

# Novel spin-orbit coupled electronic states in Ir oxides

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# Outline

- Background: why 5d transition metal oxide?
- $\text{Sr}_2\text{IrO}_4$ 
  - ✓ Novel spin-orbit integrated  $J_{\text{eff}}=1/2$  state
  - ✓ Anisotropic exchange interaction
    - Kim et al., PRL 101, 076402 (2008)
    - Jin et al., Phys. Rev. B 80, 075112(2009)
    - Moon et al., PRL 101, 226402 (2008)
- $\text{Na}_2\text{IrO}_3$ 
  - ✓ anti-ferromagnetic order with spin-orbit Zeeman field
  - ✓  $\mathbb{Z}_2$  topological number?
    - Jin et al., arXiv:0907.0743
    - Kim et al., (to be published)



# Why 4d and 5d Transition Metal Oxides?

- Close to metal-insulator transition instability
  - ✓ 4d and 5d orbitals are more extended than 3d's
  - ✓ reduced on-site Coulomb interaction strength
  - ✓ sensitive to lattice distortion, magnetic order, etc.
- Strong spin-orbit (SO) couplings
  - ✓ large atomic numbers: relativistic effect
    - ▶  $V_{\text{SO}}(3d) \leq 50 \text{ meV}$
    - ▶  $V_{\text{SO}}(5d) \approx 500 \text{ meV}$



# Physics driven by spin-orbit (SO) coupling

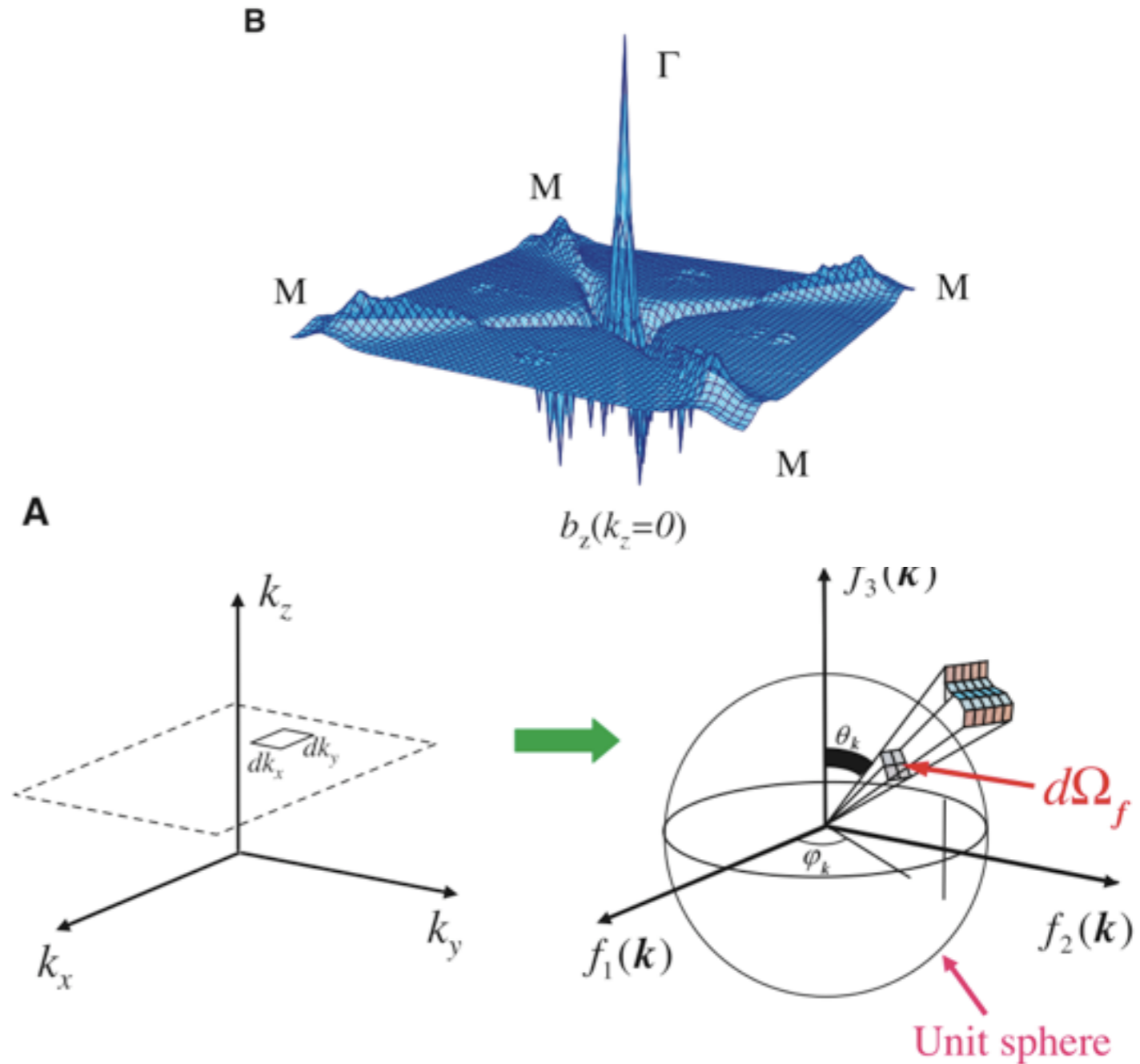
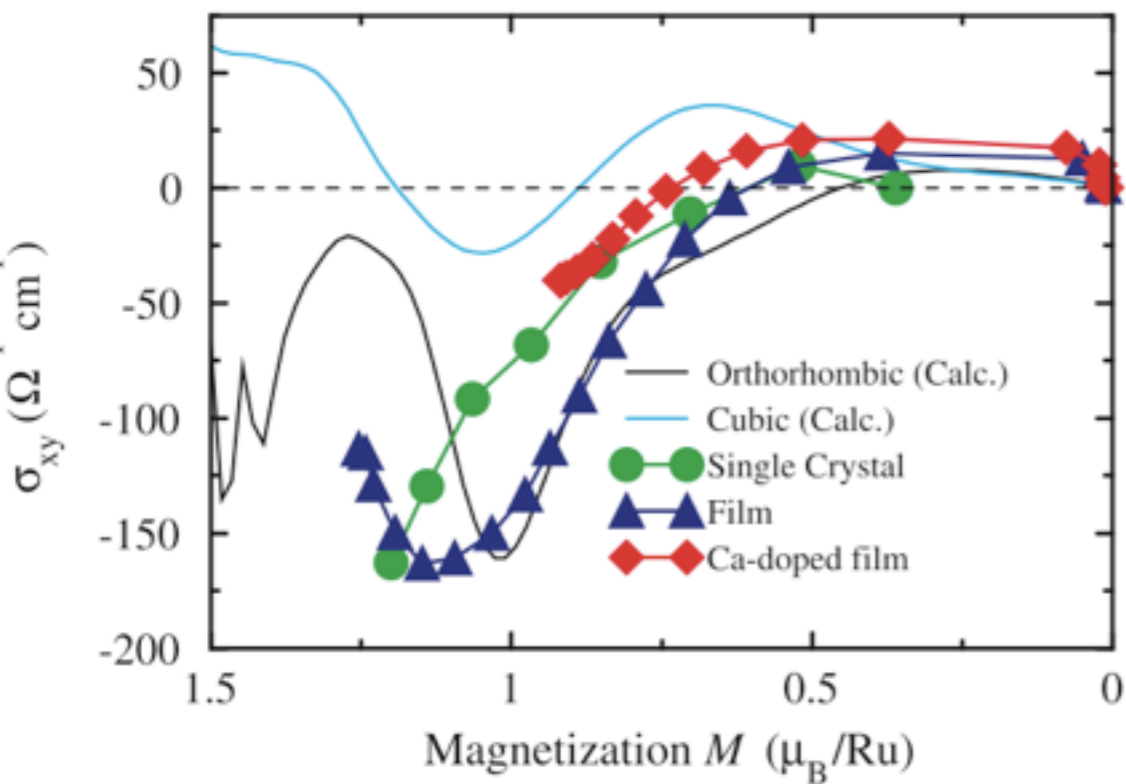
- Anisotropic magnetic exchange interactions:
  - ✓ Dzyaloshinskii-Moriya interaction
  - ✓ Multiferroic physics ...
- Anomalous Hall effect:
  - ✓  $\text{SrRuO}_3$
- Quantum spin Hall effect:
  - ✓ Spintronics
- Topological insulator
  - ✓ Magneto-electric effect, axion, ...



# Anomalous Hall effect and magnetic monopoles in momentum space

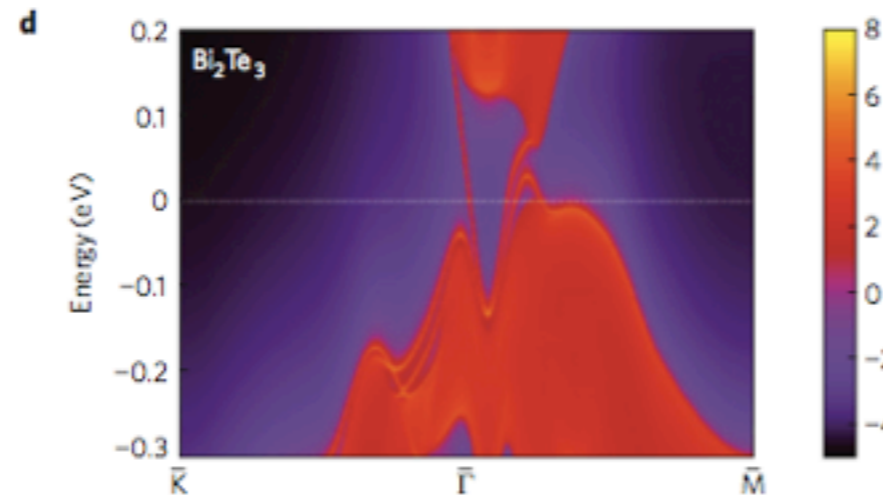
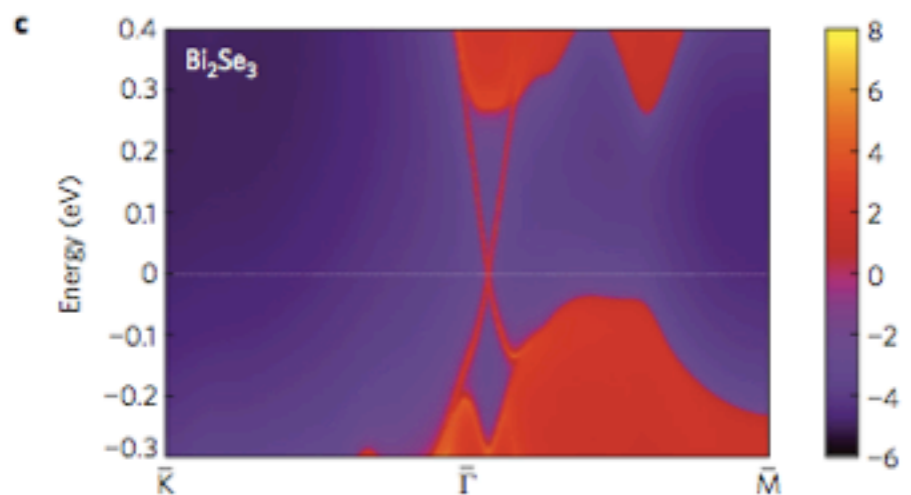
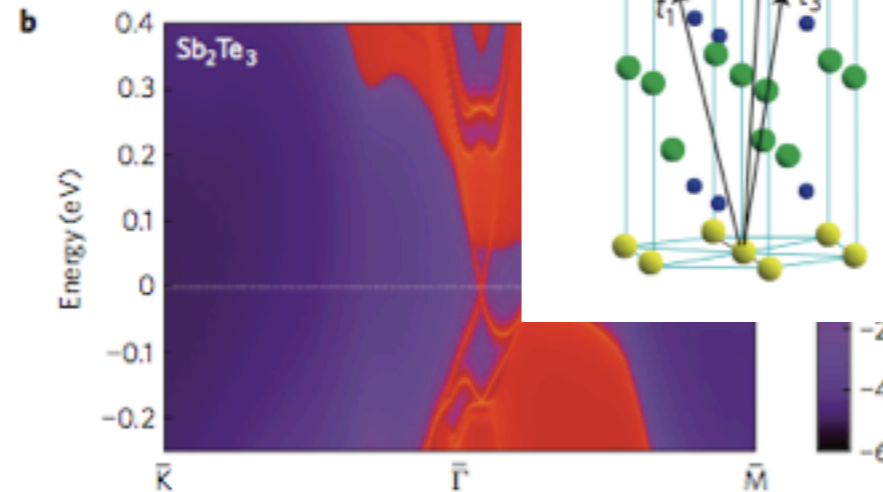
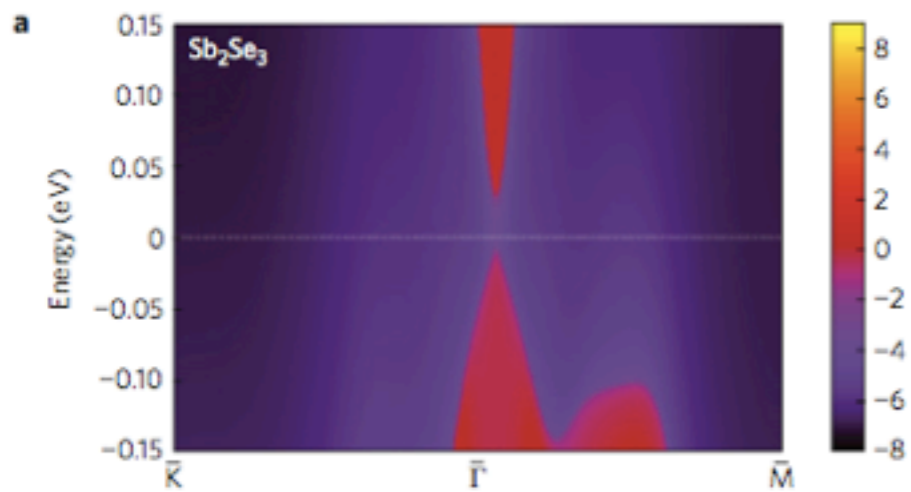
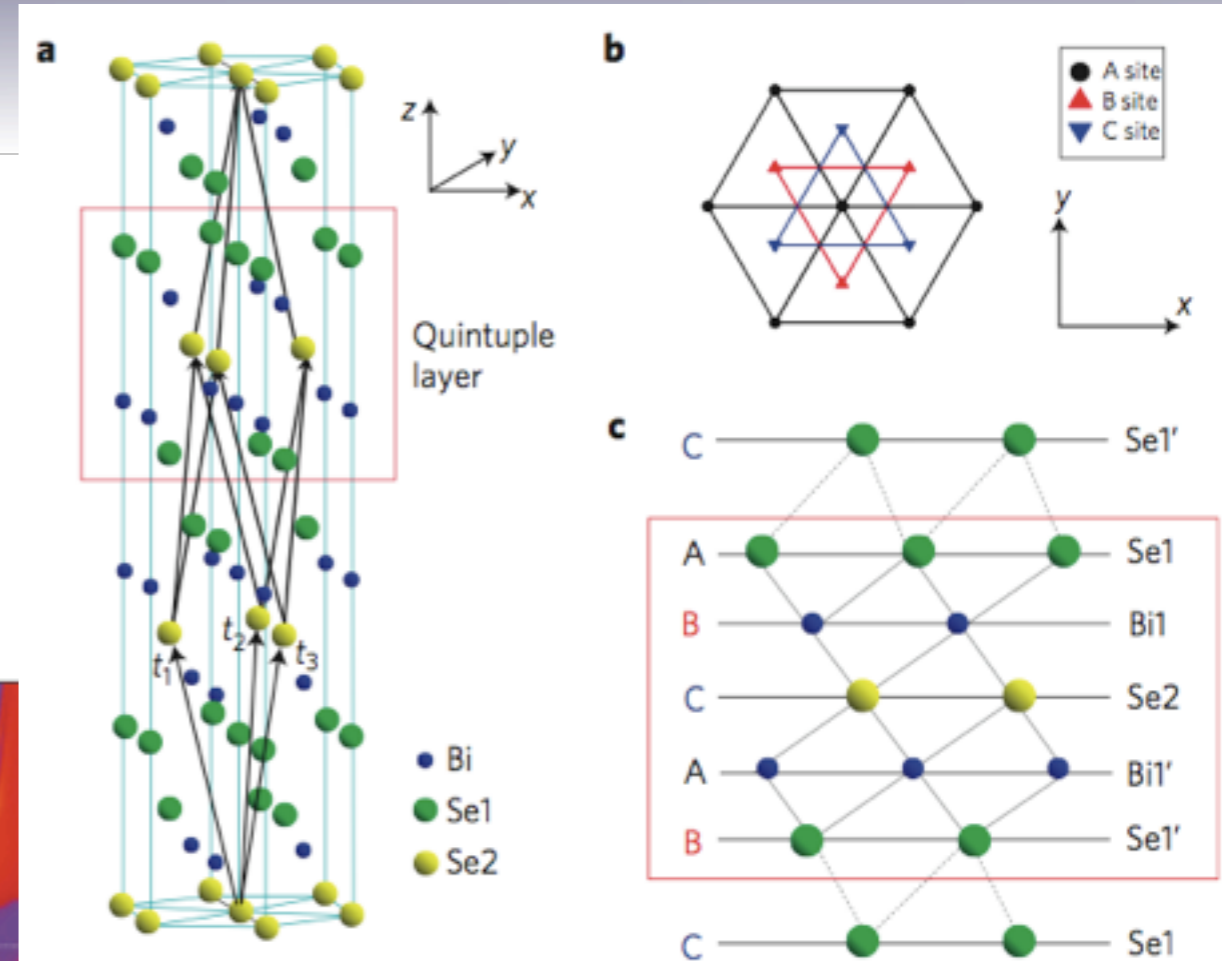
$$a_{n\mu}(\mathbf{k}) = i \langle u_{n\mathbf{k}} | \frac{\delta}{\delta \mathbf{k}_\mu} u_{n\mathbf{k}} \rangle \quad \sigma_{xy} = \sum_{n,\mathbf{k}} n_F[\varepsilon_n(\mathbf{k})] b_z(\mathbf{k}) \quad b_z(\mathbf{k}) = F_{xy}(\mathbf{k})$$

