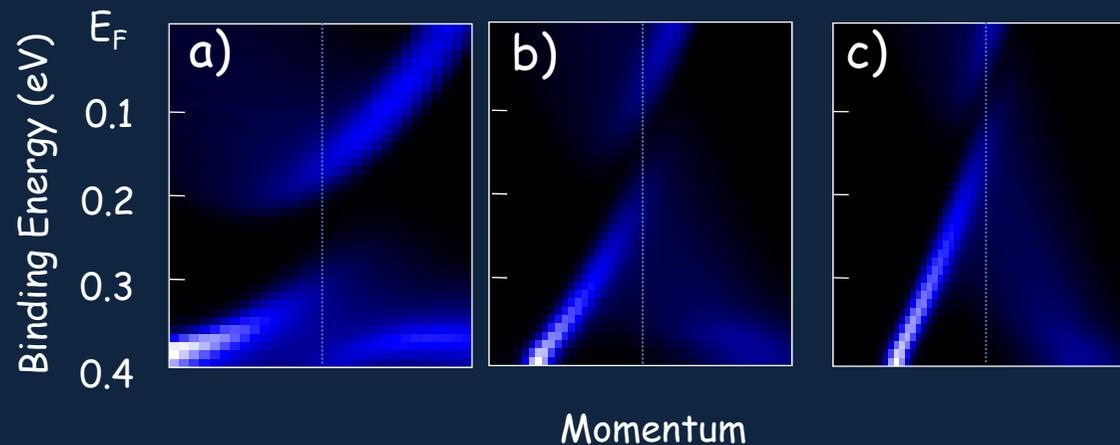


$\xi \sim 32a$  $\xi \sim 16a$  $\xi \sim 8a$  $\xi \sim 4a$  $\xi \sim 2a$ 

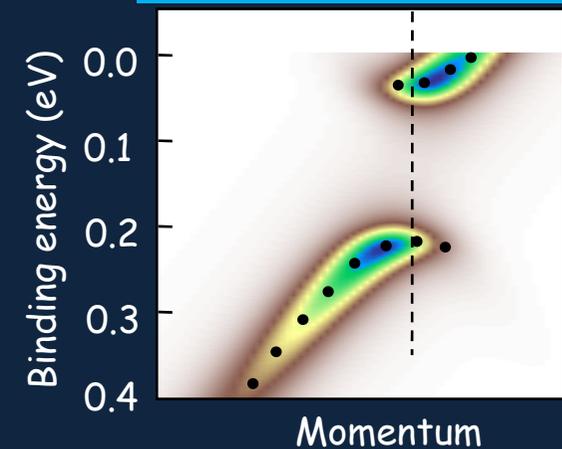
# Electron-AF SRO coupling



Short Range Order(SRO) ,  $\xi \sim 4a$

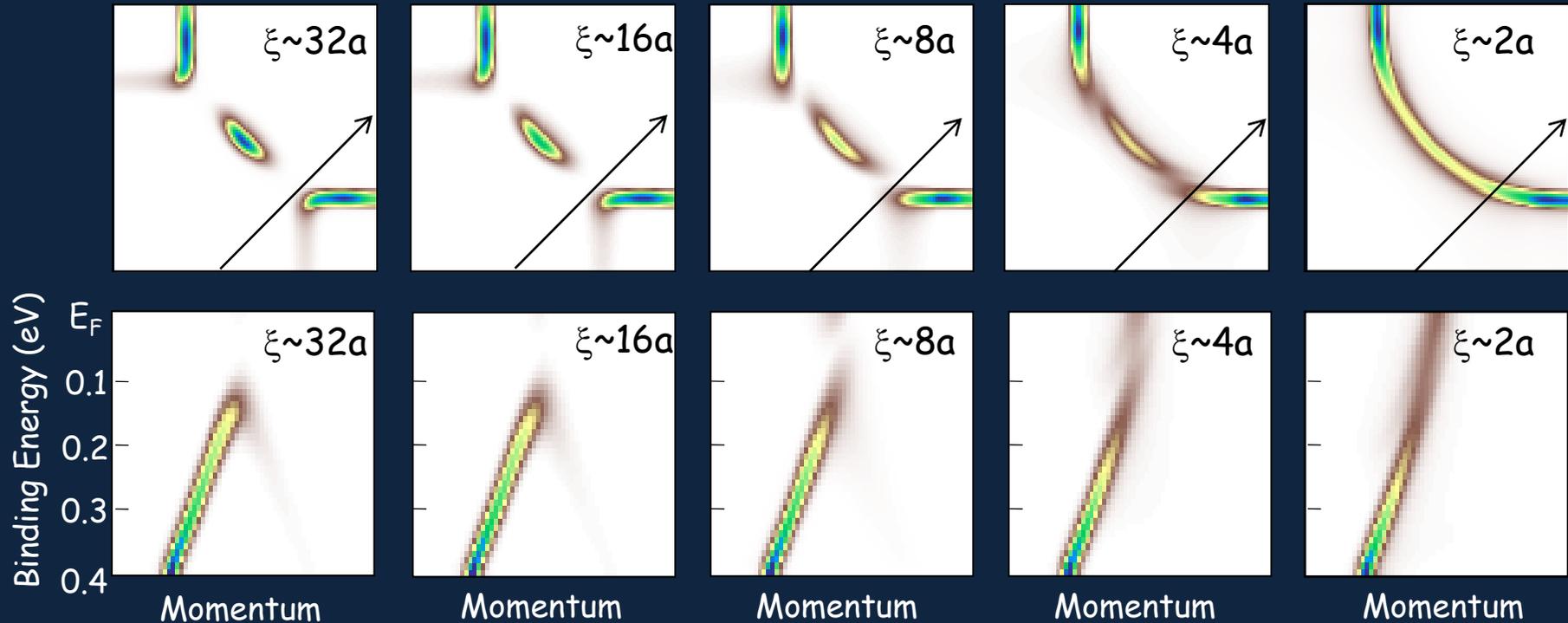


Long Range order

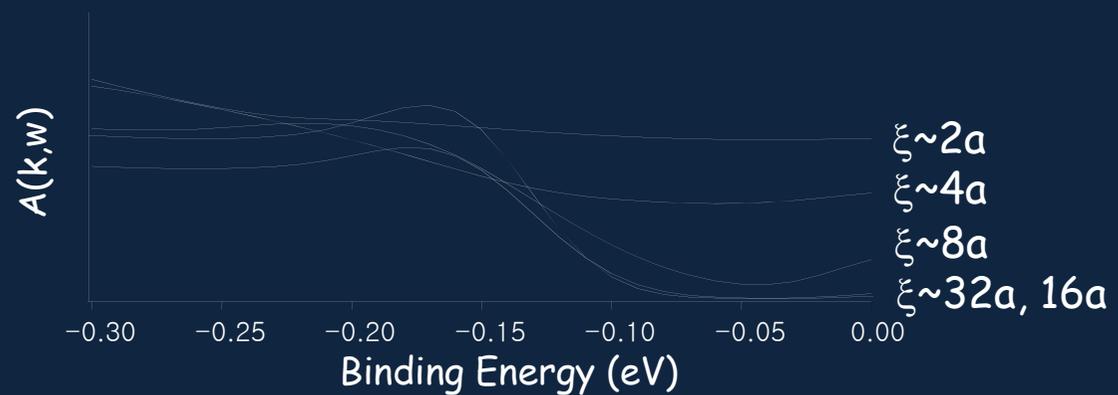


# Gap filling and $E_F$ weight

➤ Fermi surface

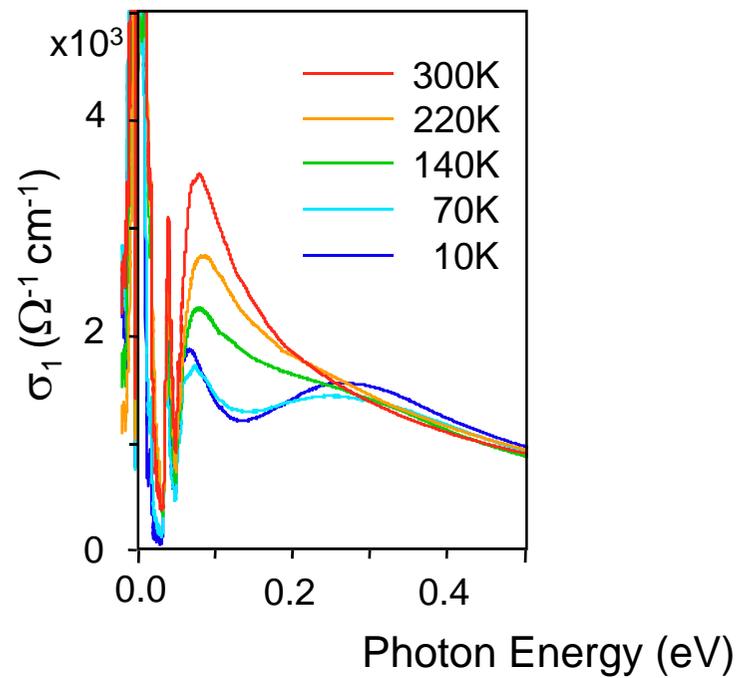


Spectral weight near  $E_F$

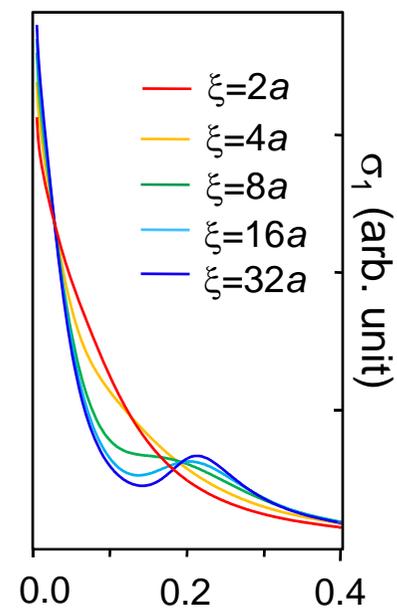


# Optical conductivity

Experiment



Simulation