$$F_{\mu\nu} = \partial_{\mathbf{k}_\mu} a_{n\nu} - \partial_{\mathbf{k}_\nu} a_{n\mu}$$

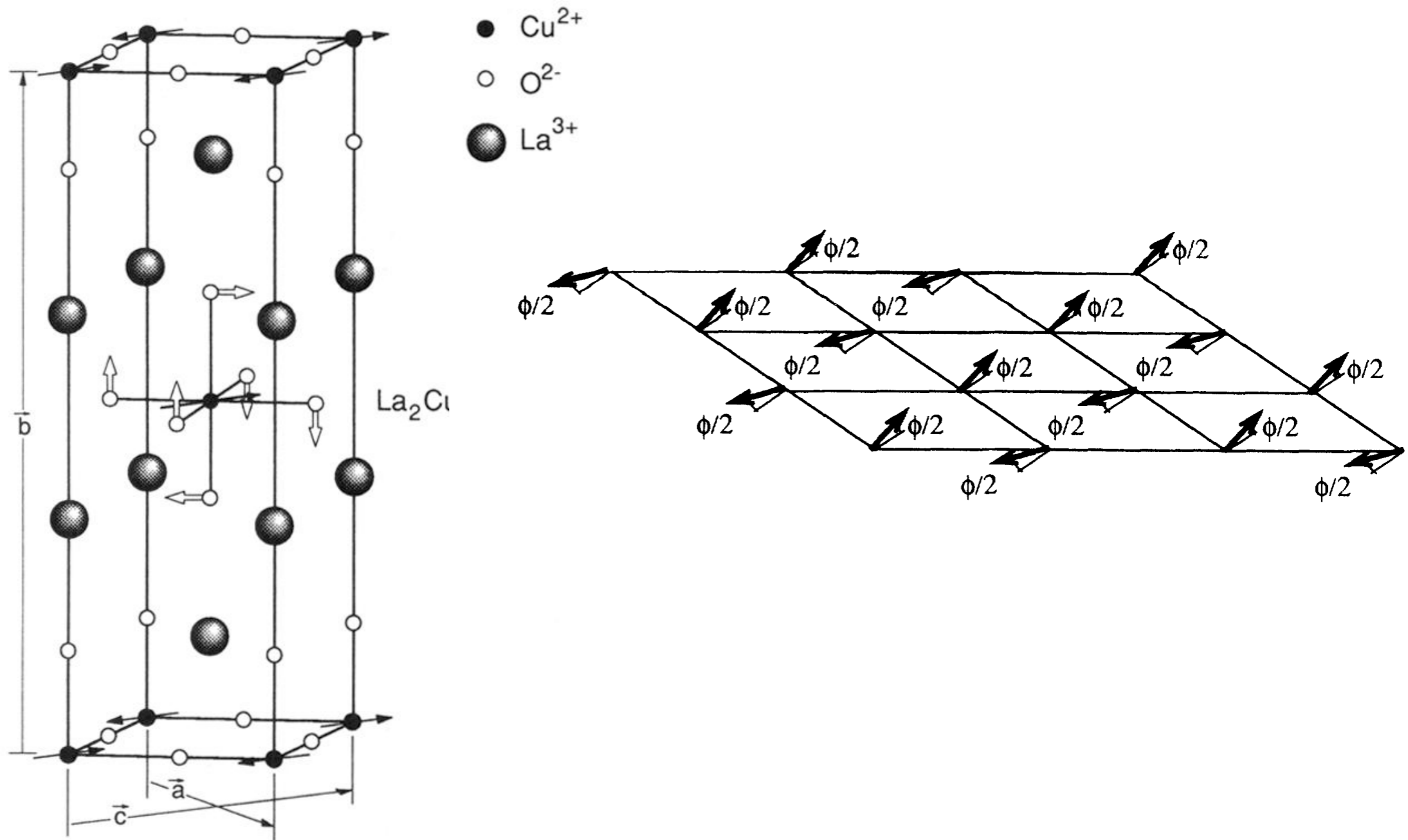


# Quantum spin Hall effect and Topological insulators

Topological insulators in  $\text{Bi}_2\text{Se}_3$ ,  $\text{Bi}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_3$  with a single Dirac cone on the surface



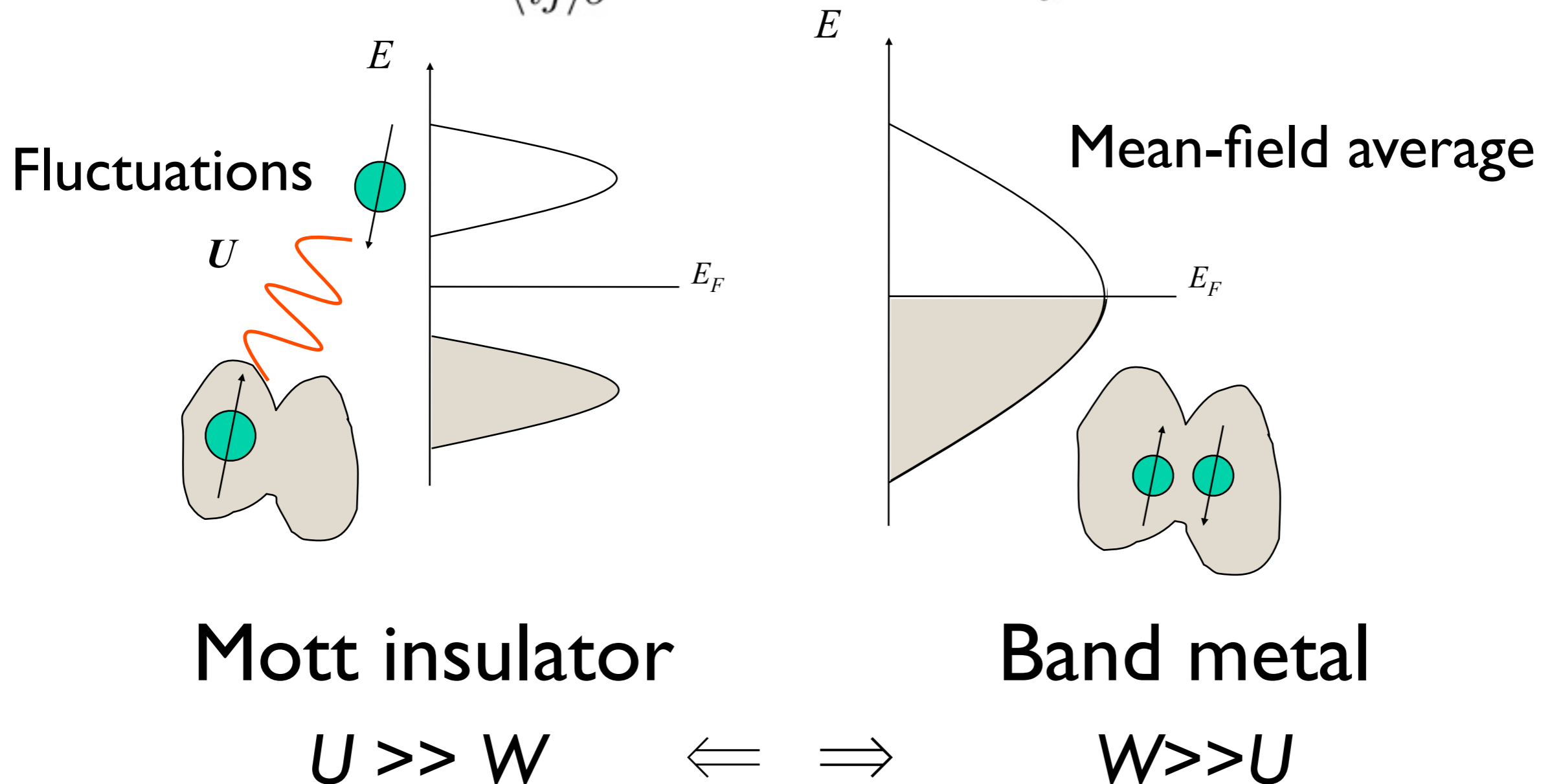
# Dzyaloshinskii-Moriya interactions in $\text{La}_2\text{CuO}_4$



# Metal-Insulator Transition

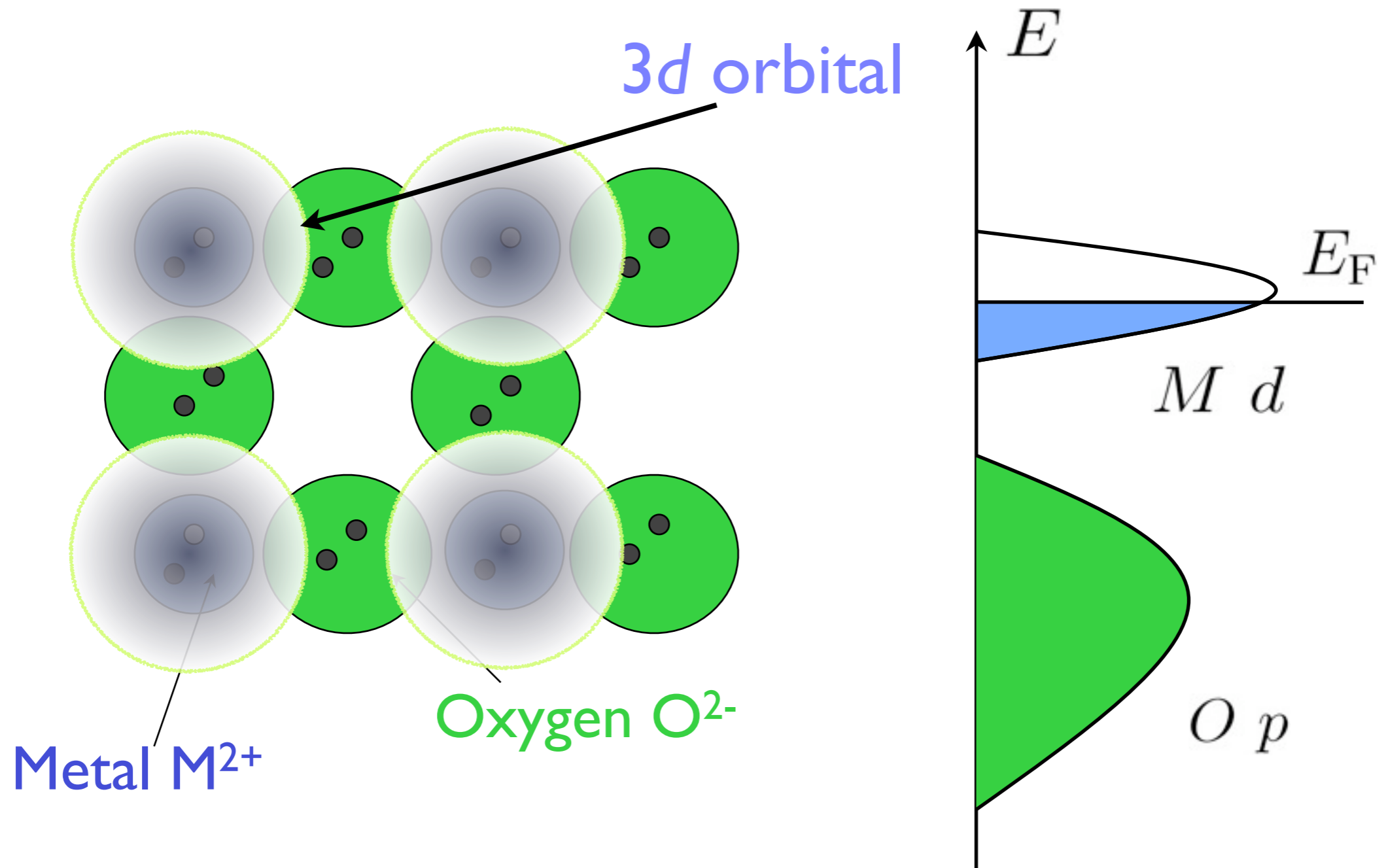
- Hubbard model:

$$H = \sum_{\langle ij \rangle \sigma} t_{ij} c_{i\sigma}^{\dagger} c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$





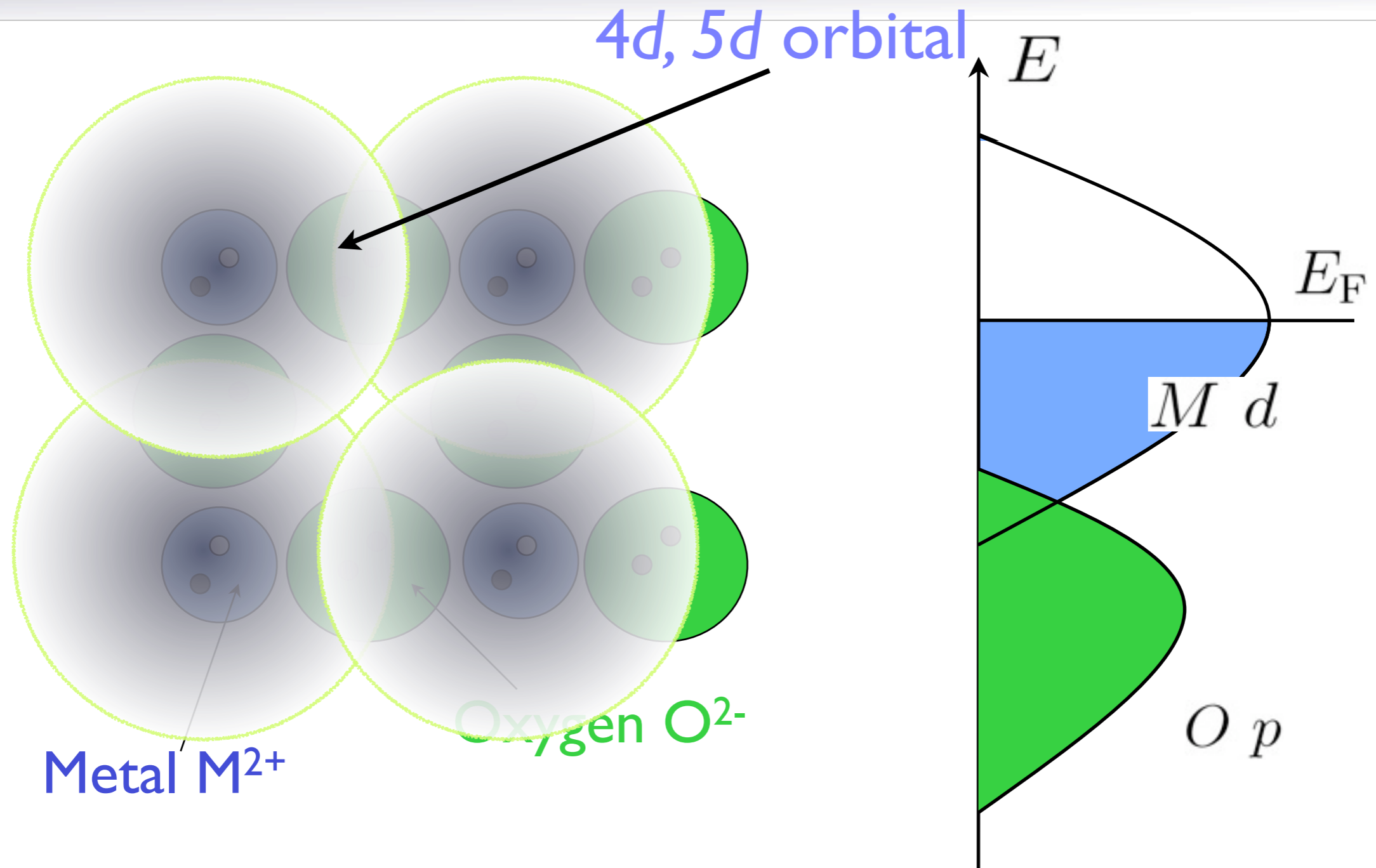
# 3d transition metal oxides (TMO)



Localized 3d orbital  $\rightarrow$  a narrow band!



# 4d and 5d transition metal oxides

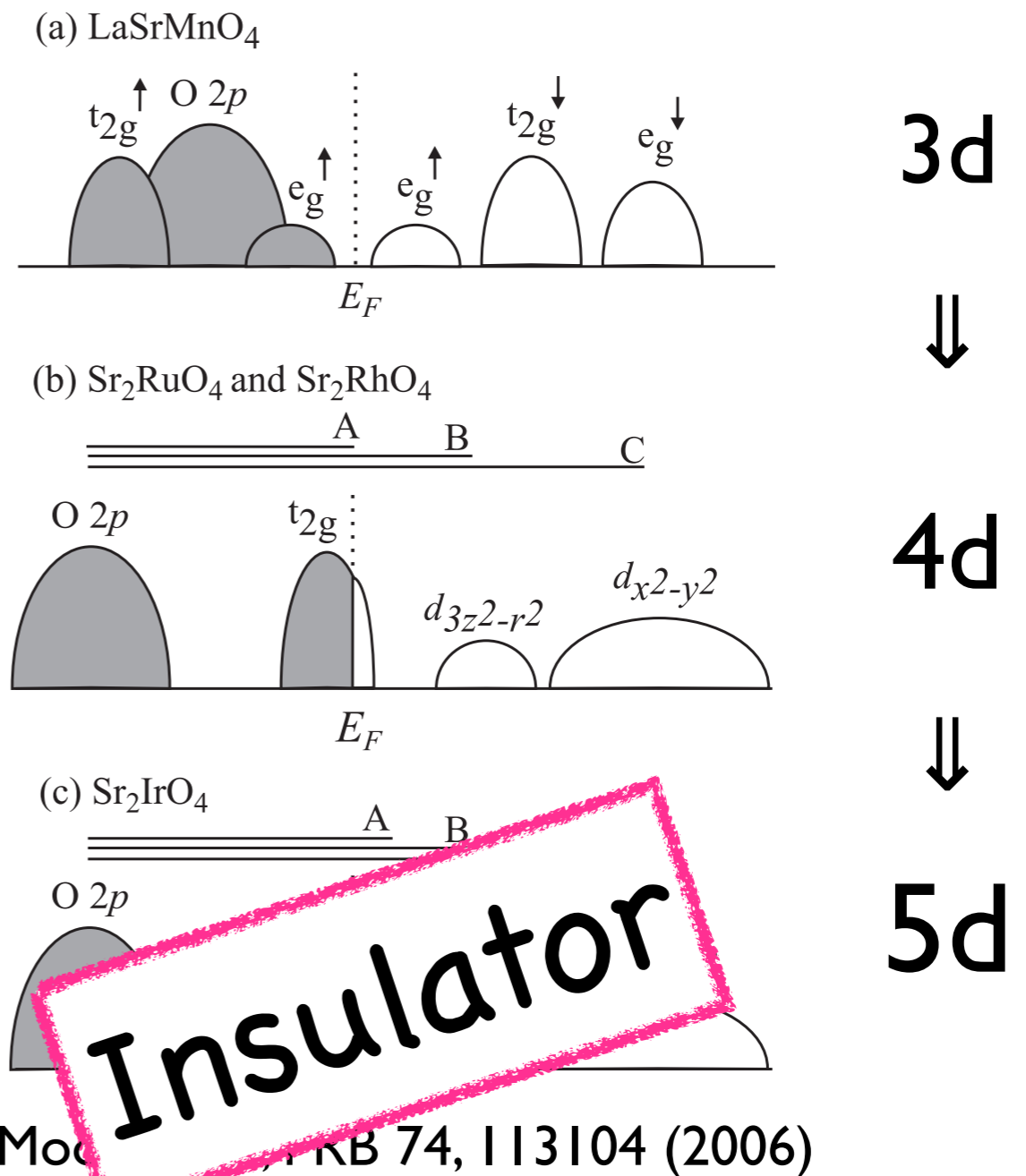
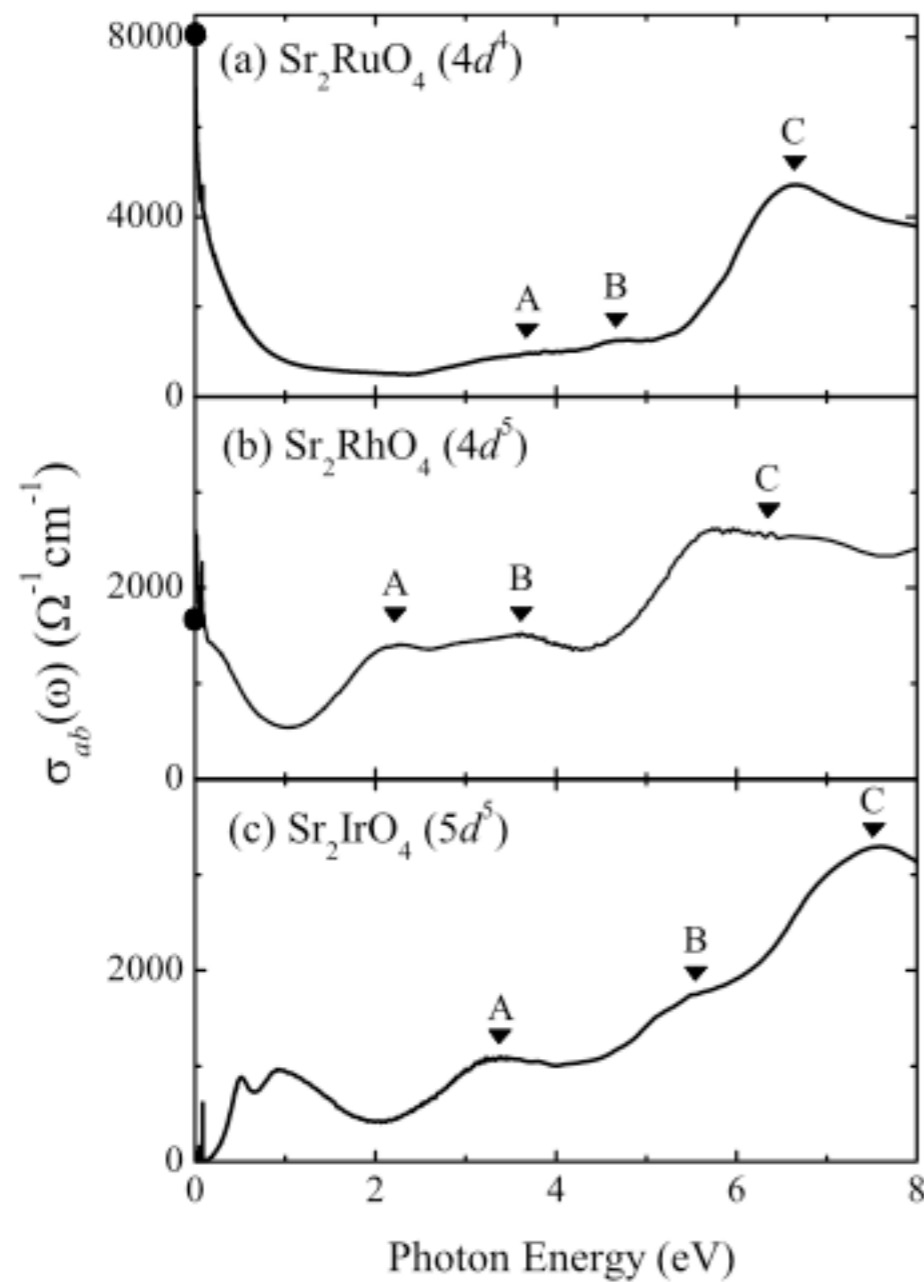


Extended 4d, 5d orbitals → **wider** band!