# The model....

1. Not spin-boson but phase gradient ( $\nabla\phi$ ) couples to electron.
2.  $T_c$  can be estimated based within the model.
3. The parameter  $\lambda m$  can be obtained by fitting exp data.

$$H = \sum_{ij} t_{ji} c_{j\sigma}^{\dagger} c_{i\sigma} + \lambda \sum_i \mathbf{m}_i \cdot \mathbf{S}_i$$

# Summary

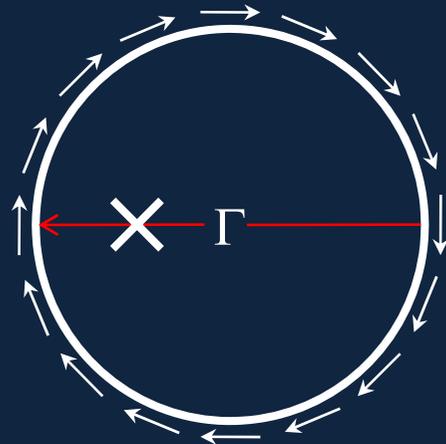
1. Correlation between pseudo-gap behavior and AF ordering
2. Pseudo-gap does not close but fills up as AF ordering decreases
3. ARPES spectral function and optical conductivity are well explained within AF phase fluctuation model