# 4d and 5d transition metal oxides?

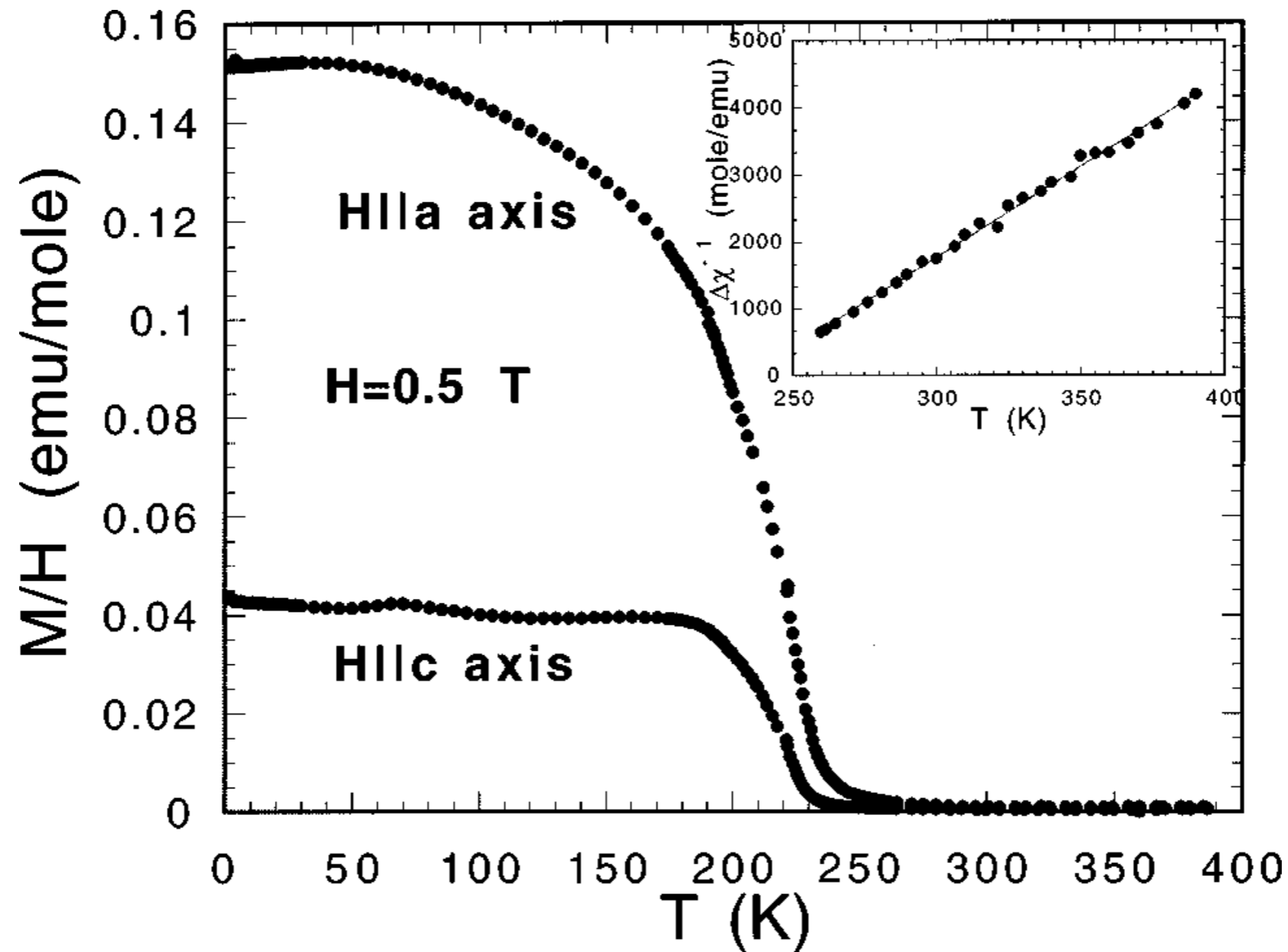
For the same  $K_2NiF_4$  structure:  $La_2CuO_4$



4d, 5d orbitals: more extended  $\rightarrow$  larger band width  
 $\rightarrow$  expect a metallic band structure in  $Sr_2IrO_4$ !??



# So why is $\text{Sr}_2\text{IrO}_4$ insulating?



Even more puzzling is that  $\text{Sr}_2\text{IrO}_4$  exhibits weak ferromagnetism!

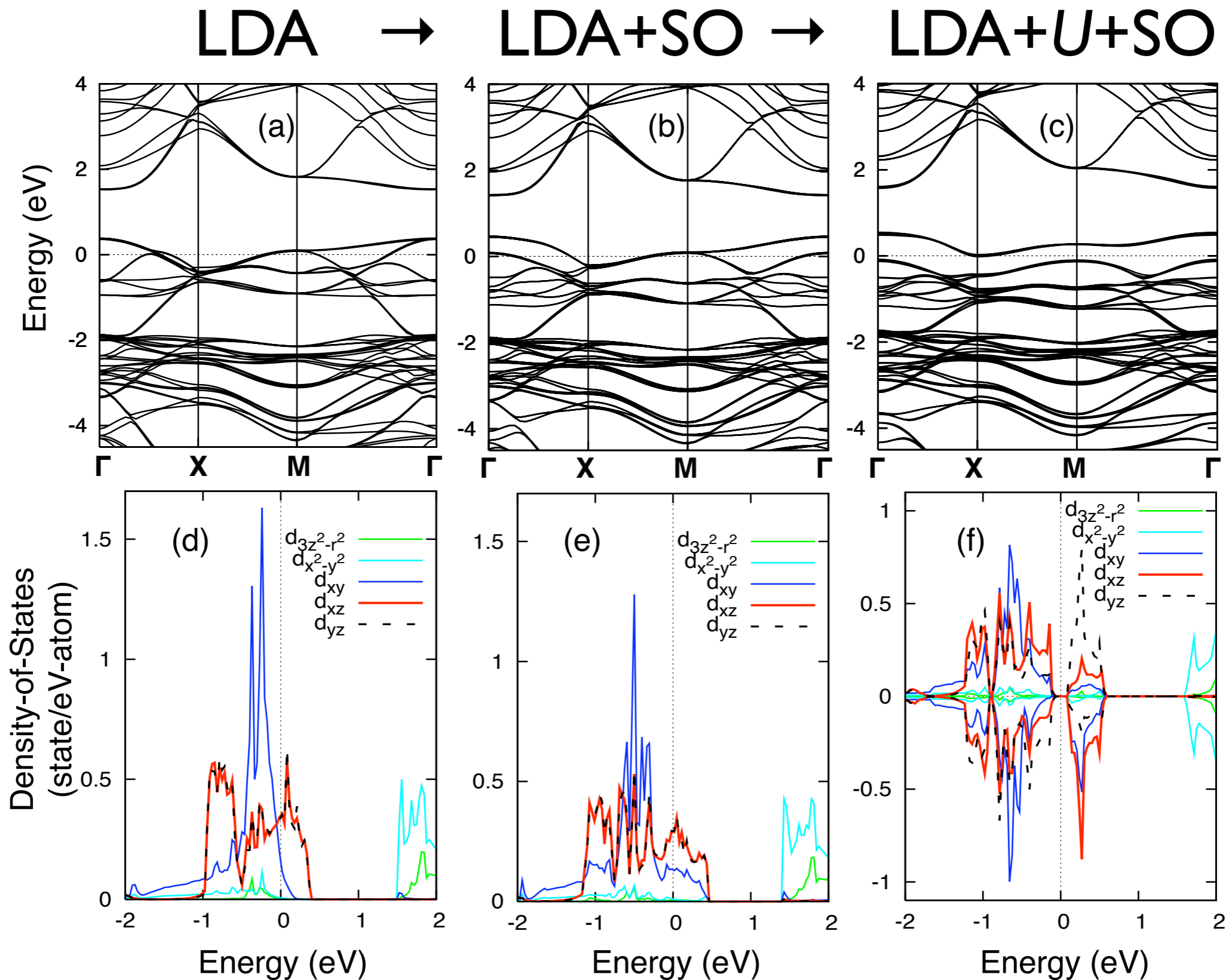


# Calculation methods

- OpenMX code (<http://www.openmx-square.org>)
- **LDA+U** methods
- Relativistic pseudo-potential including **spin-orbit terms**:  
**LDA+U+SO** calculations
- LDA exchange-correlation potential
- Non-collinear spin configurations

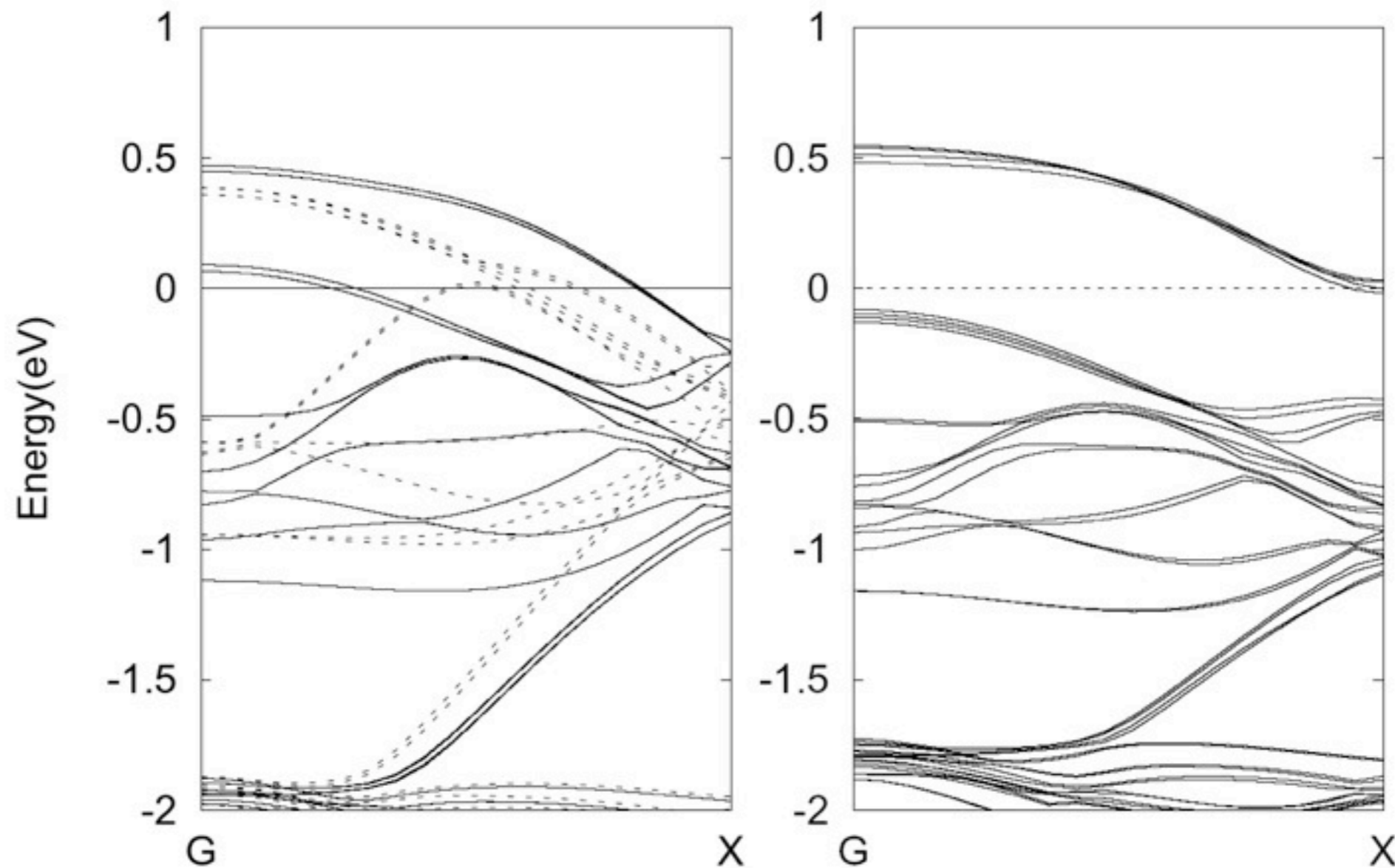


# Sr<sub>2</sub>IrO<sub>4</sub> band structure



# Tight-binding $t_{2g}$ bands of $\text{Sr}_2\text{IrO}_4$

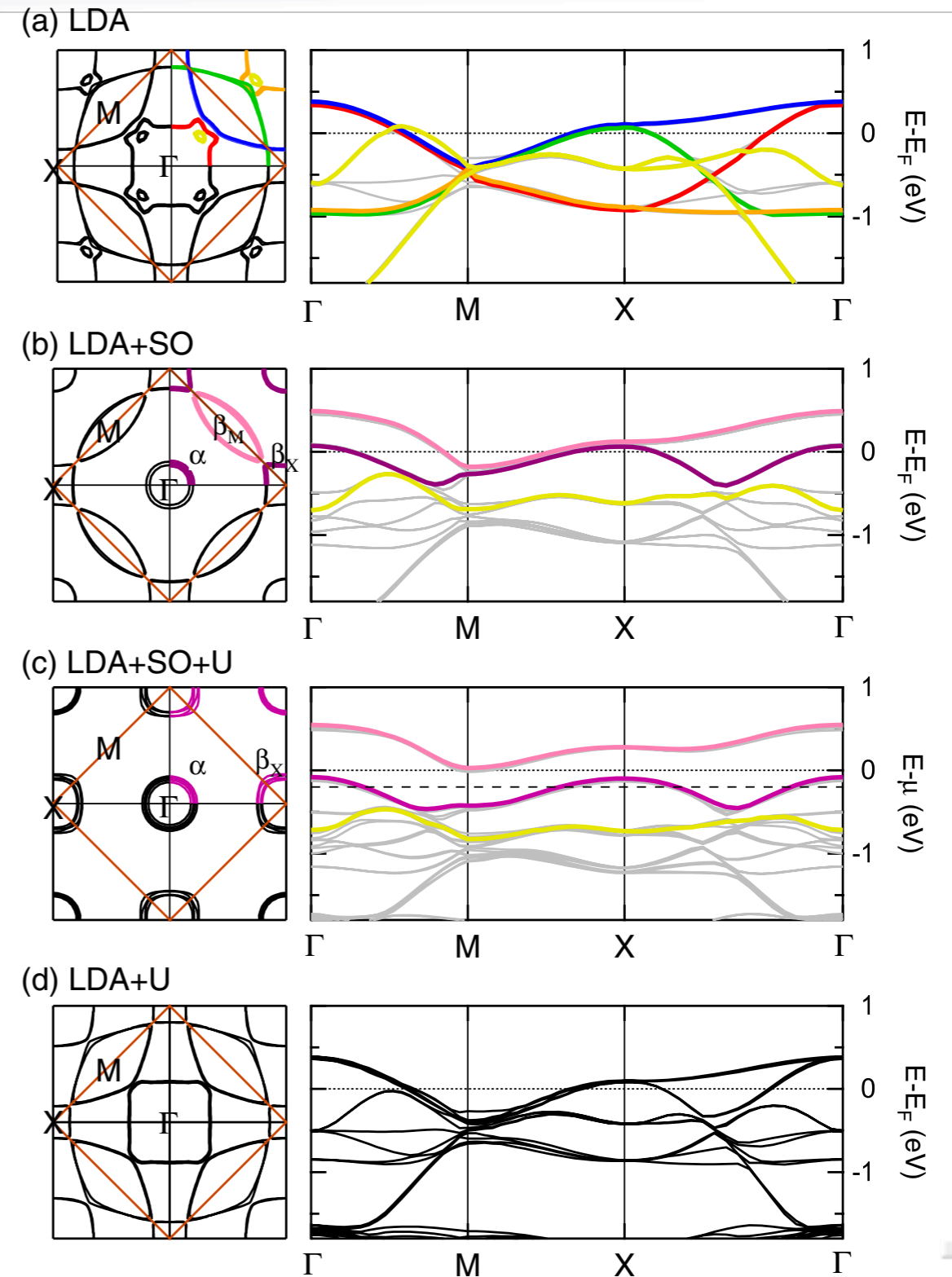
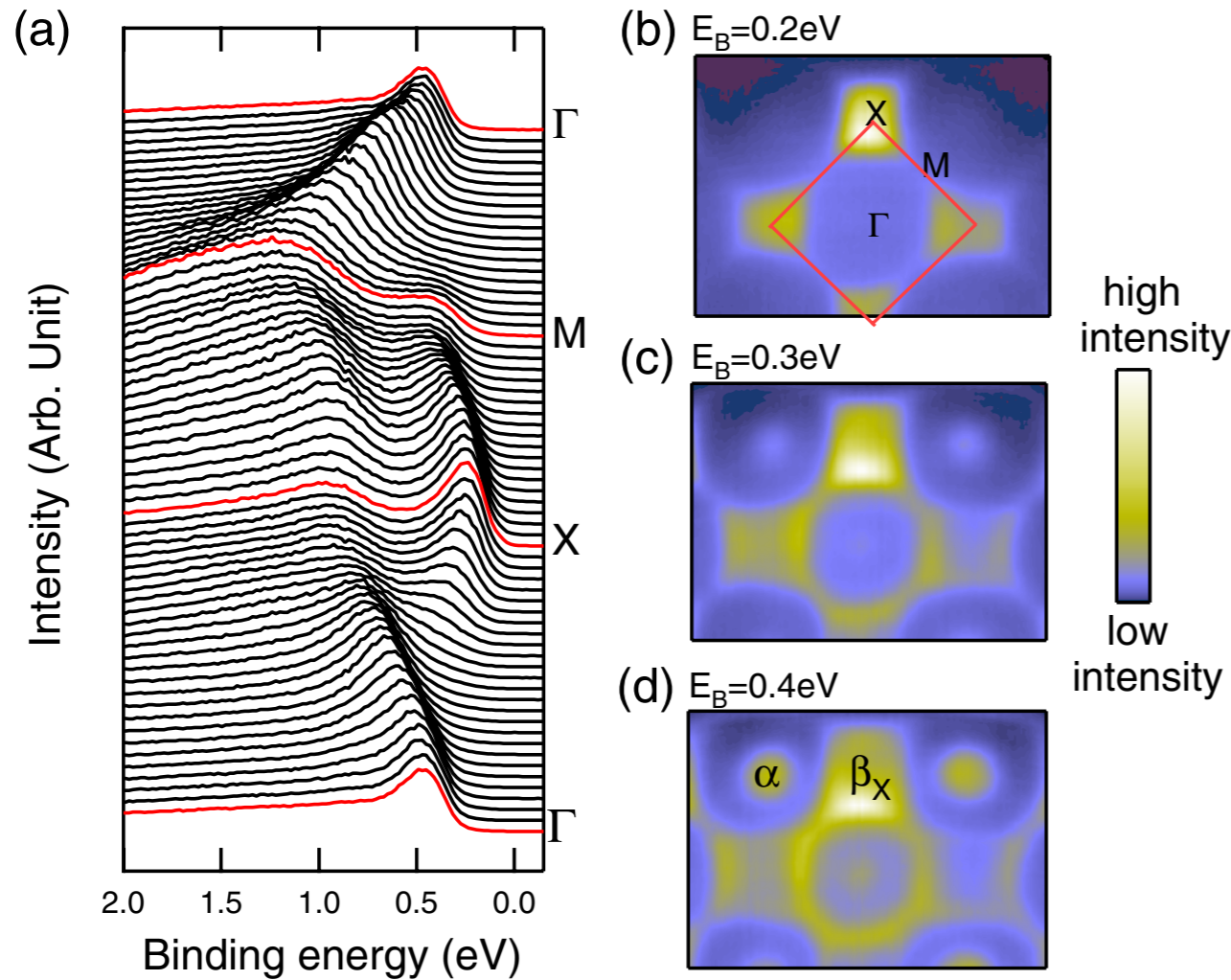
Evolution of  $t_{2g}$  bands by SO coupling and on-site U



LDA  $\rightarrow$  LDA+SO  $\rightarrow$  LDA+U+SO

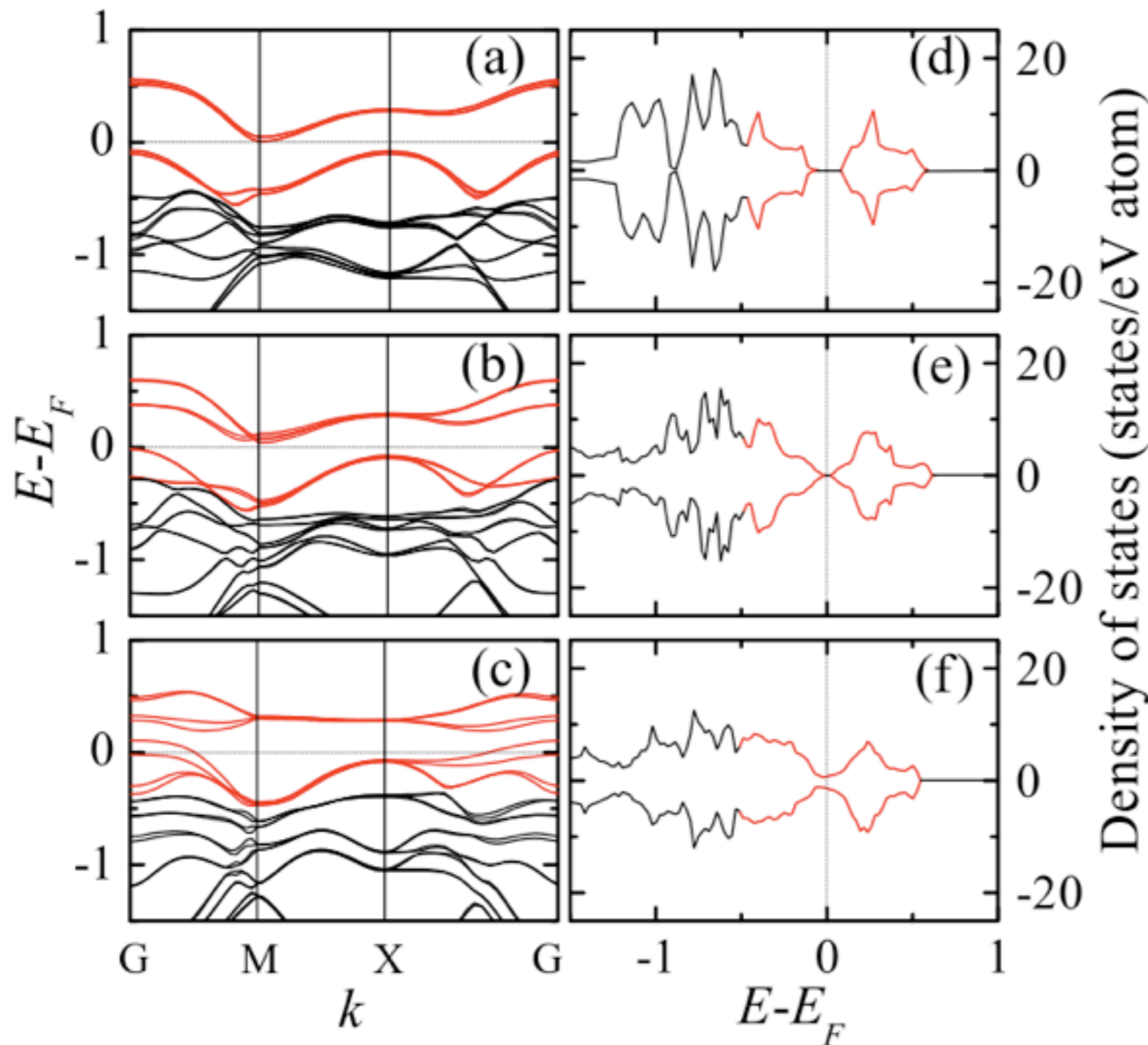


# Comparison with ARPES Experiment

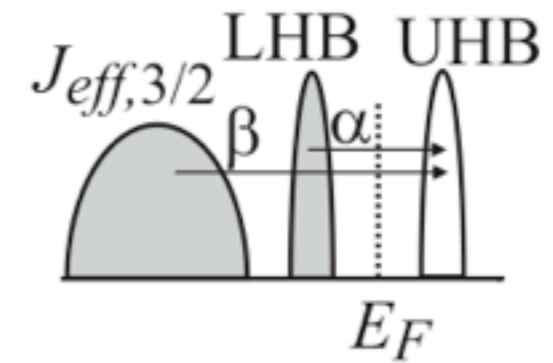




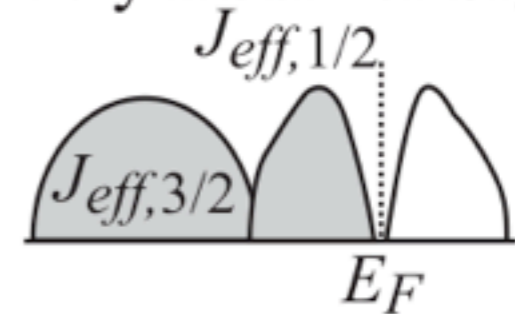
# Insulator-to-metal transition in $\text{Sr}_{n+1}\text{Ir}_n\text{O}_{3n+1}$



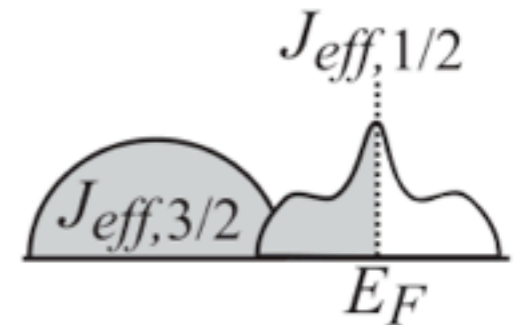
(a) Mott insulator  $\text{Sr}_2\text{IrO}_4$



(b) Barely insulator  $\text{Sr}_3\text{Ir}_2\text{O}_7$



(c) Correlated metal  $\text{SrIrO}_3$

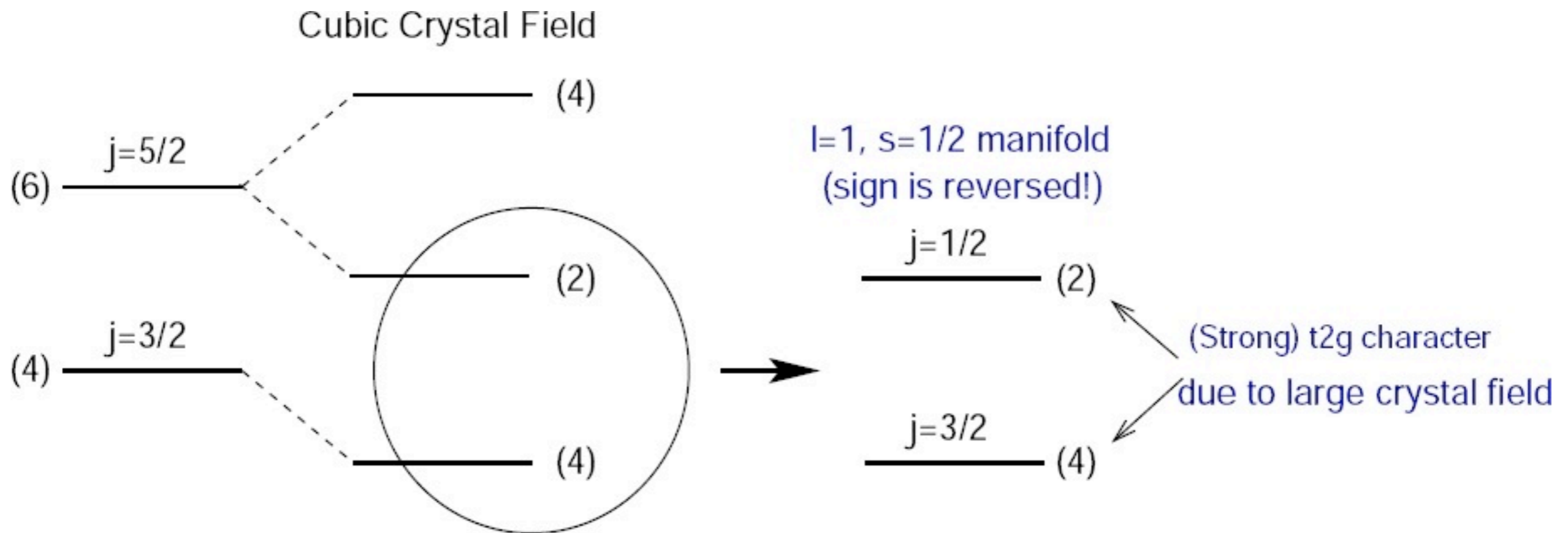


Increase of  $M$



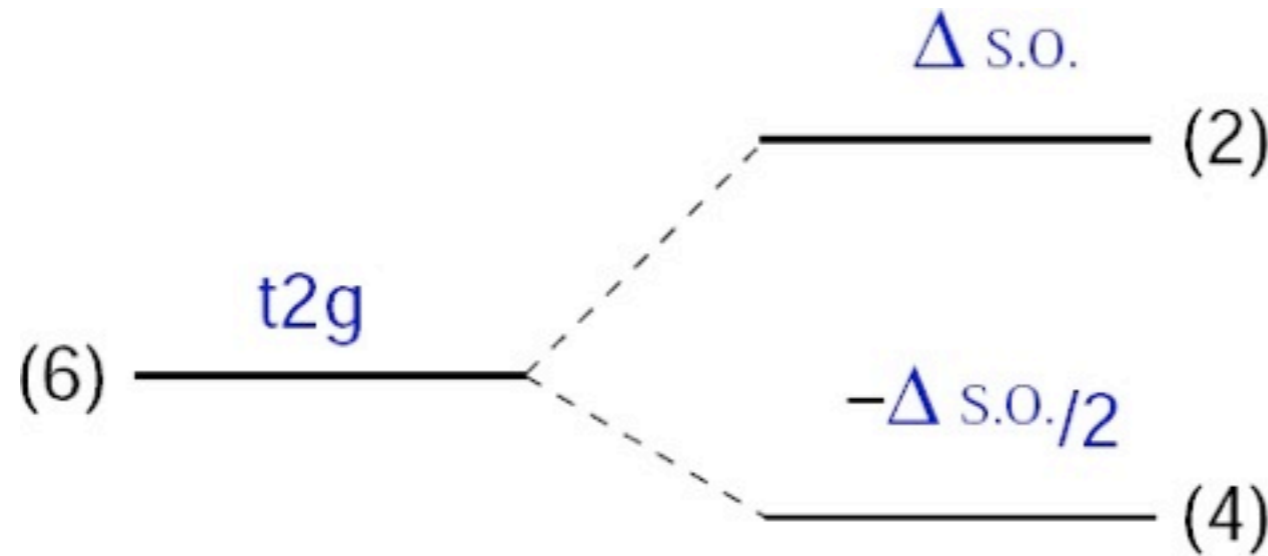
# Large $\lambda_{SO}$ coupling in the atomic limit

$$\mathcal{H}_{SO} = \lambda \mathbf{L} \cdot \mathbf{S} = \lambda \left[ L_z S_z + \frac{1}{2} (L_+ S_- + L_- S_+) \right]$$