# Quasi-particle dynamics in topological insulator $\text{Bi}_2\text{Se}_3$

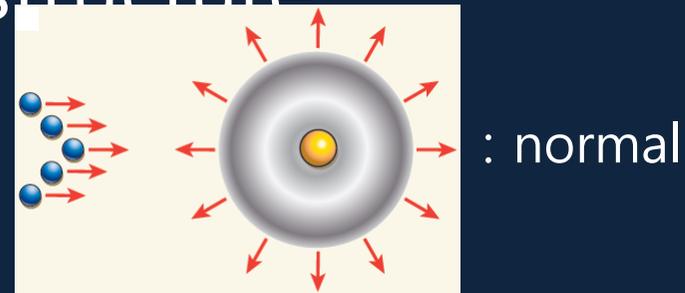
S. R. Park, W. S. Jung, Chul Kim, D. J. Song, C. Kim,  
S. Kimura, K. D. Lee and N. Hur

# Importance

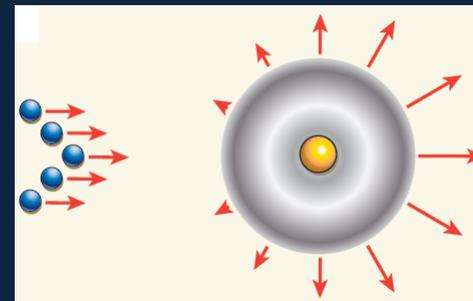
1. Long lifetime of surface metallic states due to helical spin structure



FS of surface state  
and spin structure



: normal



: TI

2. Protected surface metallic states

- No Fermi surface instability

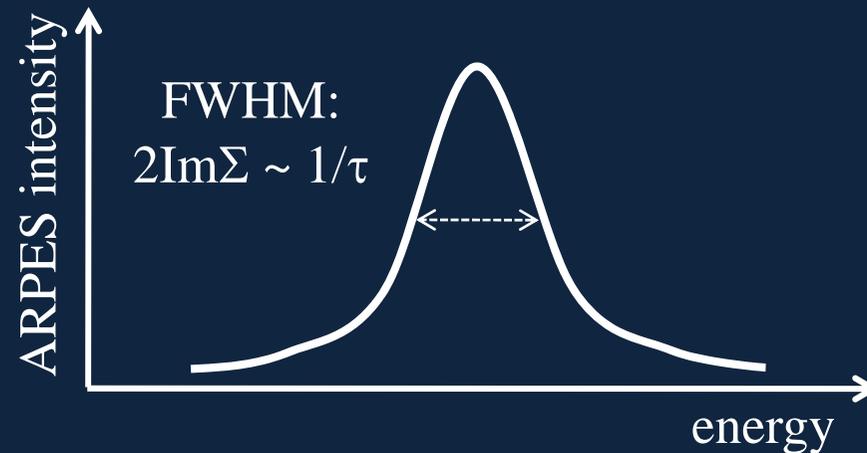
➔ Dissipationless nano-device and spintronics

Long lifetime?  
- ARPES studies

# ARPES for lifetime measurement

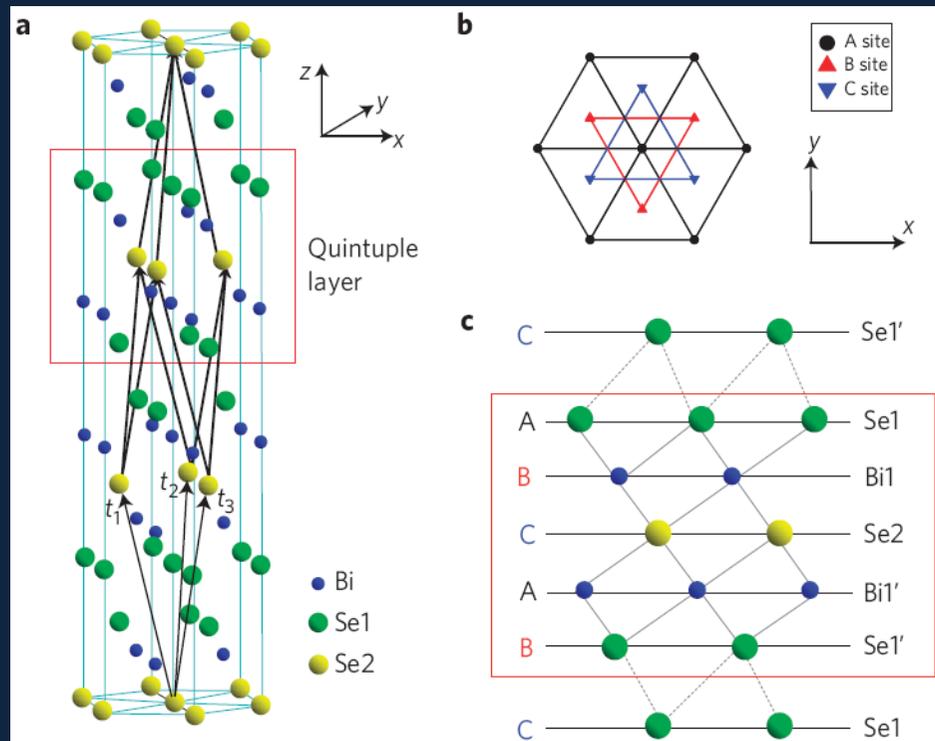
## Spectral function

$$A(k, \omega) = \frac{1}{\pi} \frac{\text{Im}\Sigma(k, \omega)}{(\omega - \varepsilon_k - \text{Re}\Sigma(k, \omega))^2 + \text{Im}\Sigma(k, \omega)^2}$$



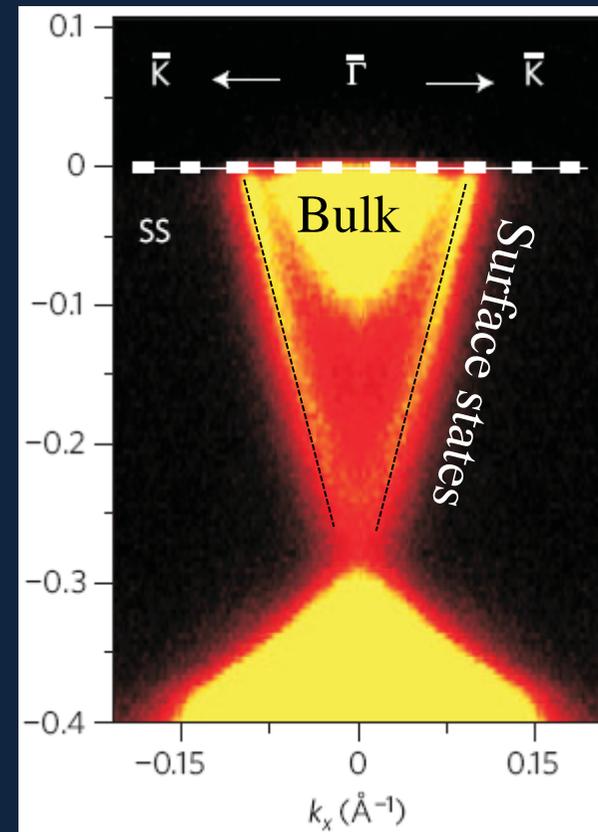
# ARPES on TI "Bi<sub>2</sub>Se<sub>3</sub>"

## Crystal structure



H. Zhang *et al.*, Nat. Phys. (2009)

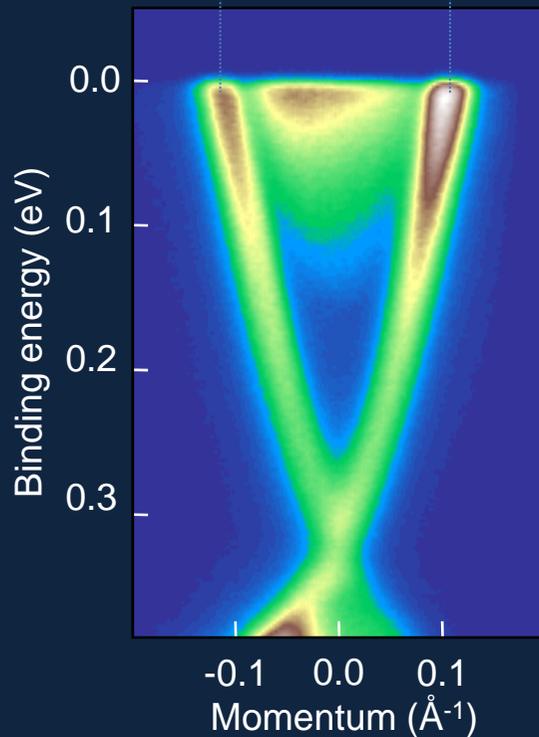
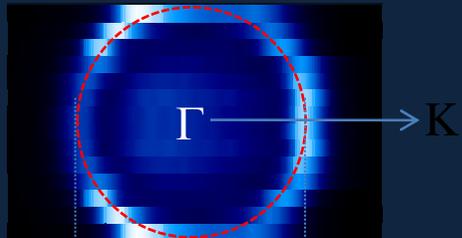
## Surface states



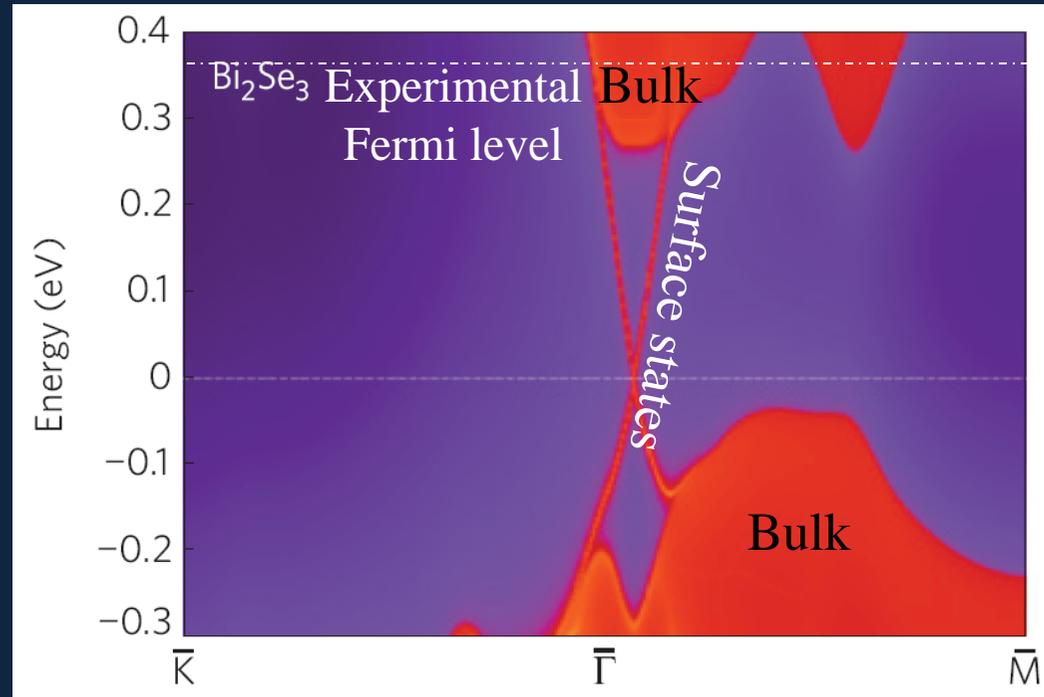
Y. Xia *et al.*, Nat. Phys. (2009)