# Small $\lambda_{SO}$ in the band limit

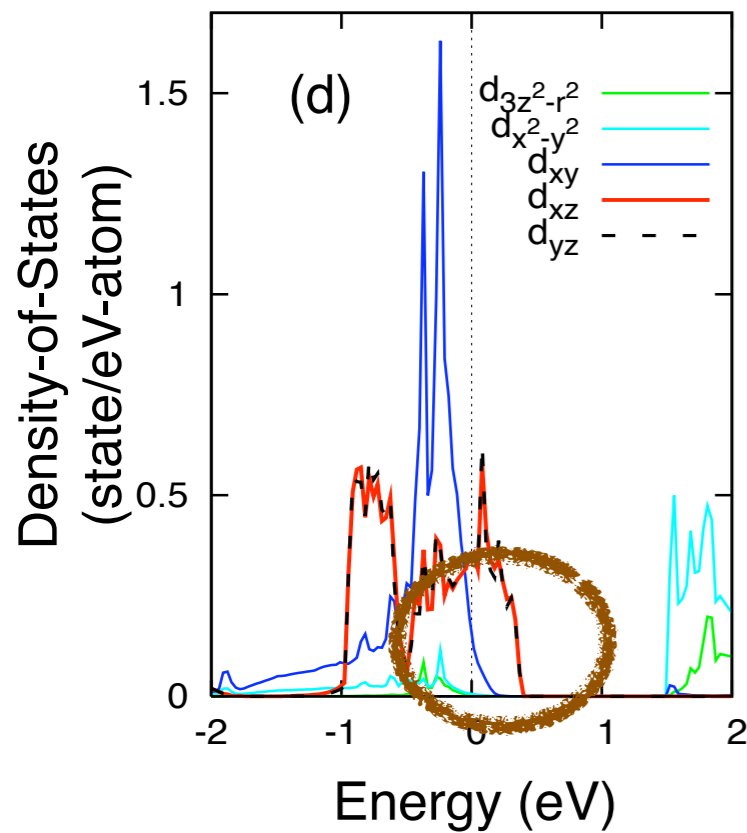
$$\mathcal{H}_{SO} = \lambda \mathbf{L} \cdot \mathbf{S} = \lambda \left[ L_z S_z + \frac{1}{2} (L_+ S_- + L_- S_+) \right]$$



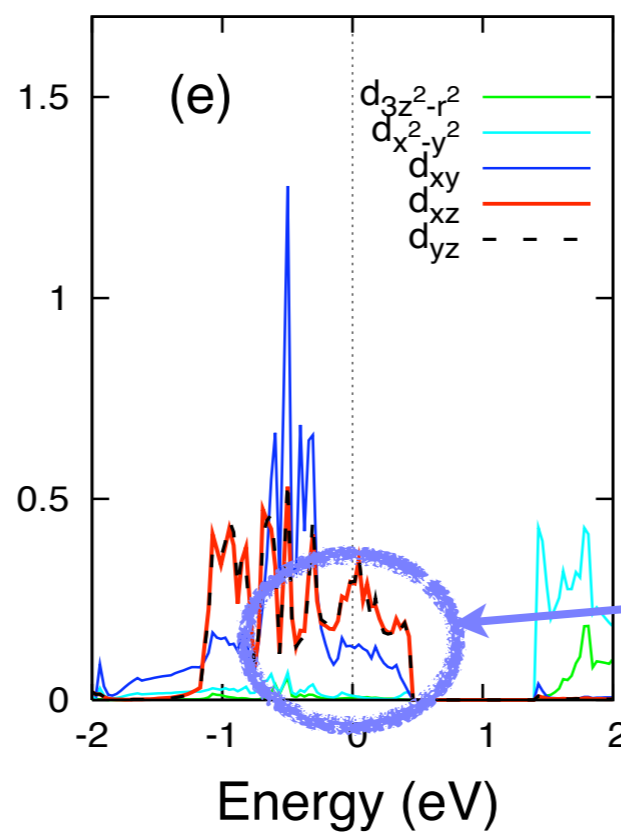
$$\begin{aligned} & |xy, \uparrow\rangle + |yz, \downarrow\rangle + i |zx, \downarrow\rangle, \\ & |xy, \downarrow\rangle - |yz, \uparrow\rangle + i |zx, \uparrow\rangle \end{aligned}$$

$$\begin{aligned} & |yz, \downarrow\rangle + i |zx, \downarrow\rangle \\ & |yz, \uparrow\rangle - i |zx, \uparrow\rangle \end{aligned}$$

$$\begin{aligned} & |xy, \uparrow\rangle - (|yz, \downarrow\rangle + i |zx, \downarrow\rangle)/2 \\ & |xy, \downarrow\rangle + (|yz, \uparrow\rangle - i |zx, \uparrow\rangle)/2 \end{aligned}$$



LDA

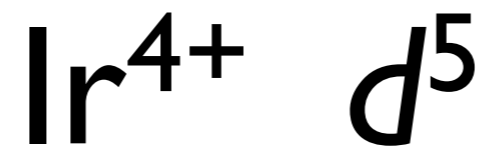
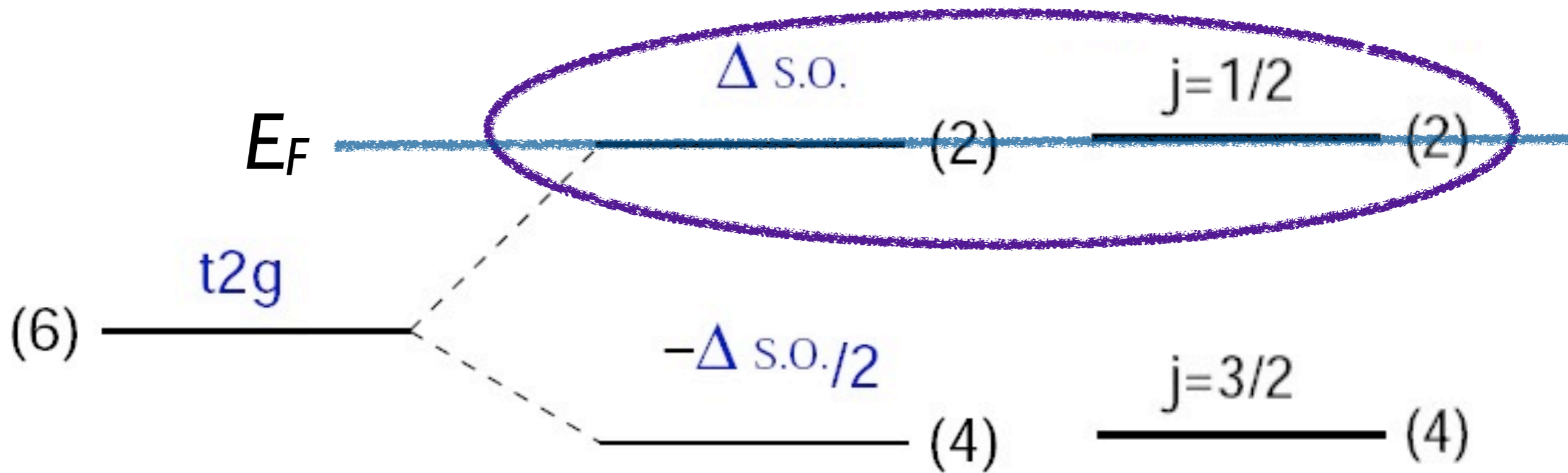


LDA+SO

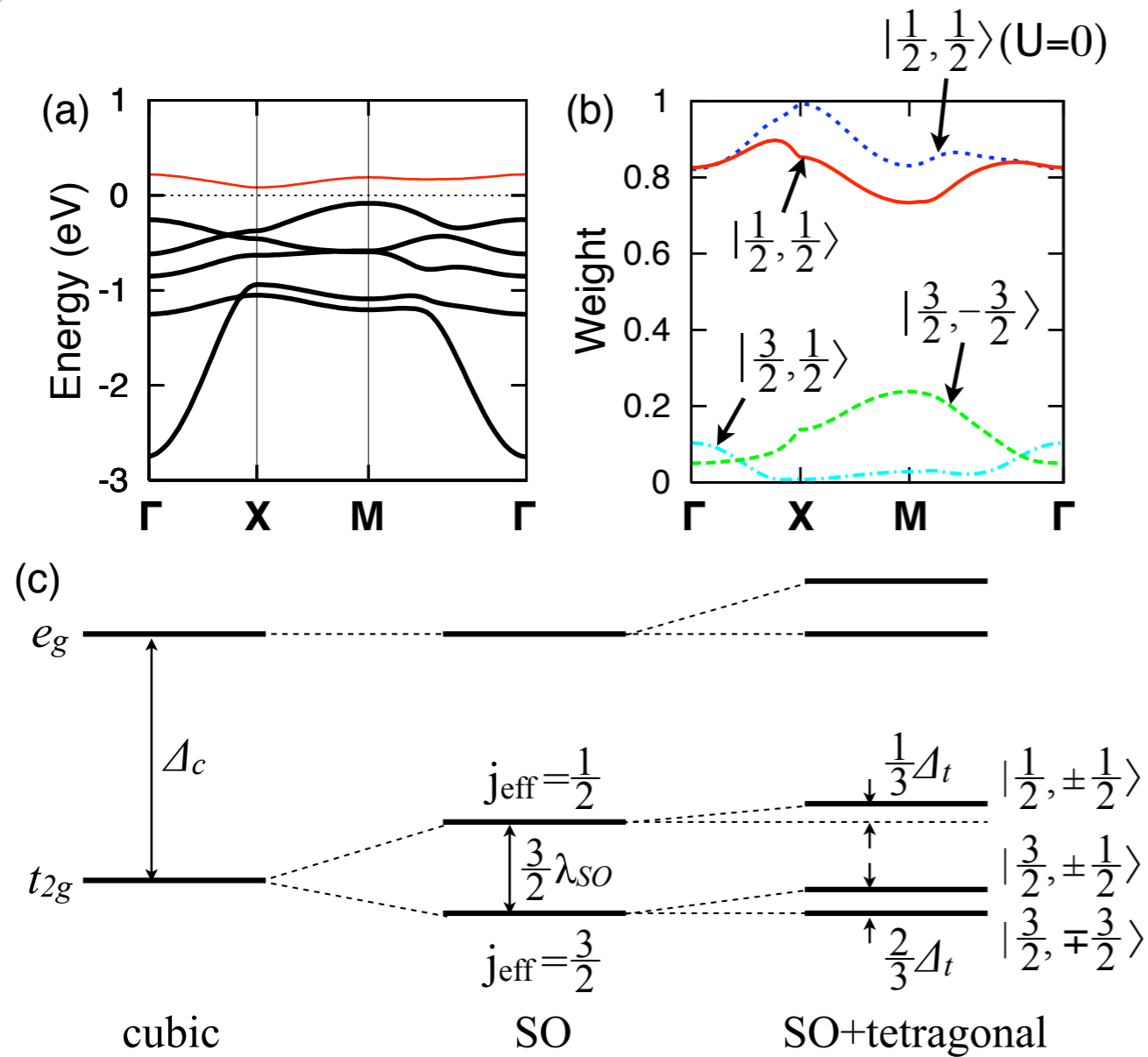
Increase of  $d_{xy}$ -component



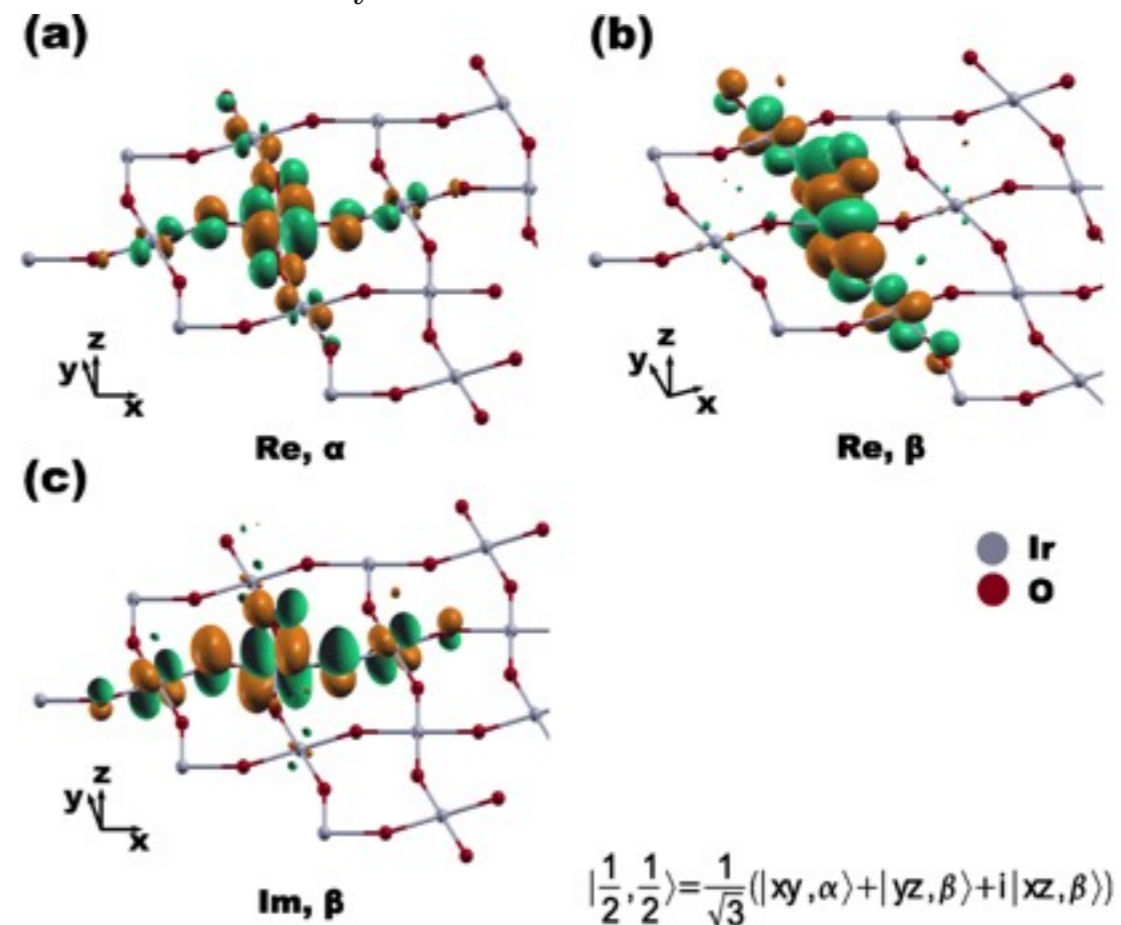
# Localized and Itinerant Pictures



# t2g tight-binding model and Wannier functions



$$\mathcal{H} = \sum_{\langle ij \rangle \alpha \beta \sigma} t_{ij}^{\alpha \beta} c_{i \alpha \sigma}^\dagger c_{j \beta \sigma} + \frac{1}{2} \sum_{i(\alpha \sigma) \neq (\beta \sigma')} U^{\alpha \beta} n_{i \alpha \sigma} n_{i \beta \sigma'} + \lambda_{\text{SO}} \sum_i \mathbf{L}_i \cdot \mathbf{S}_i$$