# Our ARPES data (15 K, 8eV P. E.)

Fermi surface



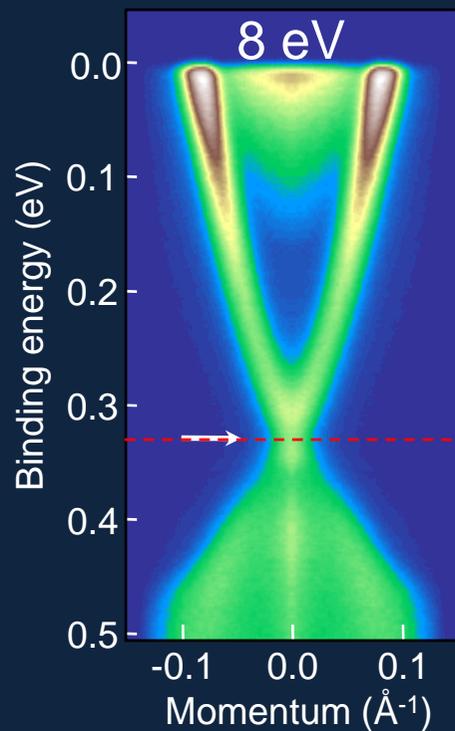
- Transport measurements as a bulk sensitive tool also report metallic behavior



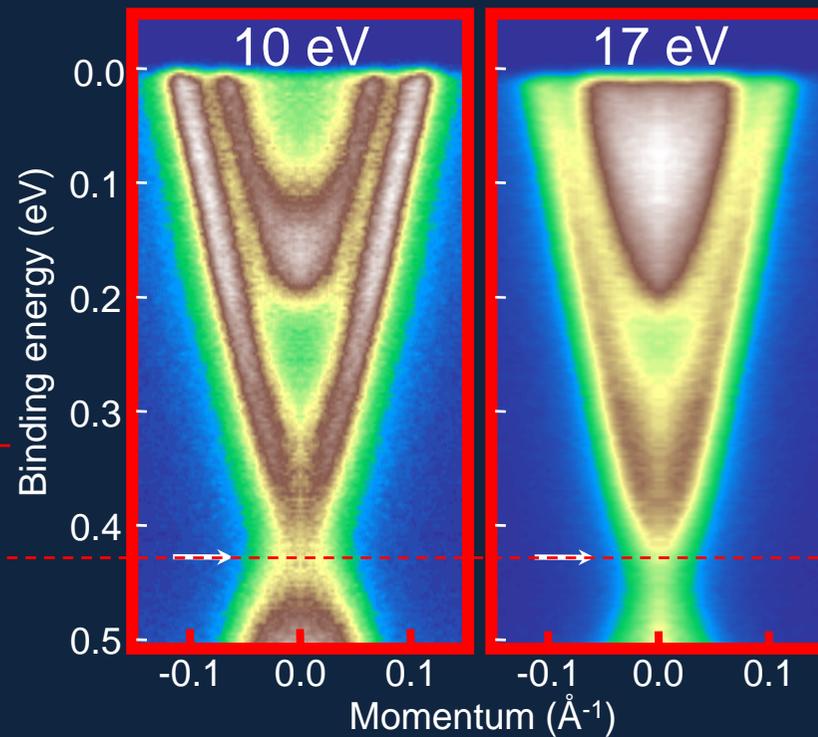
H. Zhang *et al.*, Nat. Phys. (2009)