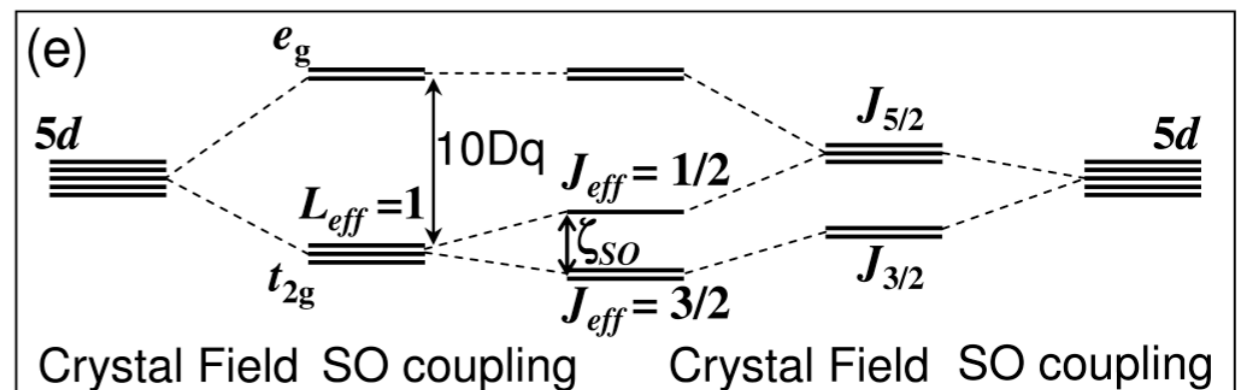
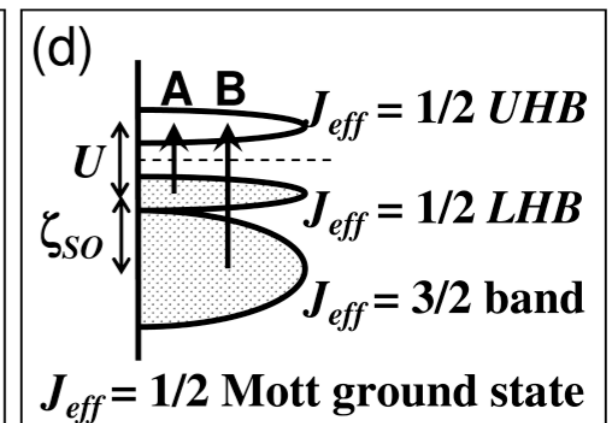
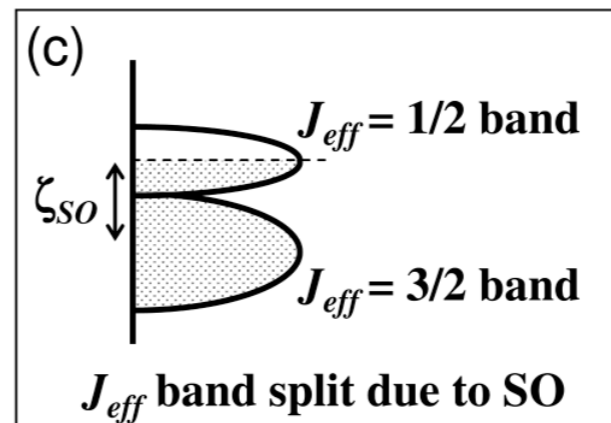
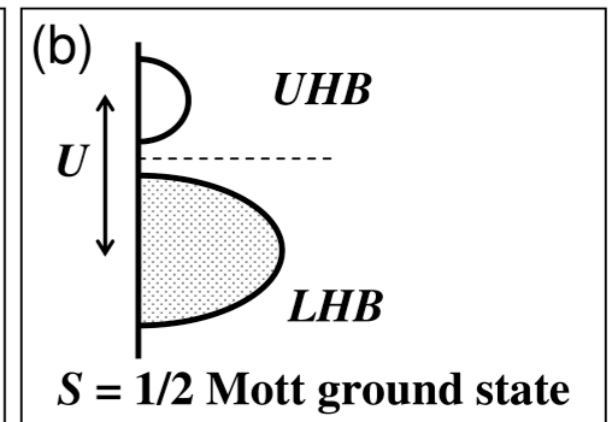
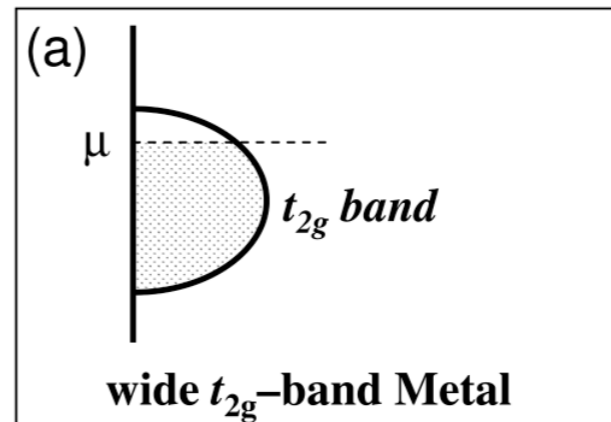
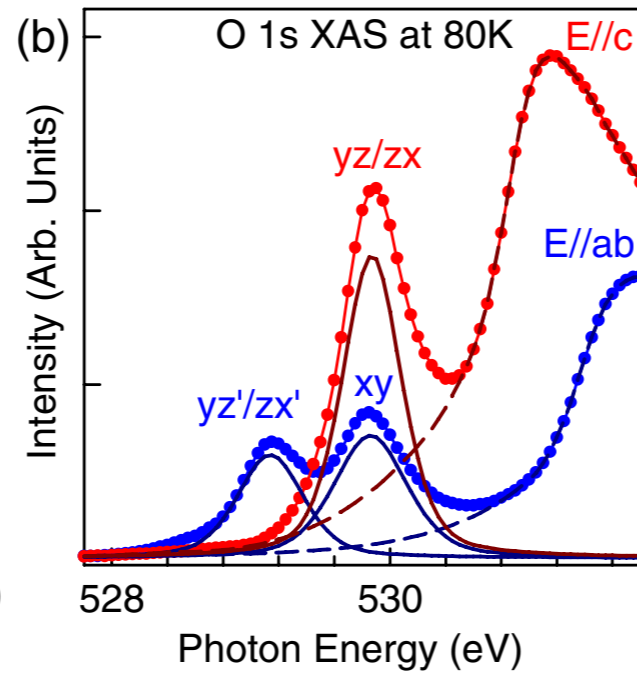
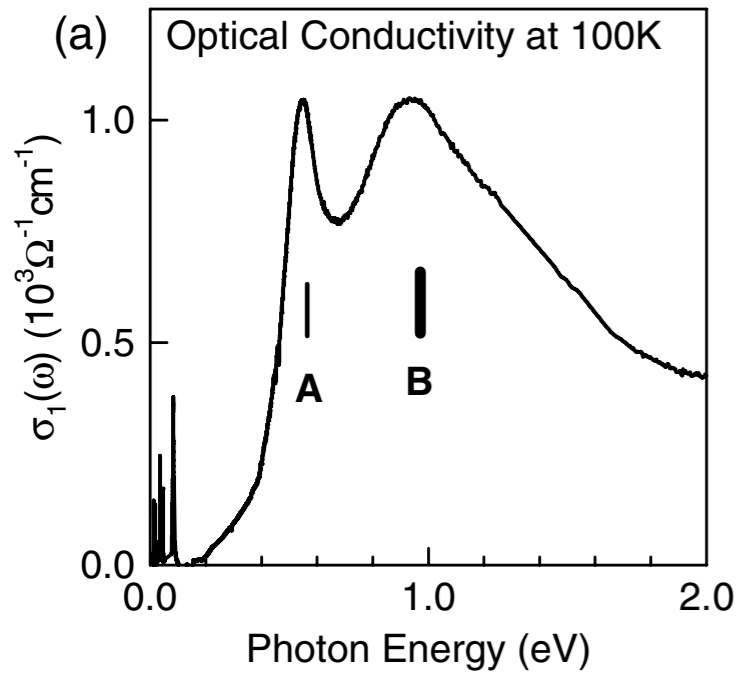
$$|j_{\text{eff}} = 1/2, \pm 1/2\rangle = \mp \frac{1}{\sqrt{3}} |xy\rangle |\pm\rangle - \frac{1}{\sqrt{3}} (|yz\rangle \pm i|zx\rangle) |\mp\rangle$$

**Robust  $J_{\text{eff}}=1/2$  spin-orbit integrated state**

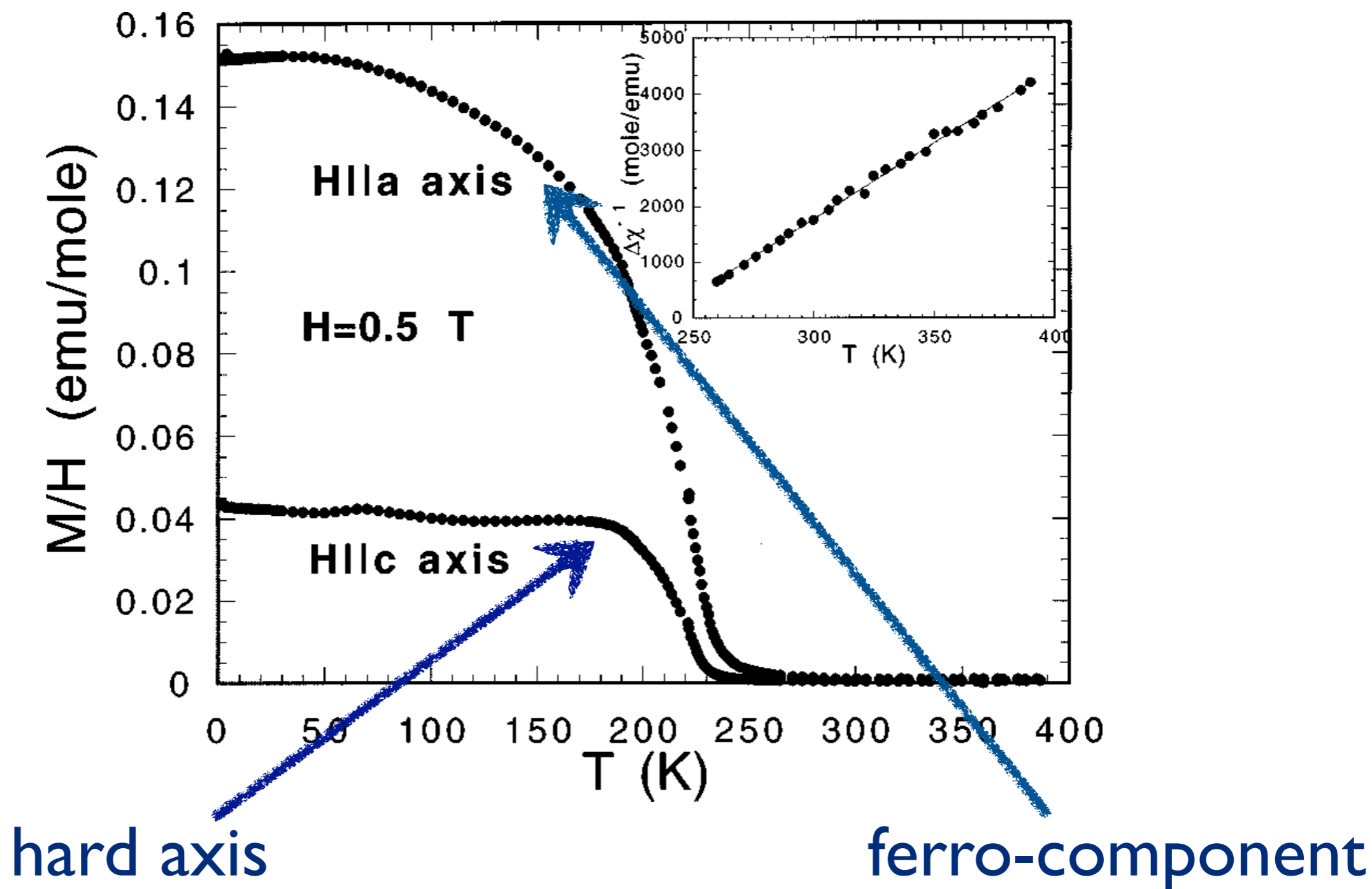


# Sr<sub>2</sub>IrO<sub>4</sub>: $J_{\text{eff}}=1/2$ Mott insulator

$$|j_{\text{eff}} = 1/2, \pm 1/2\rangle = \mp \frac{1}{\sqrt{3}} |xy\rangle |\pm\rangle - \frac{1}{\sqrt{3}} (|yz\rangle \pm i|zx\rangle) |\mp\rangle$$



# Now what about magnetism in $\text{Sr}_2\text{IrO}_4$ ?

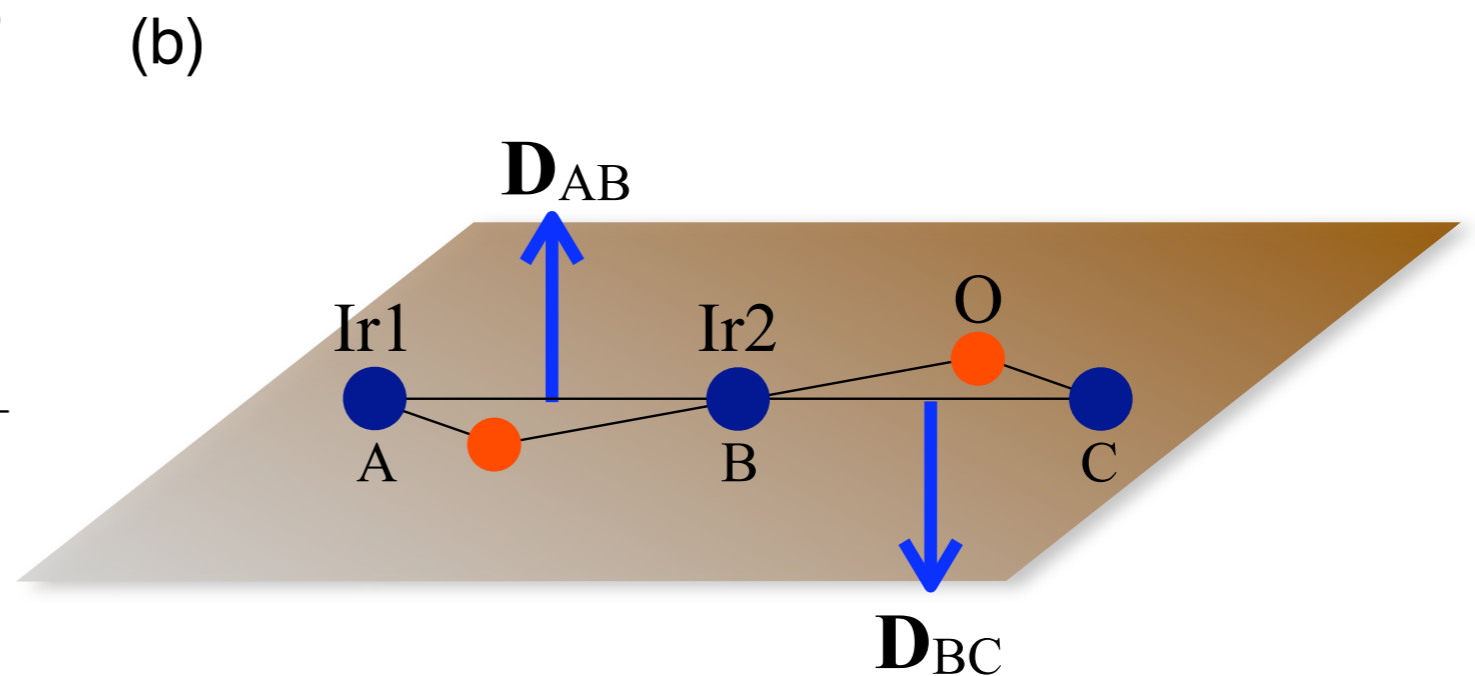
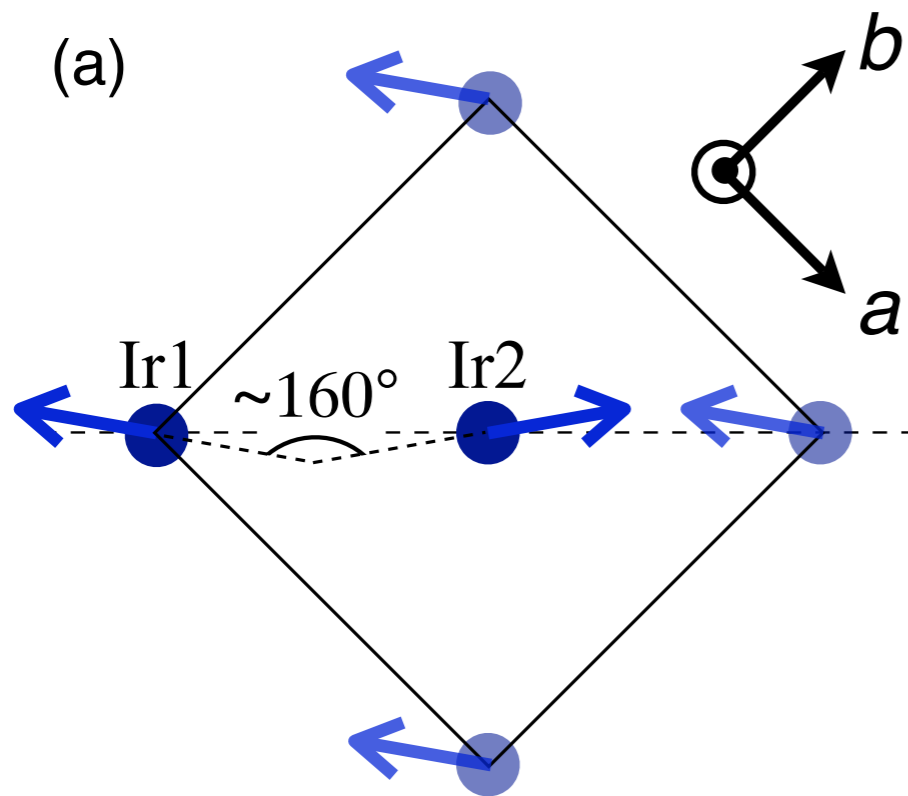


# Canted Antiferromagnetic State: $\text{Sr}_2\text{IrO}_4$

LDA+U+SO calculation predicts canted AF ordering

$$m_{\text{AFM}} = 0.36 \mu_{\text{B}}$$

$$m_{\text{C}} = 0.063 \mu_{\text{B}}$$

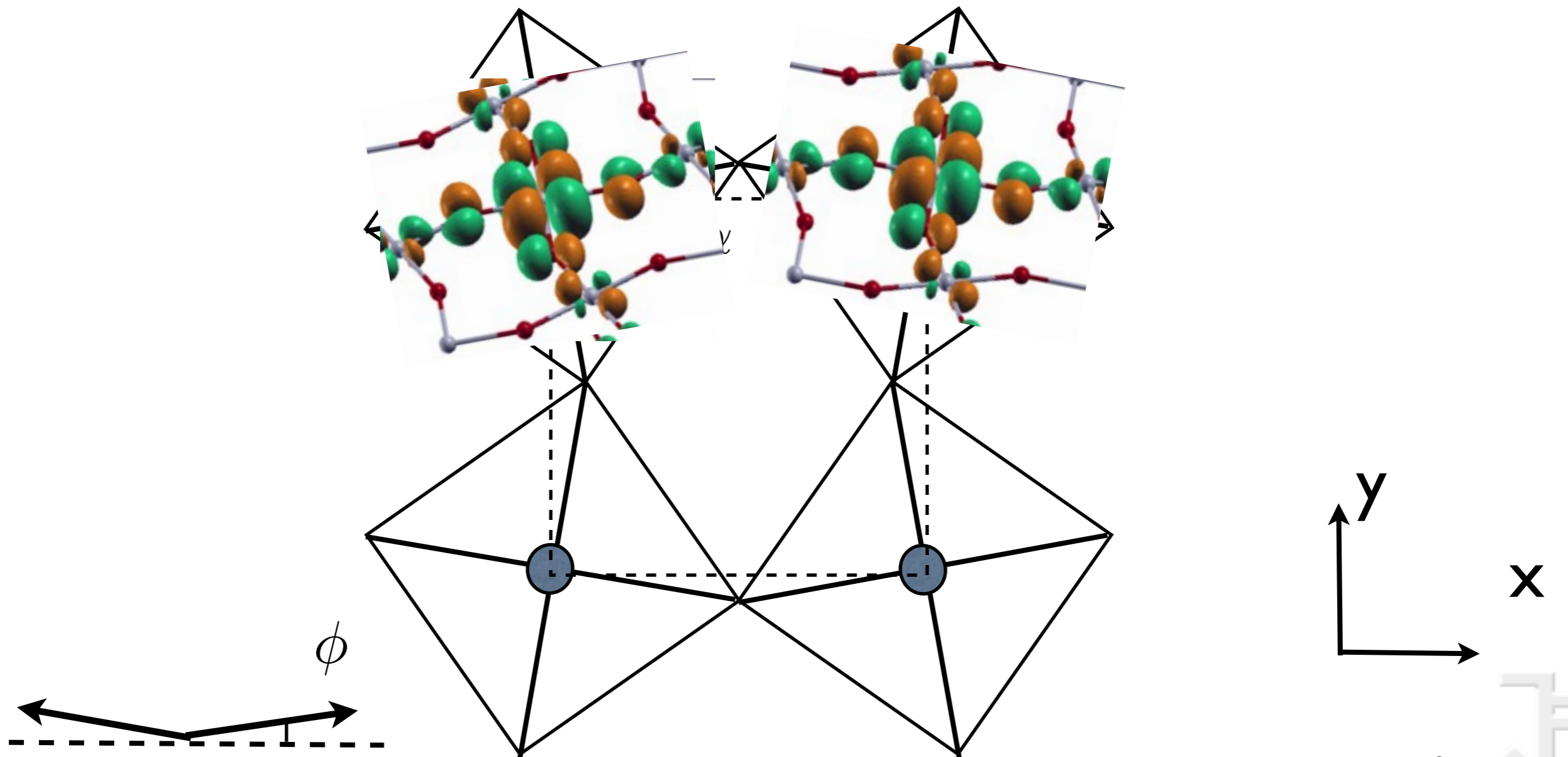




# One-band $J_{\text{eff}}=1/2$ Hubbard model for $\text{Sr}_2\text{IrO}_4$

$$\mathcal{H} = \sum_{\langle ij \rangle m_j} t_{ij} d_{im_j}^+ d_{jm_j} + U \sum_i n_{im_j=+1/2} n_{im_j=-1/2}$$

$$|j_{\text{eff}} = 1/2, \pm 1/2\rangle = \mp \frac{1}{\sqrt{3}} |xy\rangle |\pm\rangle - \frac{1}{\sqrt{3}} (|yz\rangle \pm i|zx\rangle) |\mp\rangle$$



# Effective exchange Hamiltonian for the doublet subspace

Rotation of  $\text{IrO}_6$  octahedron by  $\alpha$

$$\mathcal{H}_{ij} = I_0 \mathbf{J}_i \cdot \mathbf{J}_j + I_1 J_{zi} J_{zj} + \mathbf{D}_{ij} \cdot \mathbf{J}_i \times \mathbf{J}_j$$

$$I_0 = 4(\bar{t}_0^2 - \bar{t}_1^2)/\bar{U}$$

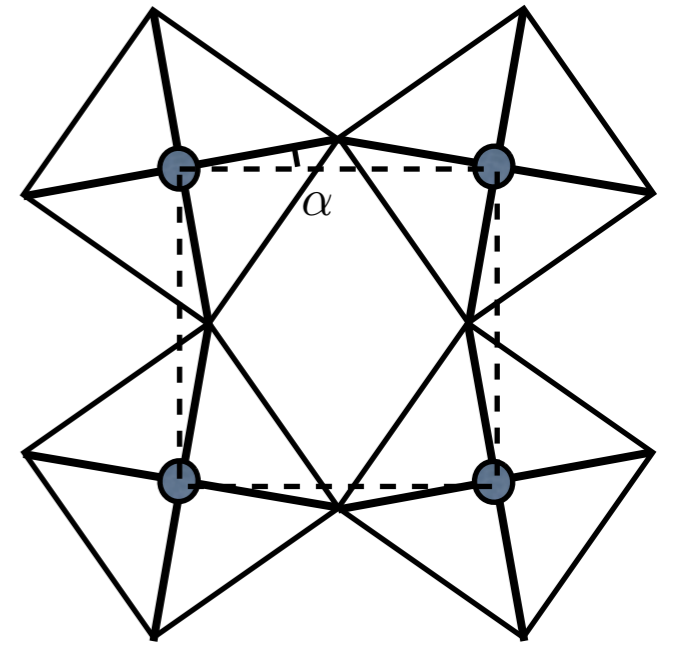
$$\mathbf{D}_{ij} = D_z \hat{\mathbf{z}}$$

$$I_1 = 8\bar{t}_1^2/\bar{U}$$

$$D_z = 8\bar{t}_0\bar{t}_1/\bar{U}$$

$$\bar{t}_0 \approx \frac{2t_0}{3} \quad \bar{t}_1 \approx -\frac{2t_0}{3} \sin \alpha$$

Dzyaloshinskii-Moriya interaction:  $\left| \frac{D_z}{I_0} \right| \approx \left| \frac{2t_1}{t_0} \right| \sim 2\alpha$



# Effective Pseudo-Spin Hamiltonian

$$\begin{aligned}\mathcal{H}_{\text{eff}} &= \langle \gamma | \mathcal{H}_{\text{SO}} + \mathcal{H}_{\text{SO}} \frac{1}{\varepsilon - \mathcal{H}'} \mathcal{H}_{\text{SO}} + \dots | \gamma \rangle \\ &= \sum_{i\mu, j\nu} d_{i\mu, j\nu} J_{i\mu} J_{j\nu} + \dots\end{aligned}$$

Unquenched orbital degrees of freedom:  
 $J_{\text{eff}} = 1/2$  state

$$\mathcal{H}_{\text{eff}} = \sum_{\langle ij \rangle} \vec{D}_{ij} \cdot \vec{S}_i \times \vec{S}_j$$



# Summary

- New form of Mott insulator  $\text{Sr}_2\text{IrO}_4$ :  
spin-orbit entangled  $j_{\text{eff}}=1/2$  ground state
  - ✓ Strong anisotropic magnetic interactions:  
Dzyaloshinskii-Moriya interactions driven by the  $J_{\text{eff}}=1/2$  state
- Proximity to spin-orbit or topological insulator in  $\text{Na}_2\text{IrO}_3$ 
  - ✓ Not  $j_{\text{eff}}=1/2$  but SO-entangled  $e_g'$  state
  - ✓ AFM insulator with strong anisotropy
- Both on-site Coulomb and spin-orbit interactions contribute to the non-trivial spin and orbital orderings.