# Time dependence

Fresh surface

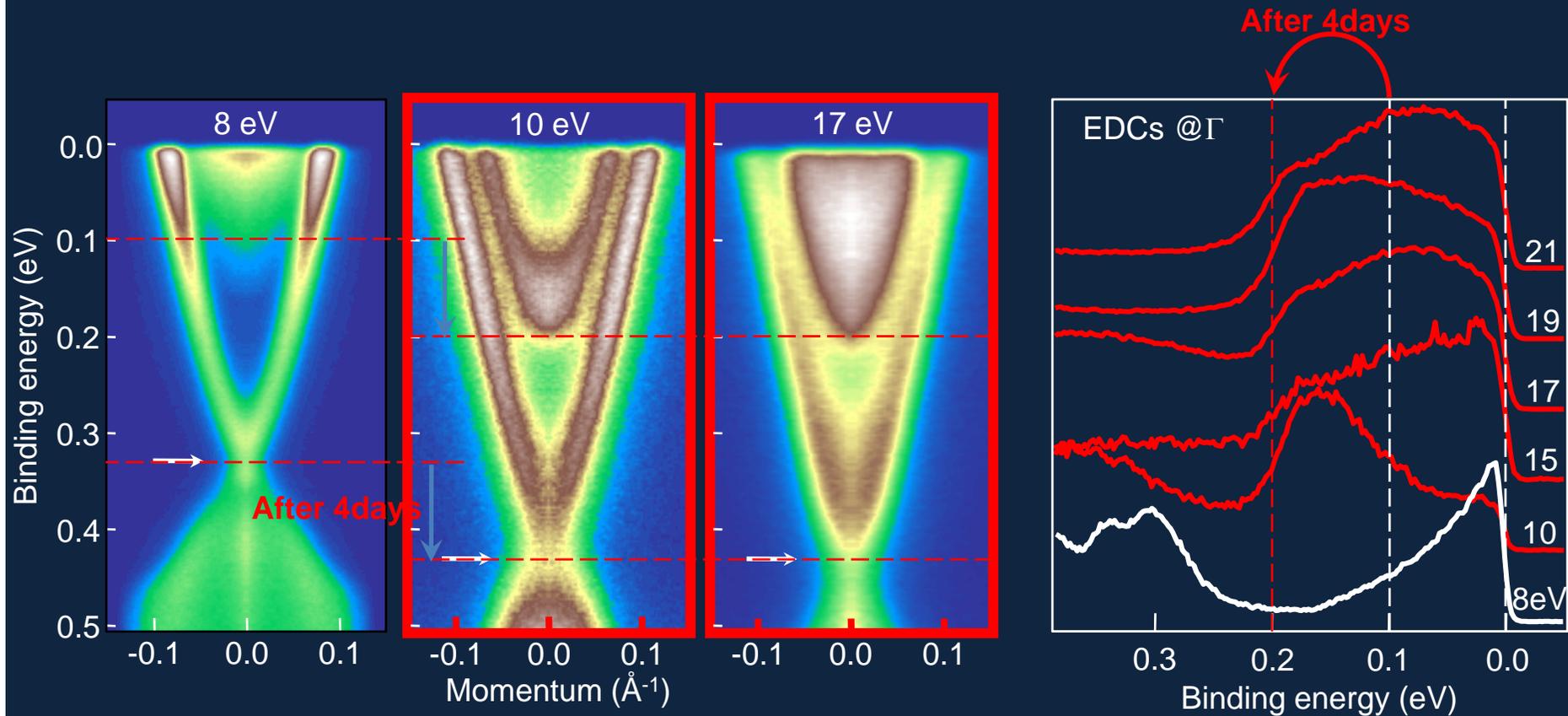


4 days later



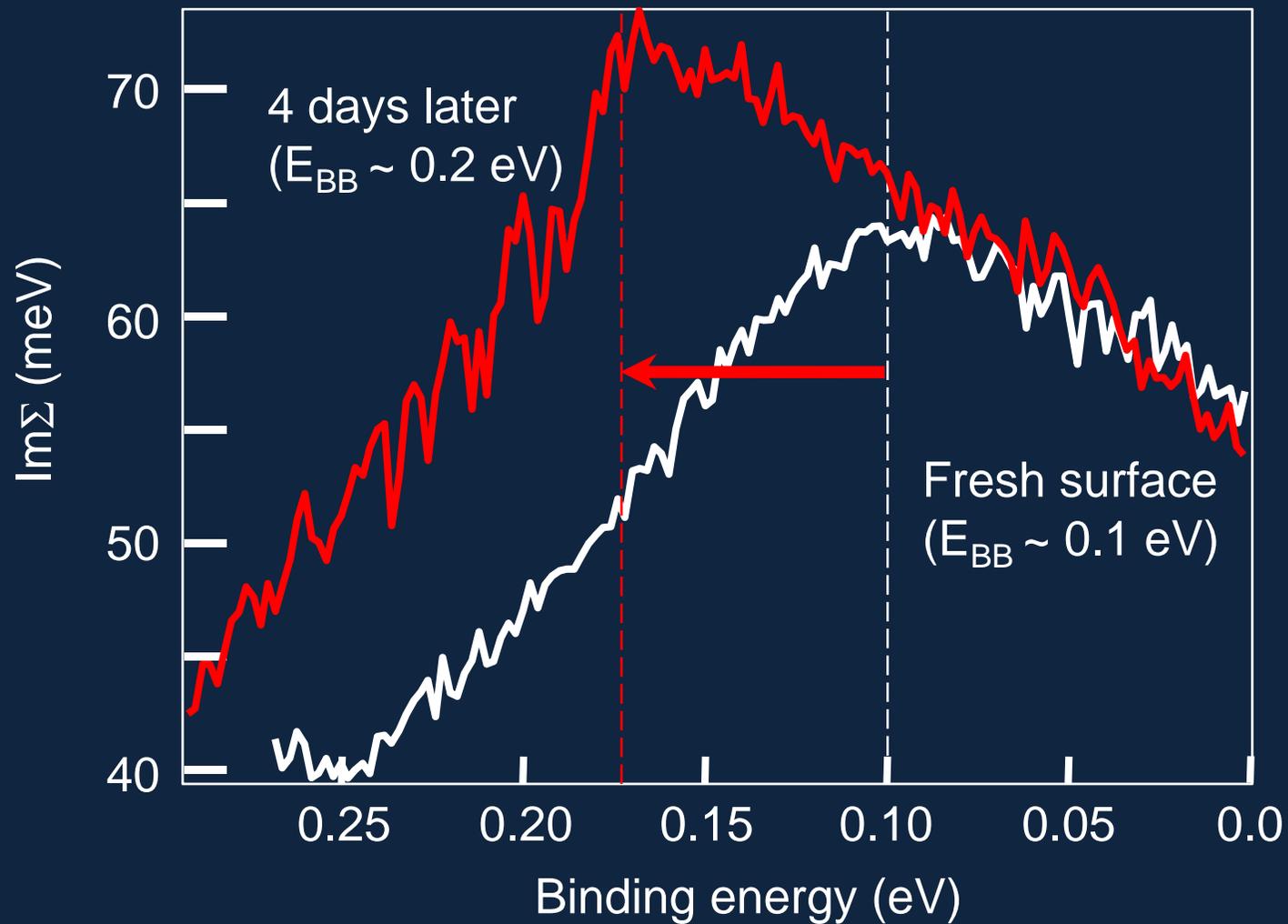
Surface (electron) doping effect with time

# Photon energy dependence

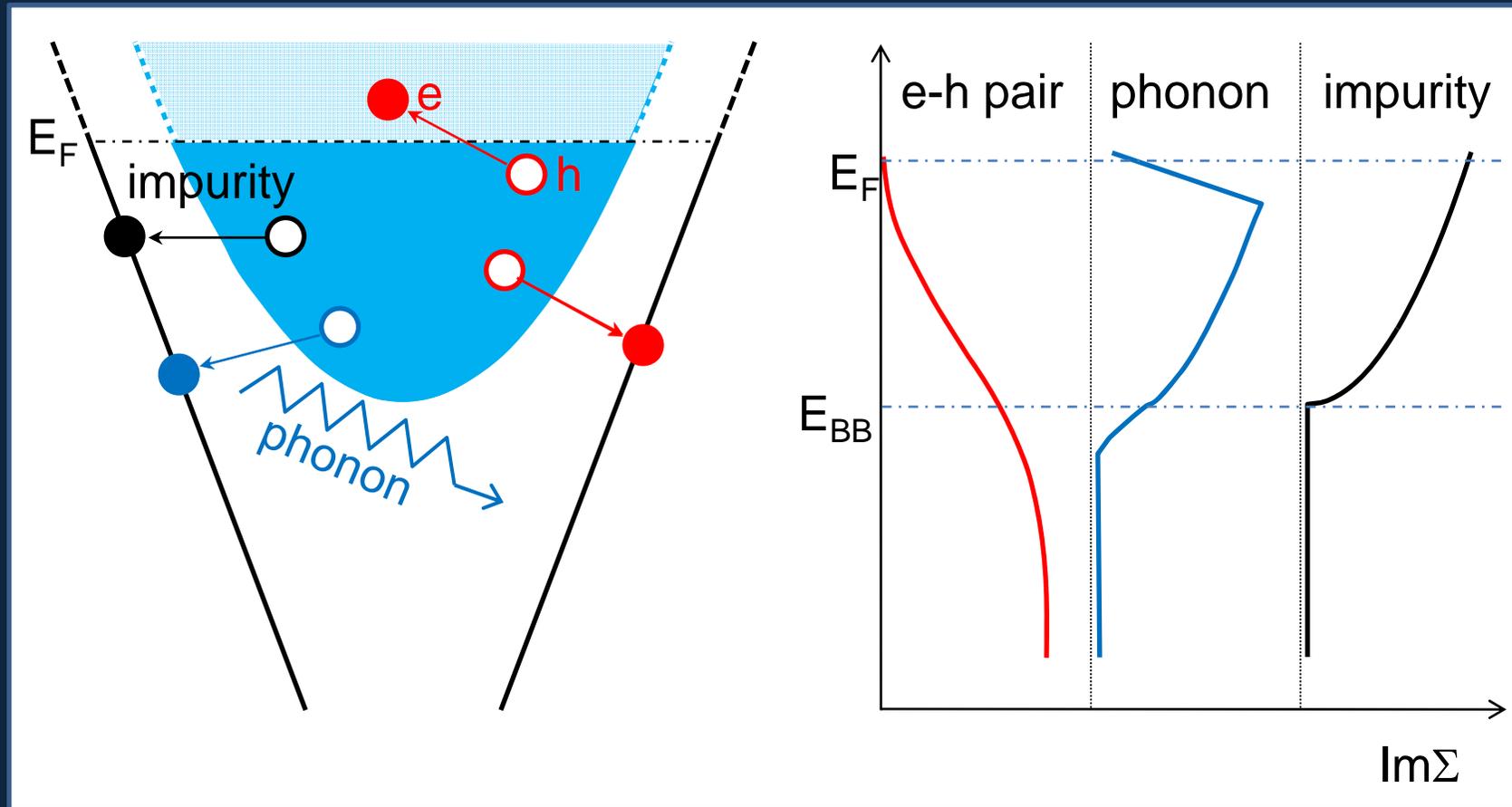


- Bulk states taken with 8 eV are suppressed due to  $k_z$ -selection rule.
- B. E. of bulk conduction band ( $E_{BB}$ )  $\sim 0.1\text{eV}$

# Life time : kink in $\text{Im}\Sigma$ at $\sim E_{\text{BB}}$

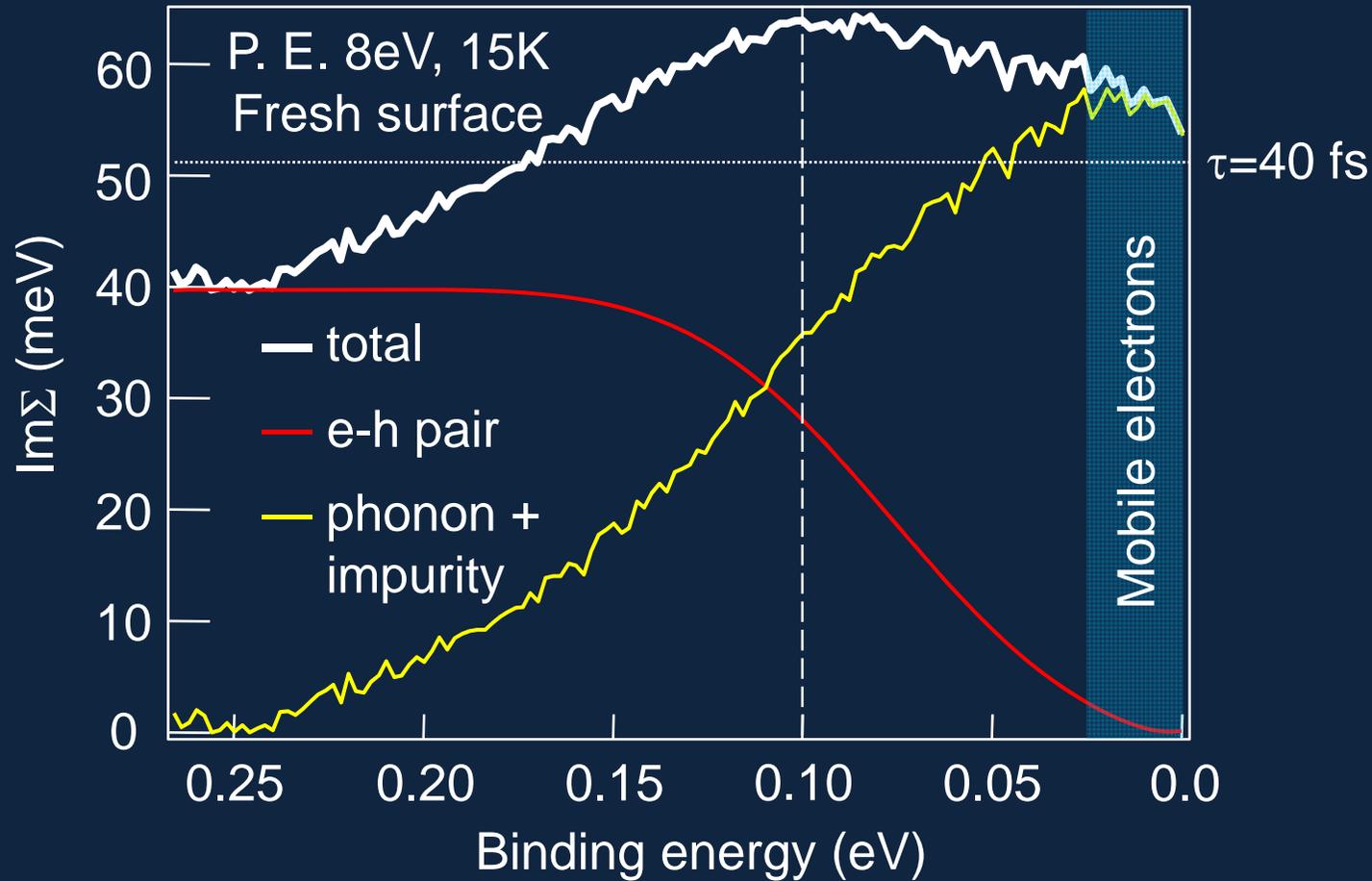


# Scattering channels



- Kink in  $\text{Im}\Sigma$  at around  $E_{BB}$  is originated from scattering due to phonon or impurity

# Surface electron lifetime



$$l_m = \tau \times v_g = 40 \cdot 10^{-15} (s) \times 5 \cdot 10^5 (m/s) = 0.02 (\mu m)$$

- Scattering to bulk states due to impurity is the main scattering channel for TM states.

## Quasi-particle scattering and protected nature of topological states in a parent topological insulator $\text{Bi}_2\text{Se}_3$

S. R. Park<sup>1</sup>, W. S. Jung<sup>1</sup>, Chul Kim<sup>1</sup>, D. J. Song<sup>1</sup>, C. Kim<sup>1,\*</sup>, S. Kimura<sup>2</sup>, K. D. Lee<sup>3</sup> and N. Hur<sup>3</sup>

<sup>1</sup>*Institute of Physics and Applied Physics, Yonsei University, Seoul, Korea*

<sup>2</sup>*UVSOR Facility, Institute for Molecular Science and The Graduate University for Advanced Studies, Okazaki 444-8585, JAPAN and*

<sup>3</sup>*Department of Physics, Inha University, Incheon 402-751, Korea*

(Dated: November 24, 2009)

We report on angle resolved photoemission spectroscopic studies on a parent topological insulator (TI),  $\text{Bi}_2\text{Se}_3$ . The line width of the spectral function (inverse of the quasi-particle lifetime) of the topological metallic (TM) states shows an anomalous behavior. This behavior can be reasonably accounted for by assuming decay of the quasi-particles predominantly into bulk electronic states through electron-electron interaction and defect scattering. Studies on aged surfaces reveal that topological metallic states are very much unaffected by the potentials created by absorbed atoms or molecules on the surface, indicating that topological states could be indeed protected against weak perturbations.

. To appear in PRB(R)

# Summary

## Experimental observation

- Kink in scattering rate at around bulk conduction band bottom

## Interpretation

- Strong scattering between surface and bulk electrons due to electron-phonon coupling or impurity near  $E_F$
- Carrier life time in TM states hardly affected by adsorbate created disorder potential